

Digital Beamforming and MIMO-SAR Systems

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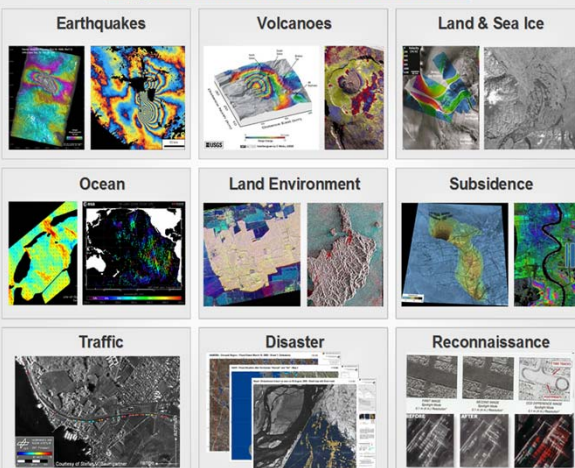
Microwaves and Radar Institute

Oberpfaffenhofen



Future SAR Systems: Motivation

Application Areas for SAR Data



Future Demands

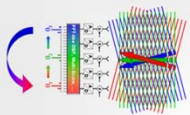
- wider coverage and shorter revisit times
- higher geometric and radiometric resolution
- new data products from coherent combinations of SAR images:
 - Delta-DEMs (ice mass balance, ...)
 - 3-D volume imaging (forest structure, ...)
 - 4-D tomography (biomass dynamics, ...)
- reliable data supply
- cost efficiency



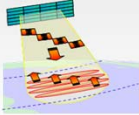
Future SAR Systems: Motivation

New SAR Techniques and Technologies

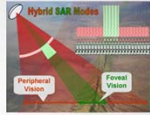
Digital Beamforming



MIMO-SAR

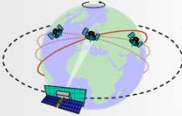


Hybrid & Adaptive SAR

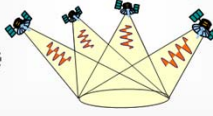


New Data Acquisition Concepts

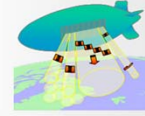
GEO - MEO - LEO



Sparse Satellite Arrays

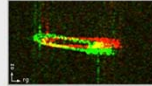


Novel Platforms

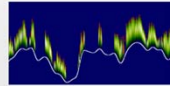


New Retrieval Algorithms and Products

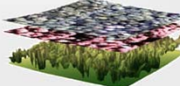
Object Dynamics



3-D & 4-D Structure



Data Fusion



Future Demands

- wider coverage and shorter revisit times
- higher geometric and radiometric resolution
- new data products from coherent combinations of SAR images:
 - Delta-DEMs (ice mass balance, ...)
 - 3-D volume imaging (forest structure, ...)
 - 4-D tomography (biomass dynamics, ...)
- reliable data supply
- cost efficiency

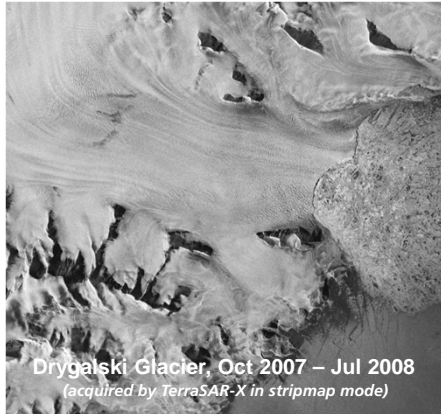


SAR System Design Constraints

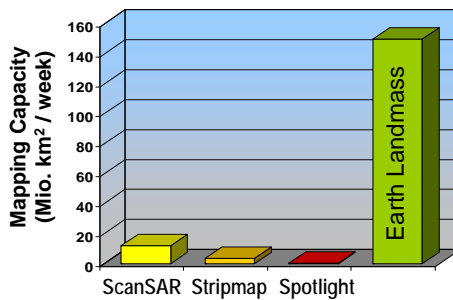


Limitations of Conventional SAR Sensors

SAR is the ideal sensor for the observation of dynamic processes on the Earth surface, but ...



	Imaging Mode (Single Pol.)		
	ScanSAR	Stripmap	Spotlight
Resolution	16 m	3 m	1 m
Swath Width	100 km	30 km	10 km
Duty Cycle	3 minutes / orbit		

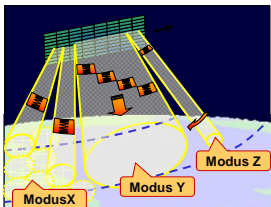


SAR Systems: State of the Art and Future Requirements



State of the Art (TerraSAR-X)	Imaging Mode (single pol.)		
	ScanSAR	Stripmap	Spotlight
Resolution	16 m	3 m	1 m
Swath Width	100 km	30 km	10 km
Orbit Duty Cycle	3 minutes per orbit		

Resolution ↔ **Swath Width** ↔ **Repeat Cycle**



Future Requirements	Imaging Mode (quad pol.)		
	Mode X	Mode Y	Mode Z
Resolution	5 m	2 m	1 m
Swath Width	500 km	200 km	100 km
Orbit Duty Cycle	> 50 minutes per orbit		

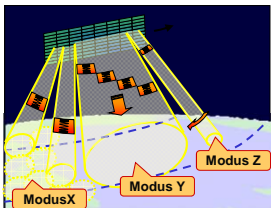


SAR Systems: State of the Art and Future Requirements



State of the Art (Sentinel-1)	Imaging Mode (single/dual pol.)		
	EW	IW	SM
Resolution	40 m	20 m	5 m
Swath Width	400 km	250 km	80 km
Orbit Duty Cycle	25 minutes per orbit		

Resolution ↔ **Swath Width** ↔ **Repeat Cycle**



Future Requirements	Imaging Mode (quad pol.)		
	Mode X	Mode Y	Mode Z
Resolution	5 m	2 m	1 m
Swath Width	500 km	200 km	100 km
Orbit Duty Cycle	> 50 minutes per orbit		

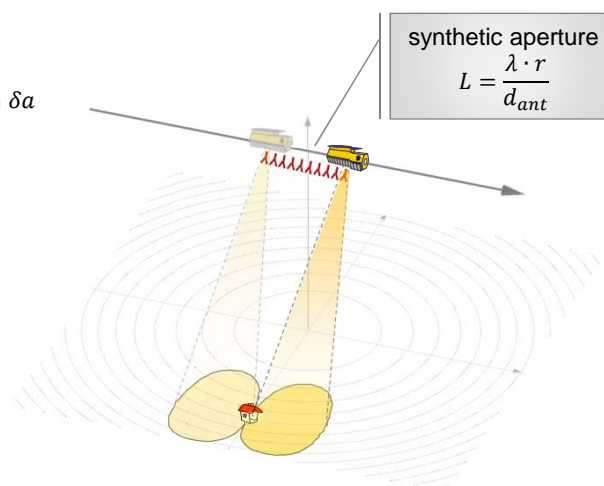


SAR System Design Constraints (1)

high azimuth resolution

- high azimuth resolution δa requires long synthetic aperture L :

$$\delta a = \frac{\lambda \cdot r}{2 L} = \frac{d_{ant}}{2}$$



SAR System Design Constraints (2)

high azimuth
resolution

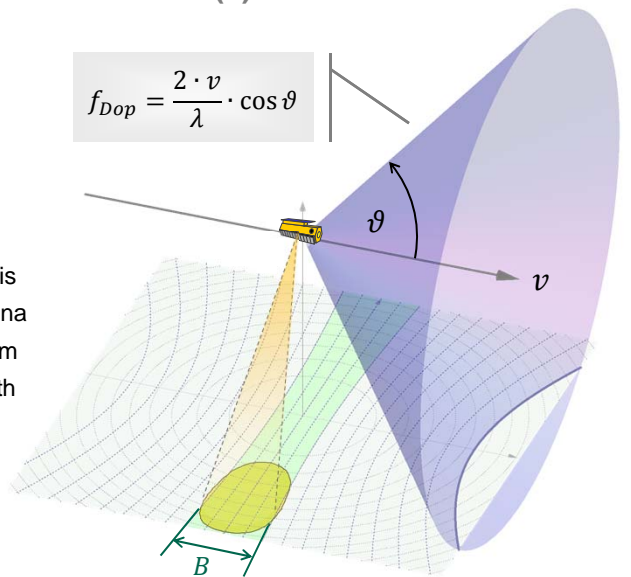
large Doppler
bandwidth

- long synthetic aperture is provided by short antenna with broad azimuth beam
- large azimuth beamwidth implies wide Doppler spectrum:

$$B = \frac{2 \cdot v}{d_{ant}} = \frac{v}{\delta a}$$



$$f_{Dop} = \frac{2 \cdot v}{\lambda} \cdot \cos \vartheta$$



SAR System Design Constraints (3)

high azimuth
resolution

large Doppler
bandwidth

high PRF

- sampling with PRF causes ambiguities (AASR)
- low AASR requires high PRF:

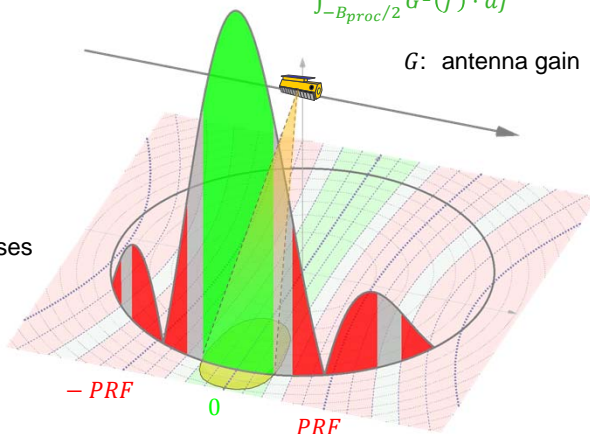
$$PRF > B = \frac{v}{\delta a}$$



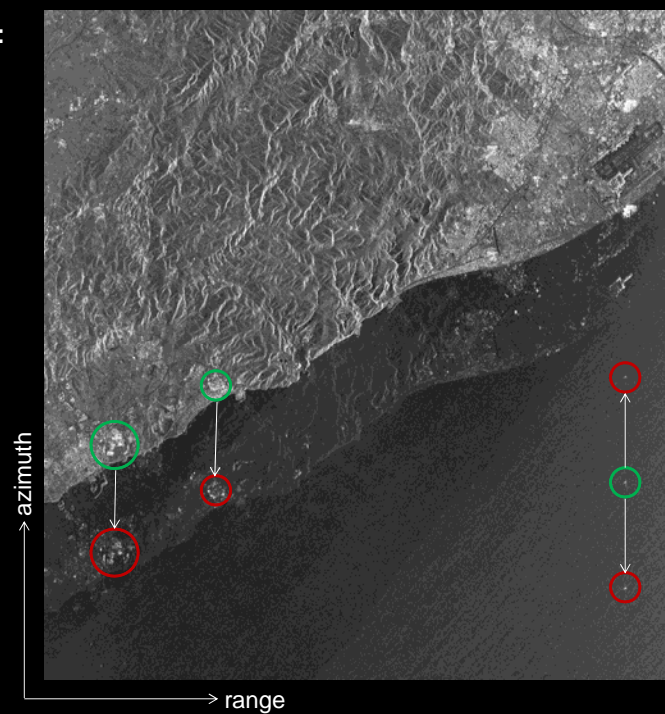
Azimuth Ambiguity-to-Signal Ratio (AASR):

$$AASR = \frac{\sum_{i \neq 0} \int_{-B_{proc}/2}^{B_{proc}/2} G^2(f + i \cdot PRF) \cdot df}{\int_{-B_{proc}/2}^{B_{proc}/2} G^2(f) \cdot df}$$

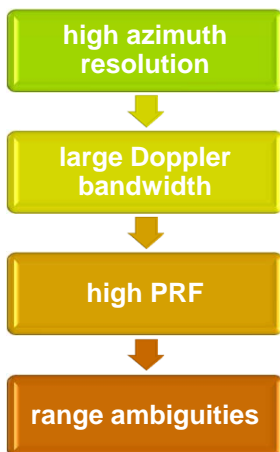
G: antenna gain



Azimuth Ambiguities: Example



SAR System Design Constraints (4)



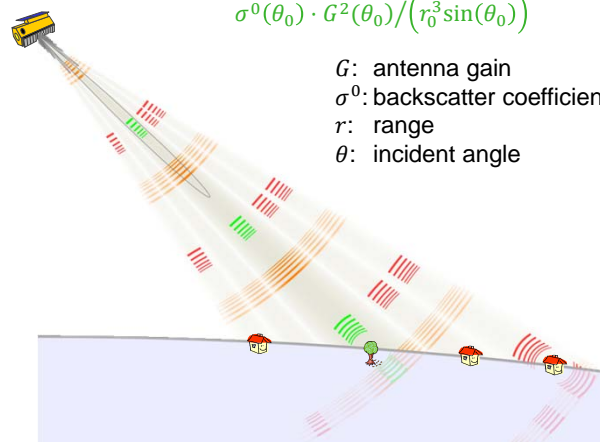
- high PRF causes range ambiguities

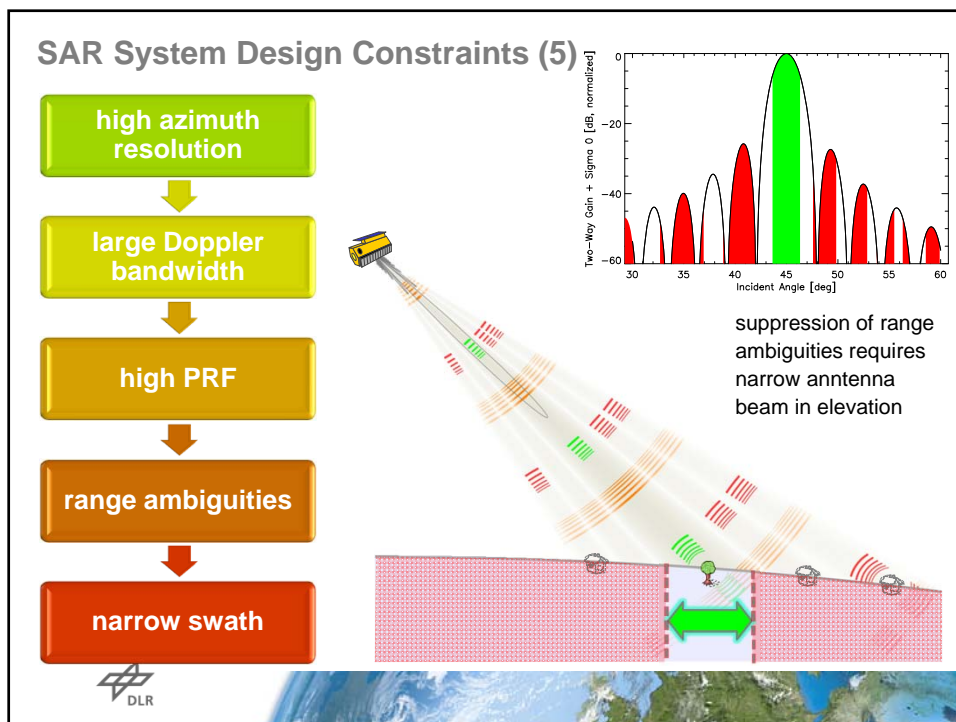
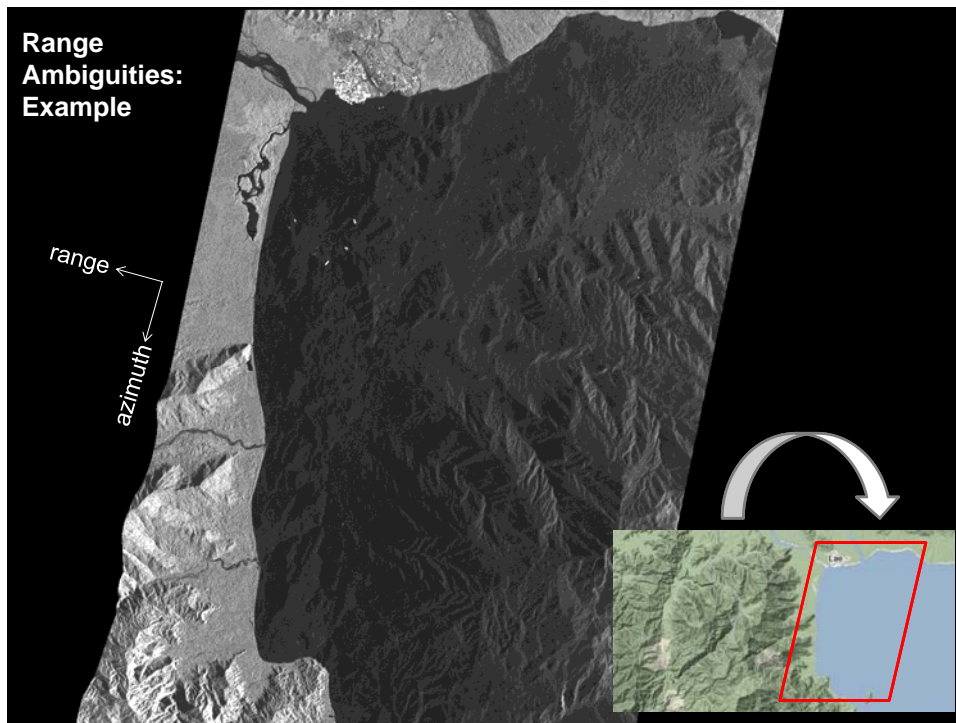


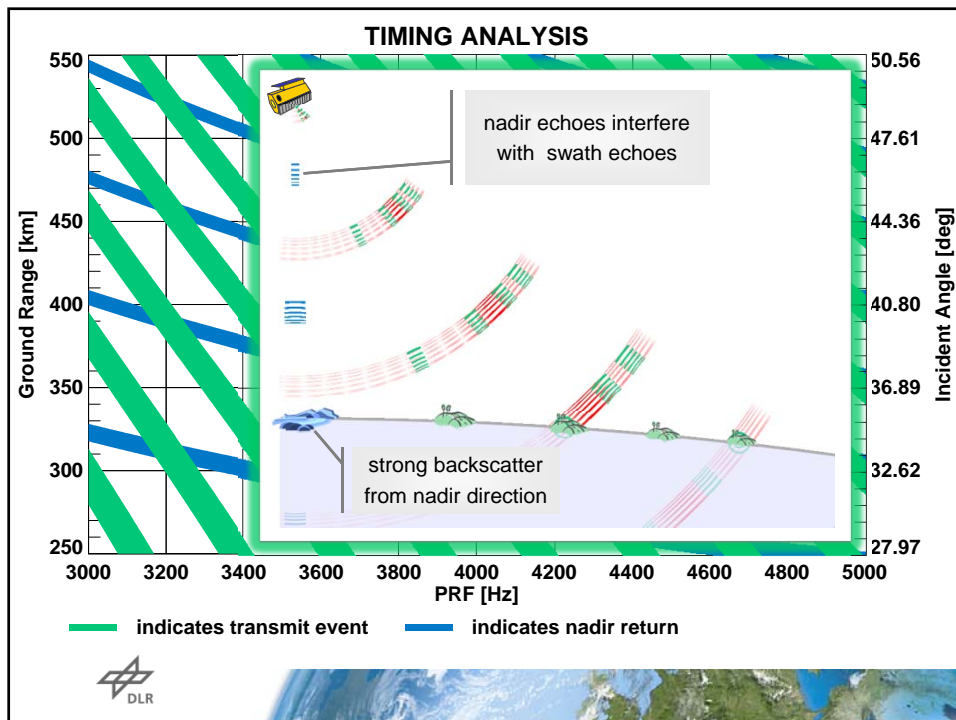
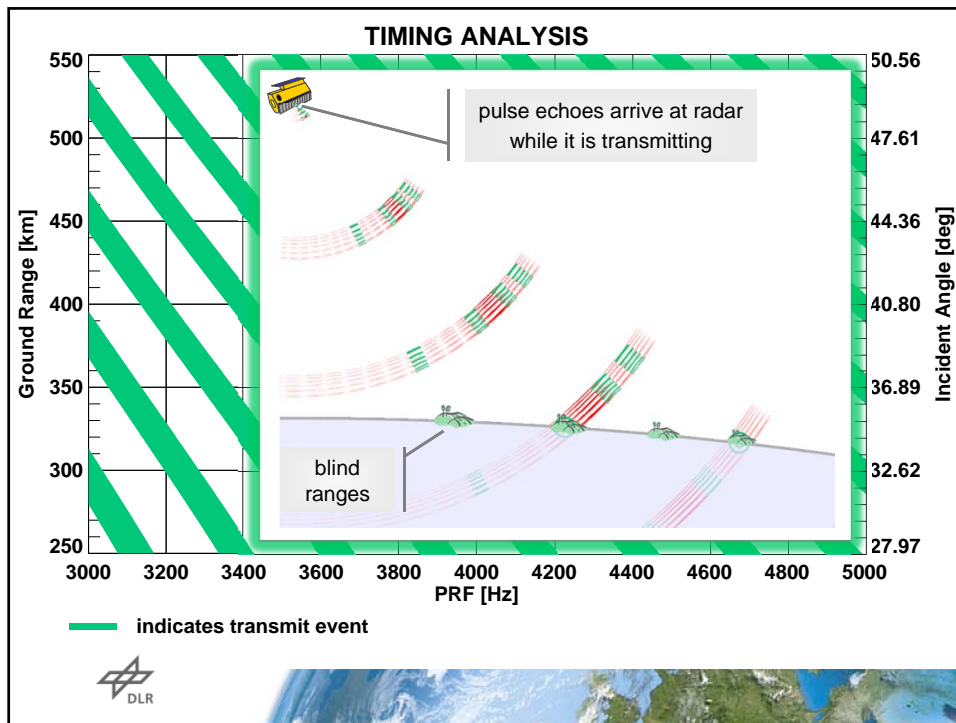
Range Ambiguity-to-Signal Ratio (RASR):

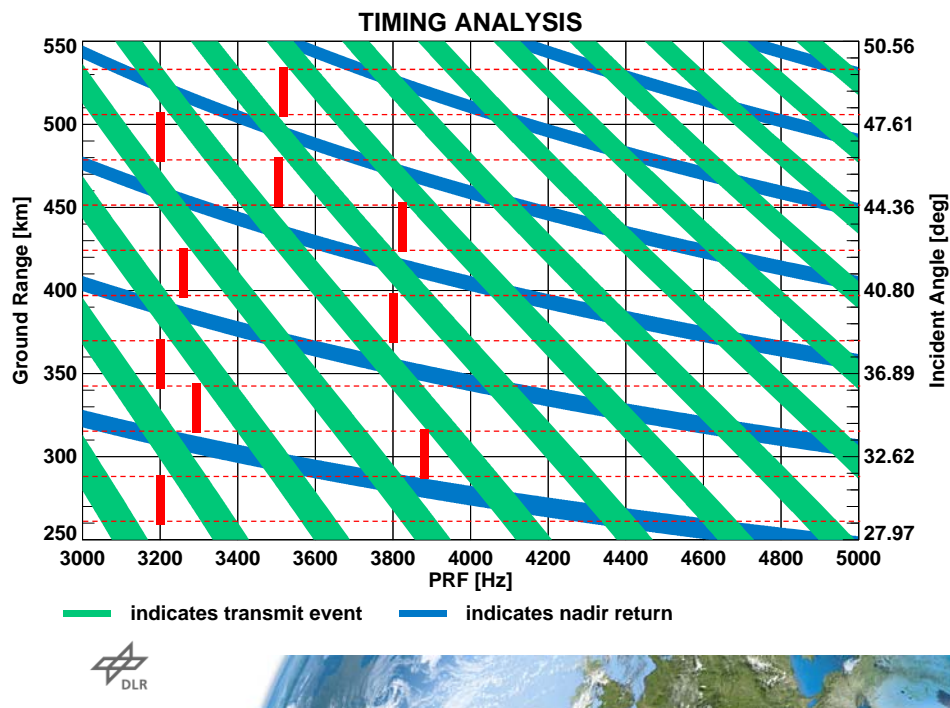
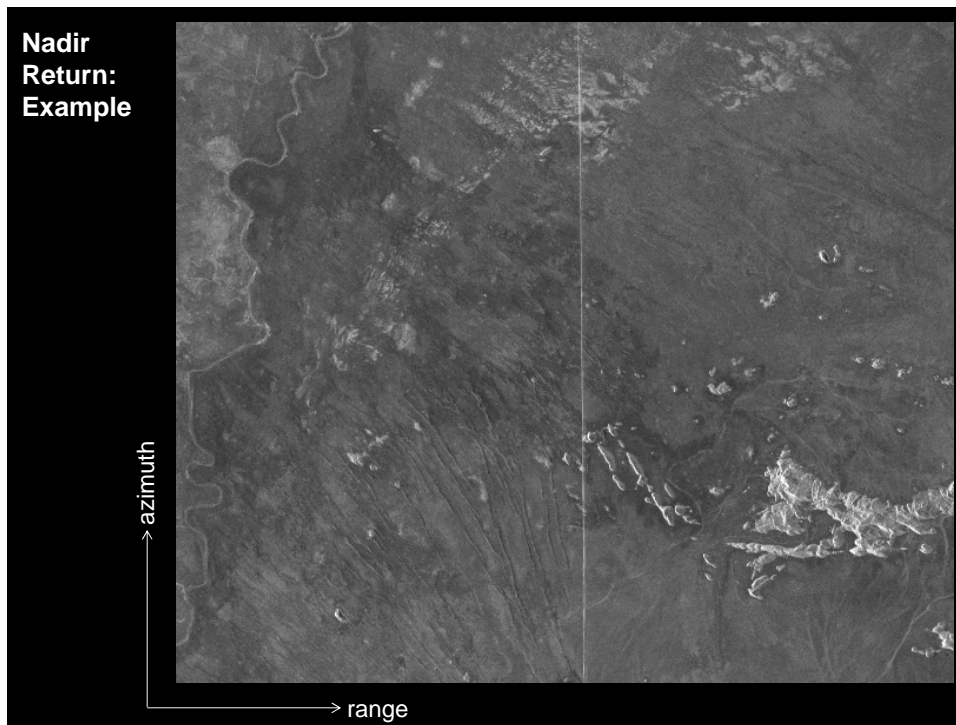
$$RASR = \frac{\sum_{i \neq 0} \sigma^0(\theta_i) \cdot G^2(\theta_i) / (r_i^3 \sin(\theta_i))}{\sigma^0(\theta_0) \cdot G^2(\theta_0) / (r_0^3 \sin(\theta_0))}$$

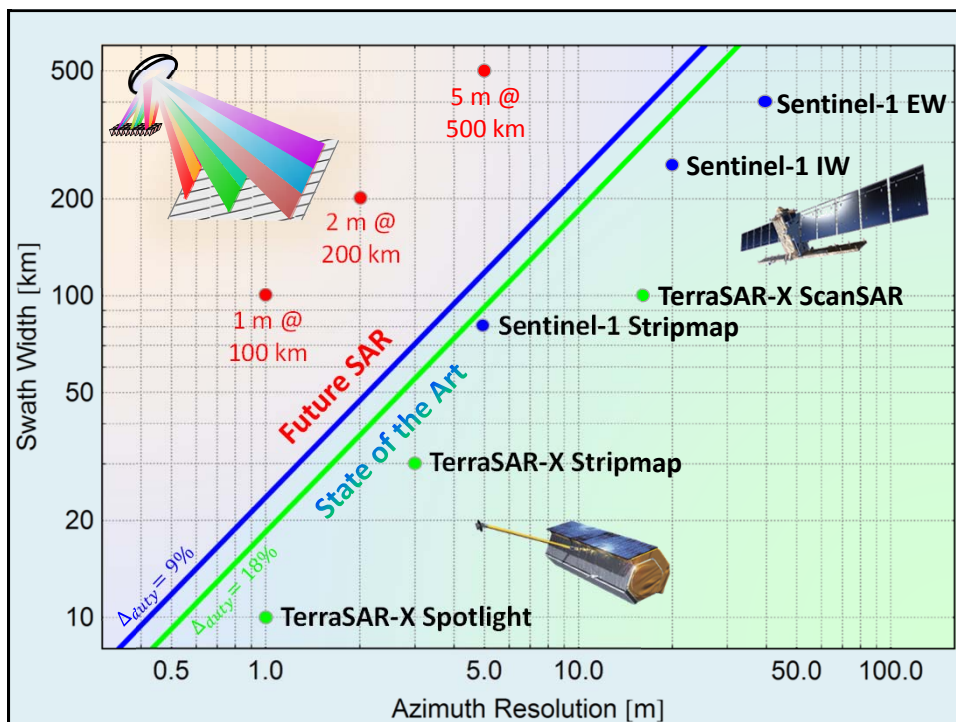
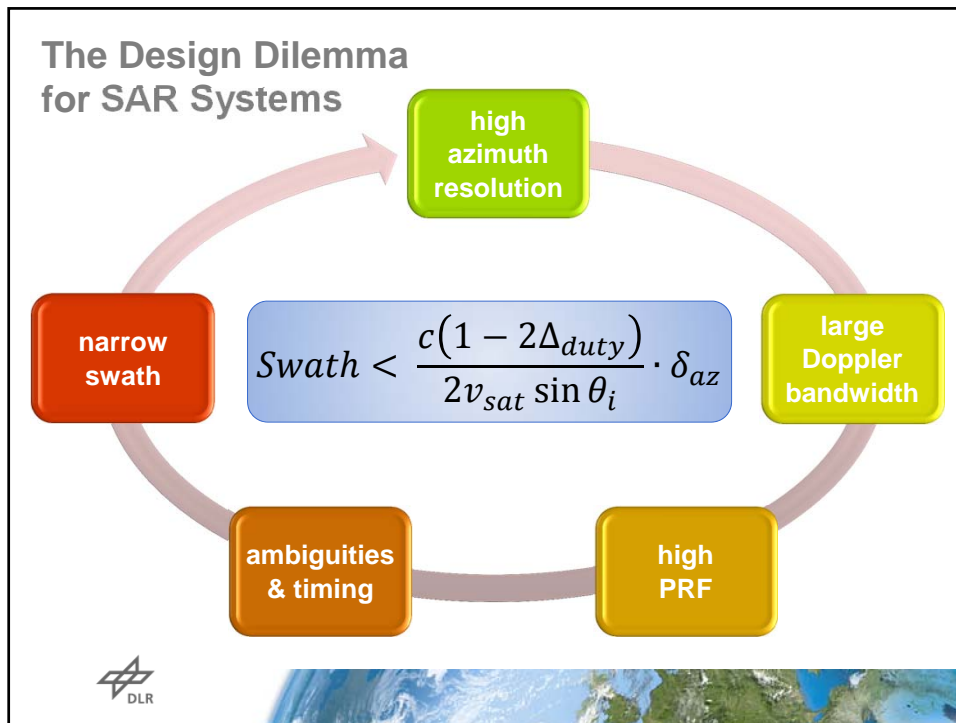
G : antenna gain
 σ^0 : backscatter coefficient
 r : range
 θ : incident angle







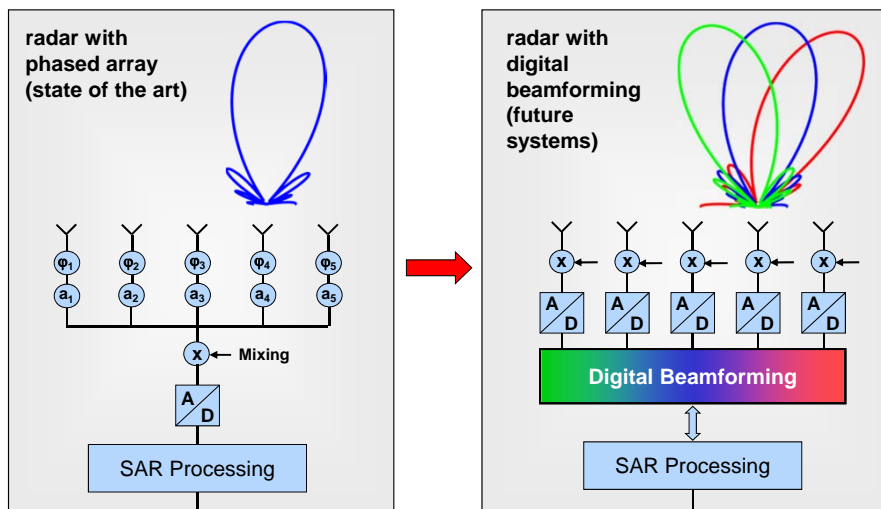




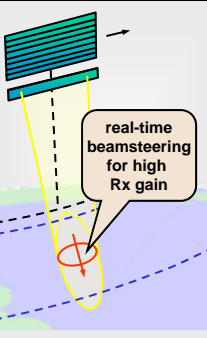
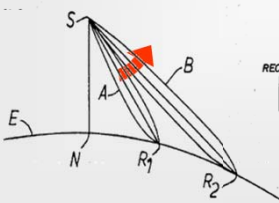
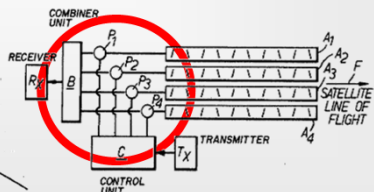
Digital Beamforming for SAR



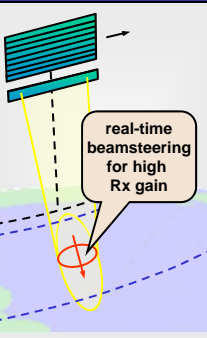
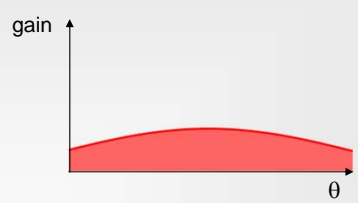


Digital Beamforming / Multichannel SAR

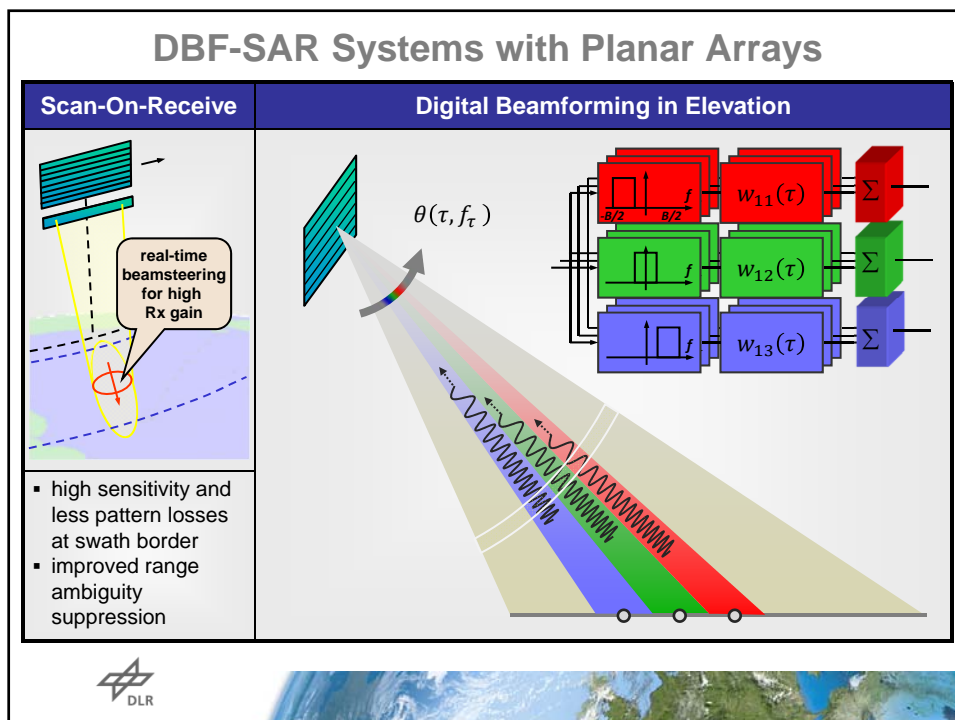
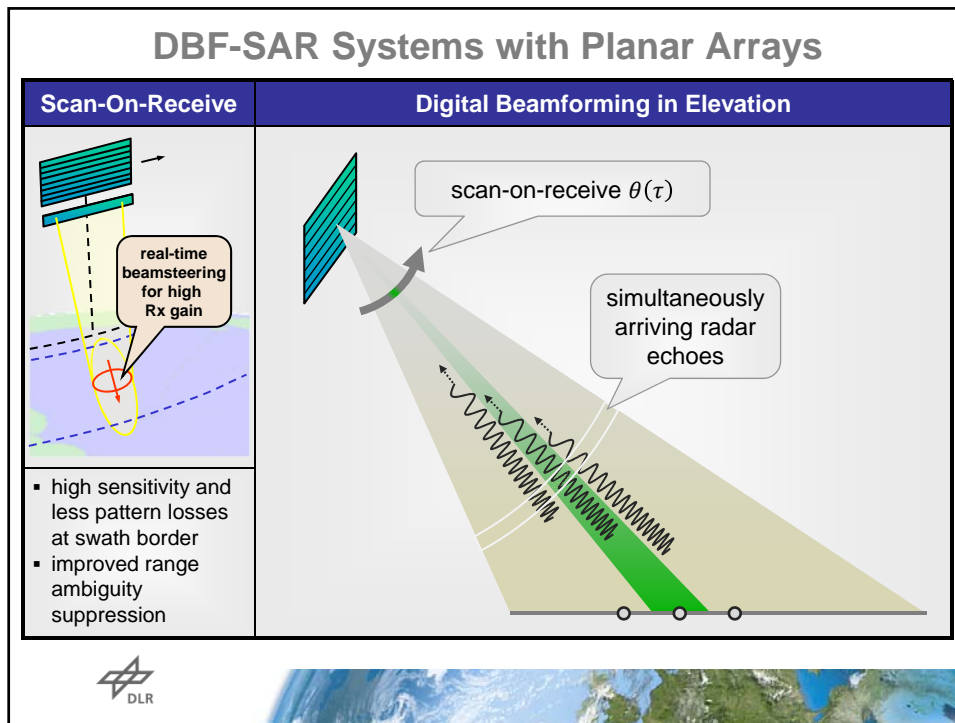


DBF-SAR Systems with Planar Arrays

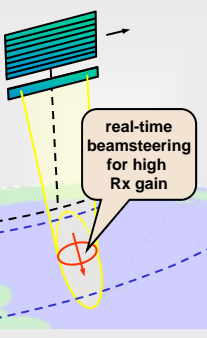


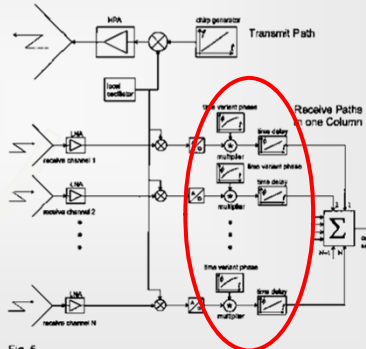
Scan-On-Receive	Digital Beamforming in Elevation
 <p>real-time beamsteering for high Rx gain</p> <ul style="list-style-type: none"> high sensitivity and less pattern losses at swath border improved range ambiguity suppression 	<p>United States Patent [19] 4,253,098</p> <p>Blythe [45] Feb. 24, 1981</p> <p>[54] RADAR SYSTEMS</p> <p>[75] Inventor: John H. Blythe, Chelmsford, England</p> <p>[73] Assignee: The Marconi Company Limited, Chelmsford, England</p> <p>[21] Appl. No.: 77,031</p> <p>[22] Filed: Sep. 19, 1979</p> <p><i>Primary Examiner—T. H. Tubbesing Attorney, Agent, or Firm—Diller, Ramik & Wight</i></p> <p>[57] ABSTRACT</p> <p>A synthetic aperture radar system is provided in which the receive beam is controlled as to its directivity so that it moves over a required swathe in accordance with the direction of reflection of an interrogating radar pulse over that swathe. In a specific example a receiving</p>   <p>J.H. Blythe, Radar Systems, US Patent 4253098, 1981.</p>

DBF-SAR Systems with Planar Arrays

Scan-On-Receive	Digital Beamforming in Elevation
 <p>real-time beamsteering for high Rx gain</p> <ul style="list-style-type: none"> high sensitivity and less pattern losses at swath border improved range ambiguity suppression 	 <p>gain</p> <p>θ</p> <p>steering law</p>  

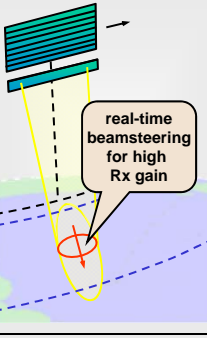
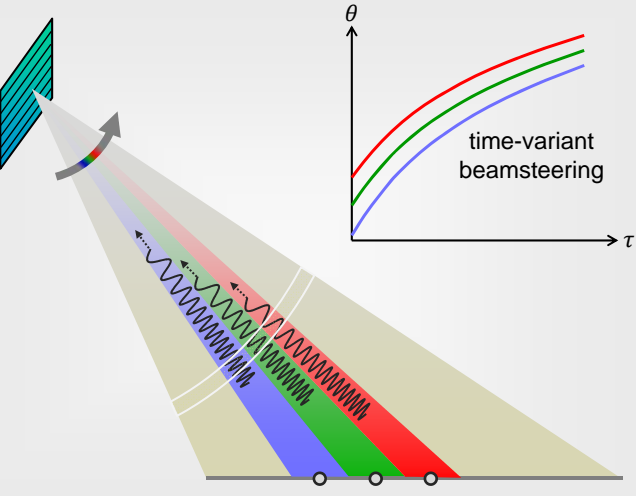


DBF-SAR Systems with Planar Arrays

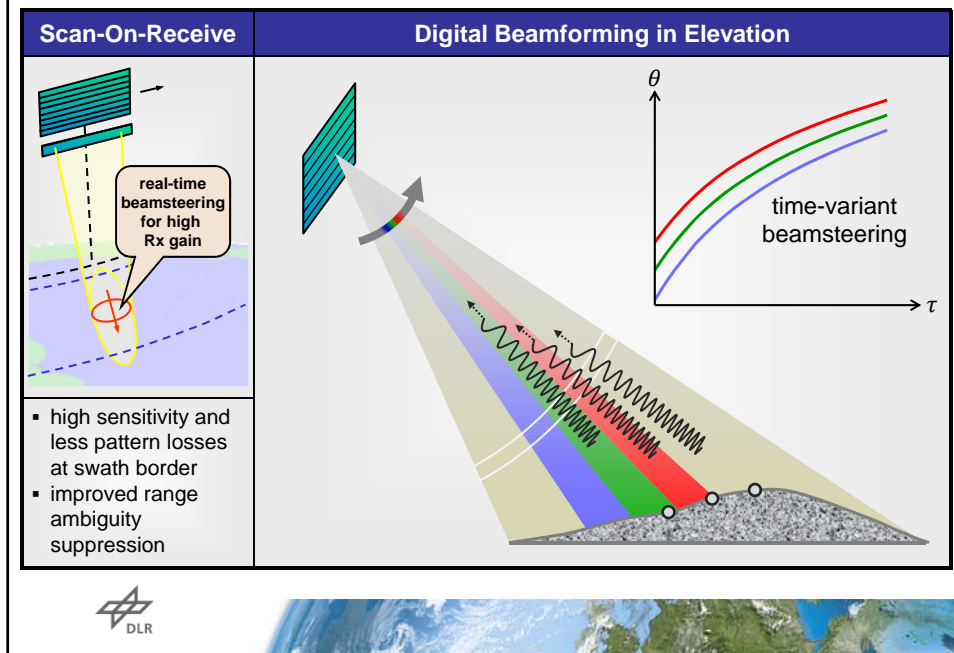
Scan-On-Receive	Digital Beamforming in Elevation
 <ul style="list-style-type: none"> high sensitivity and less pattern losses at swath border improved range ambiguity suppression 	<div style="display: flex; justify-content: space-between;"> <div> <p>Europäisches Patentamt European Patent Office Office européen des brevets</p> <p>(19) </p> <p>(12) EUROPEAN PATENT SPECIFICATION</p> <p>(45) Date of publication and mention of the grant of the patent: 08.02.2006 Bulletin 2006/06</p> <p>(21) Application number: 01106289.0</p> <p>(22) Date of filing: 15.03.2001</p> <p>(54) Side-looking synthetic aperture radar system Seitensichttradersystem mit synthetischer Apertur Système radar à visée latérale et à synthèse d'ouverture</p> <p>(84) Designated Contracting States: AT BE CH CY DE DK ES FI FR GB GR IE IT LI LU MC NL PT SE TR</p> <p>(43) Date of publication of application: 18.09.2002 Bulletin 2002/38</p> <p>(73) Proprietor: EADS Astrium GmbH 81663 München (DE)</p> <p>(72) Inventors: • Süss, Martin 88682 Salem (DE) • Wiesbeck, Werner, Prof. Dr. 75210 Kaisers-Ebernoldingen (DE)</p> <p>(74) Representative: Ullrich, Thomas EADS Deutschland GmbH Patentabteilung LG-SP 81663 Ottobrunn (DE)</p> </div> <div> <p>(11) EP 1 241 487 B1</p>  <p>Fig. 5</p>  </div> </div>

M. Süss et al., A novel high resolution, wide swath SAR system, Proc. IGARSS, pp. 1013-15, 2001.

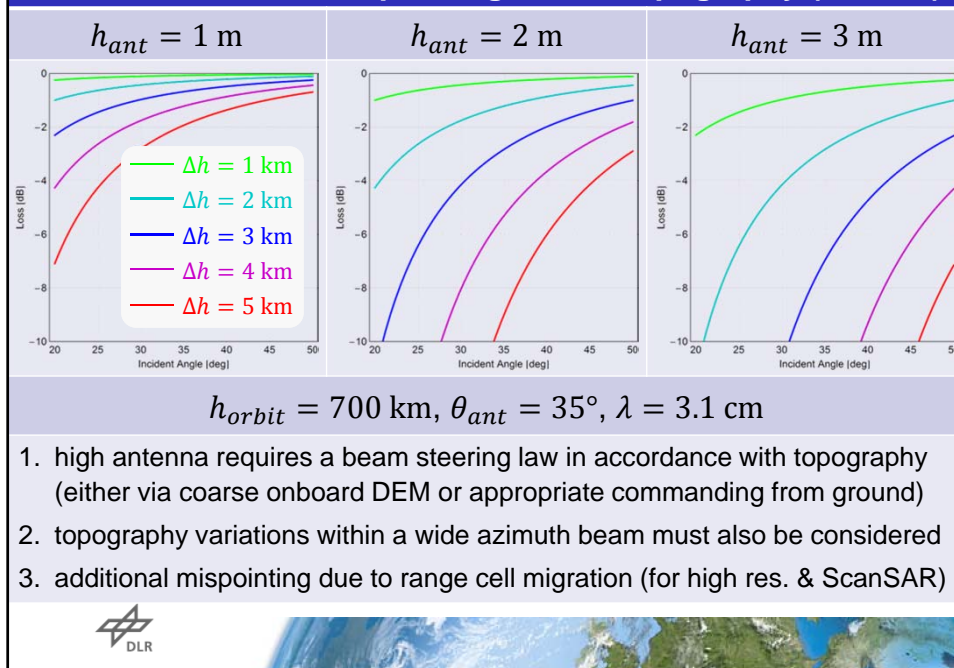
DBF-SAR Systems with Planar Arrays

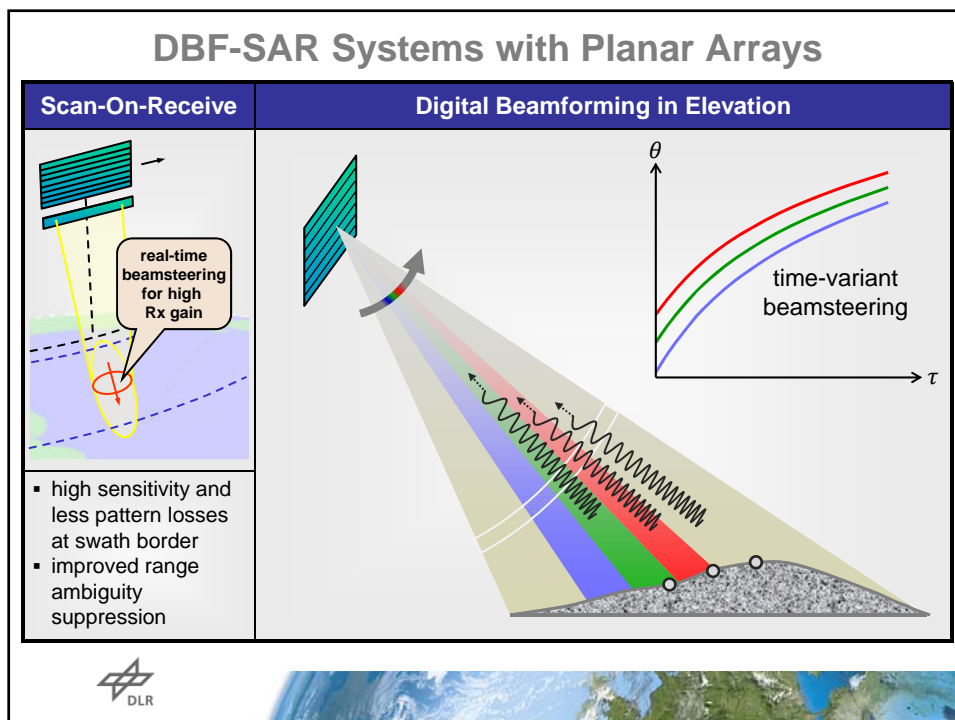
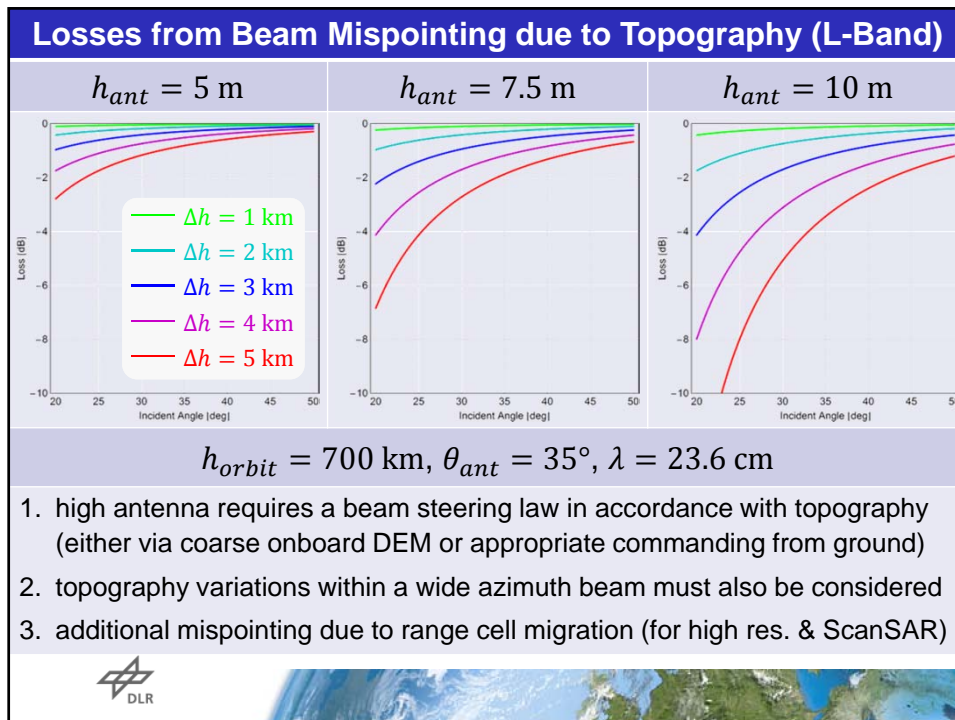
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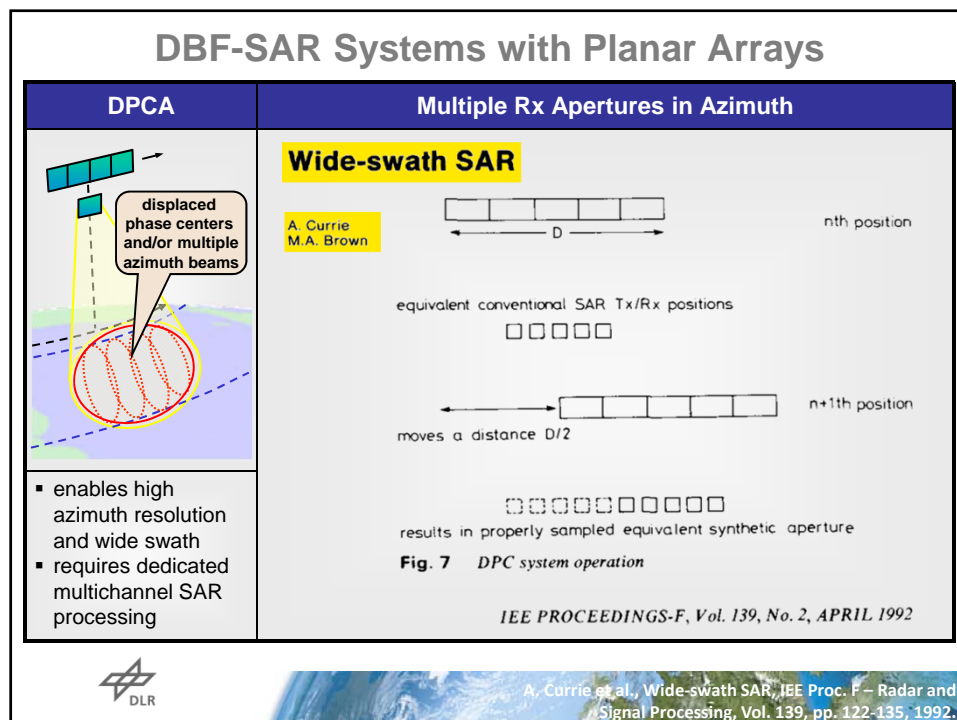
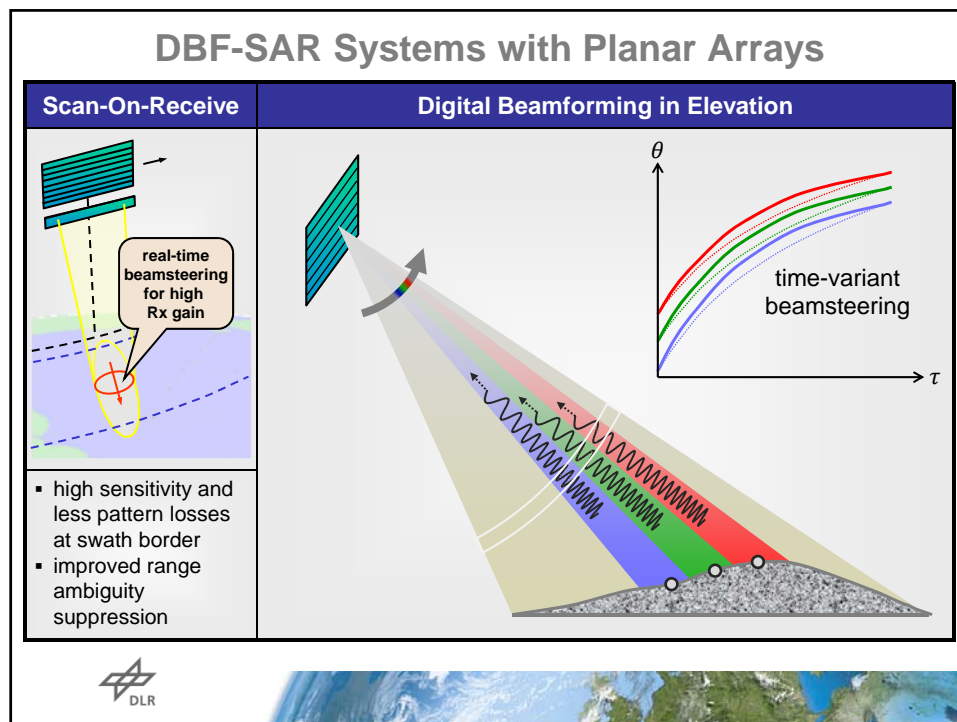
DBF-SAR Systems with Planar Arrays



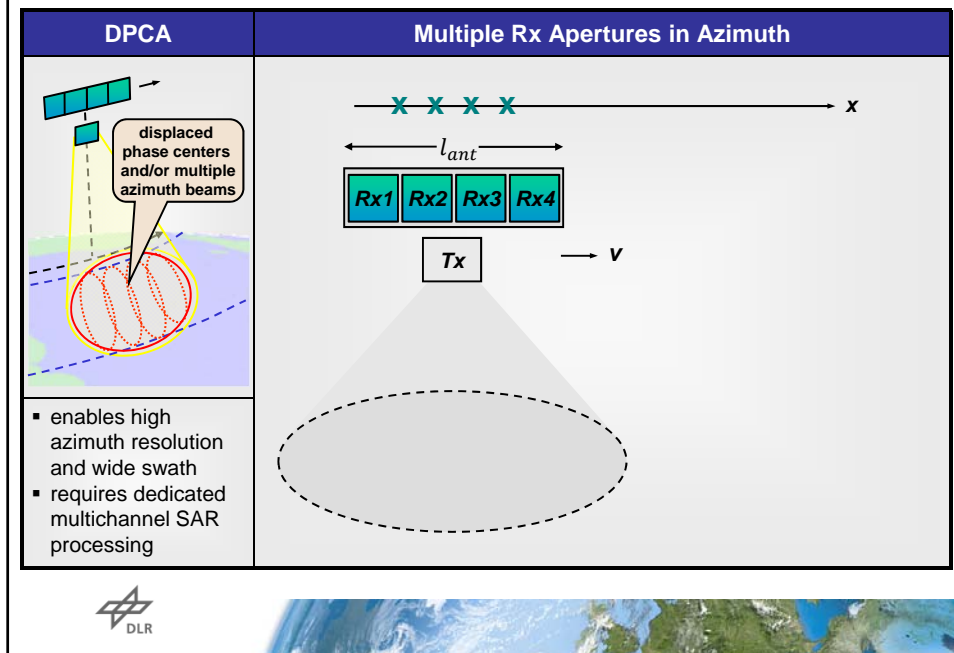
Losses from Beam Mispointing due to Topography (X-Band)



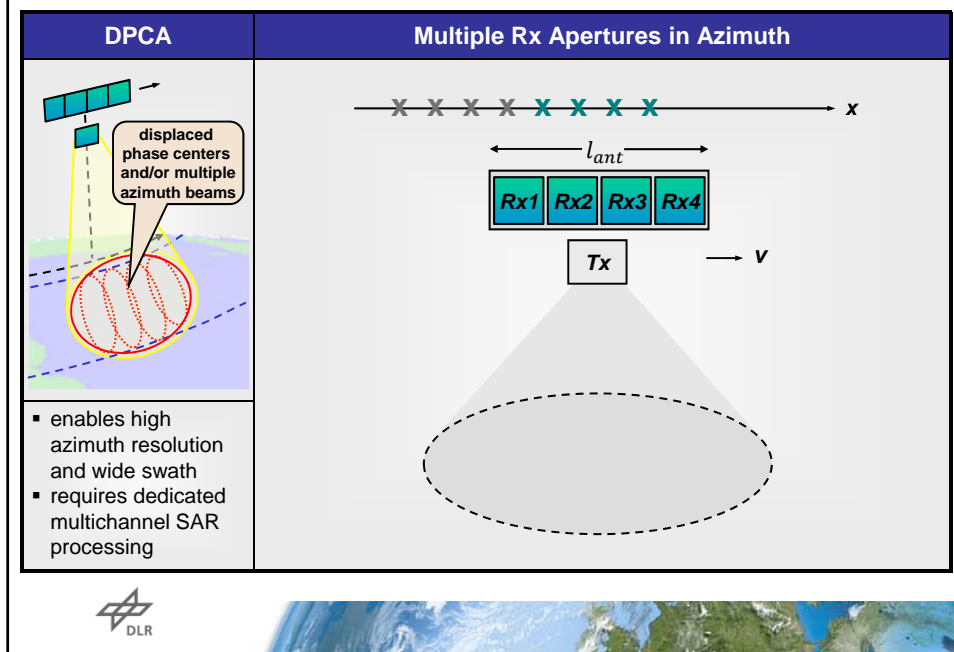


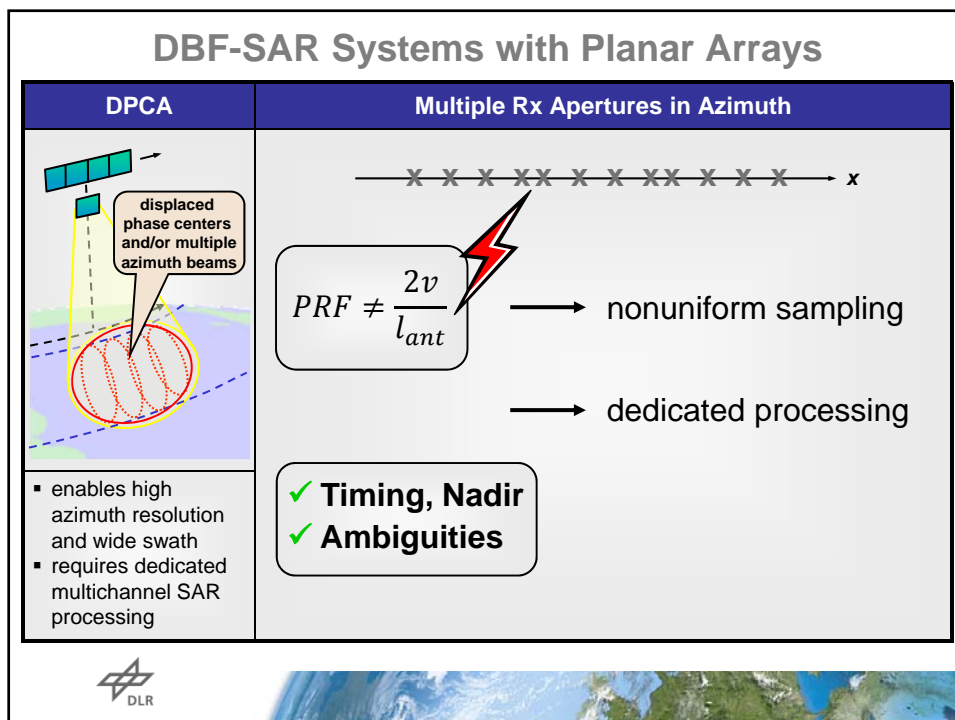
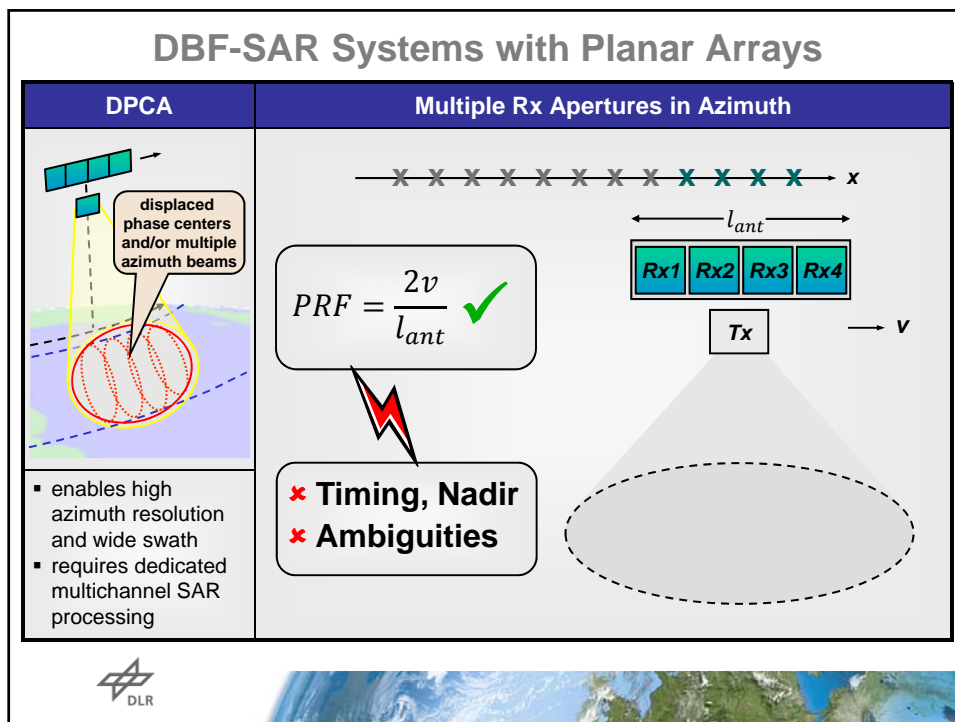


DBF-SAR Systems with Planar Arrays

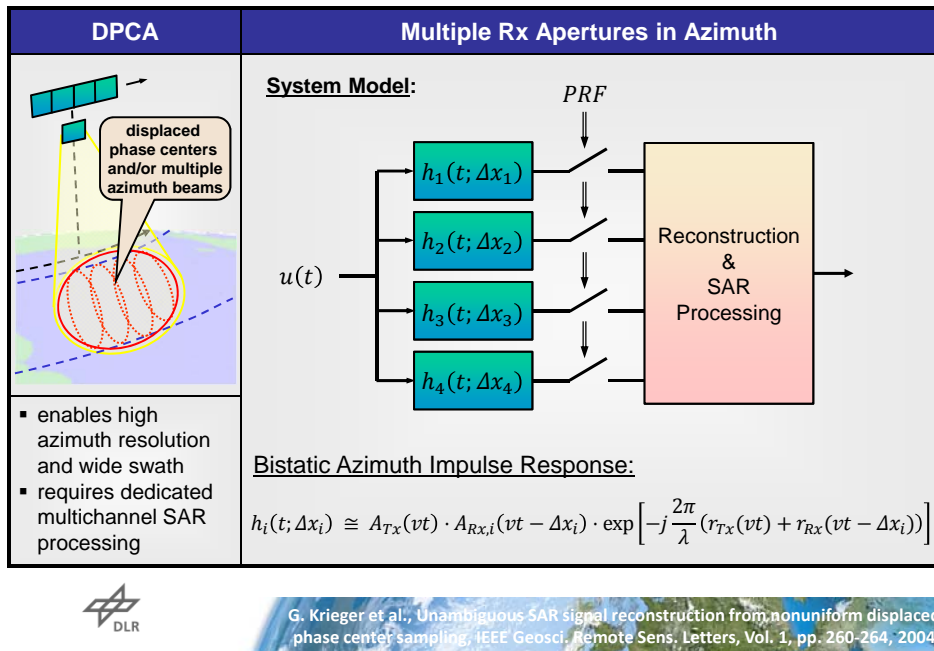


DBF-SAR Systems with Planar Arrays

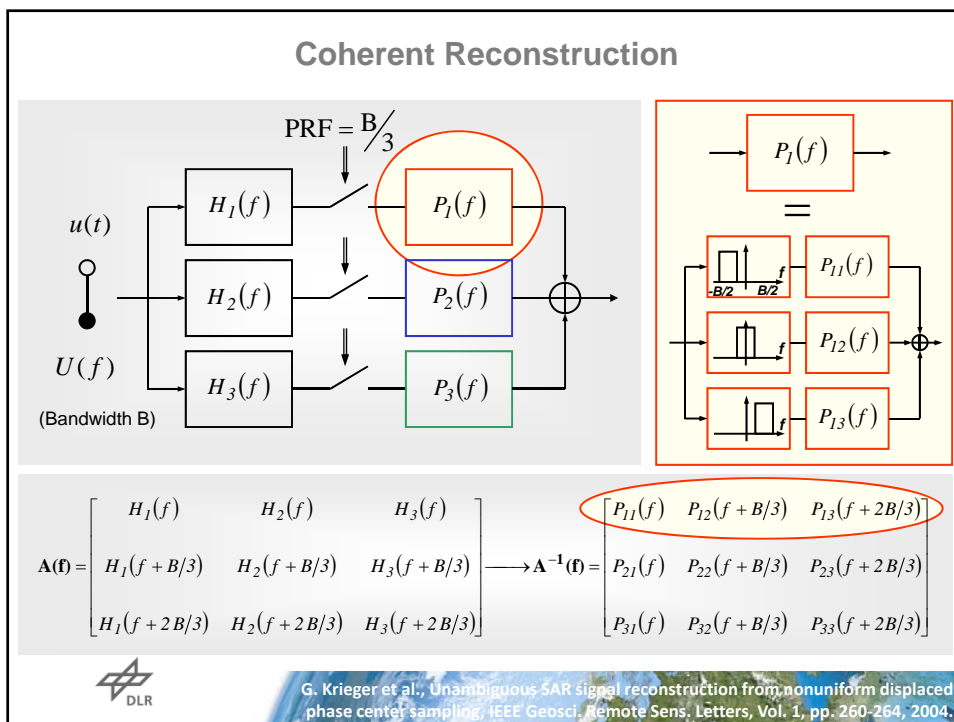




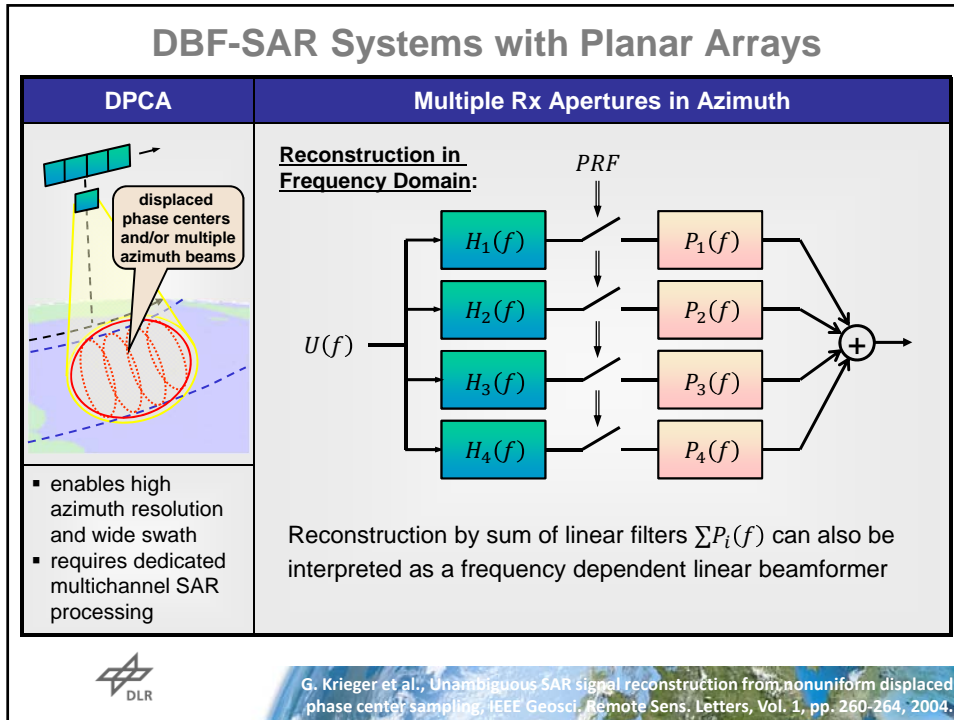
DBF-SAR Systems with Planar Arrays



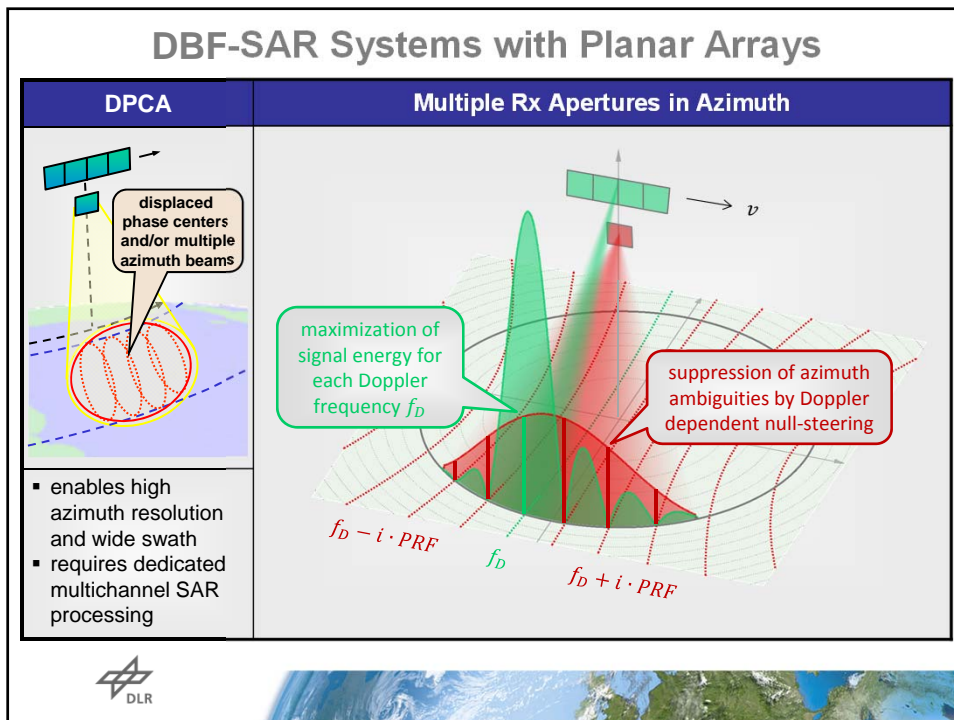
Coherent Reconstruction



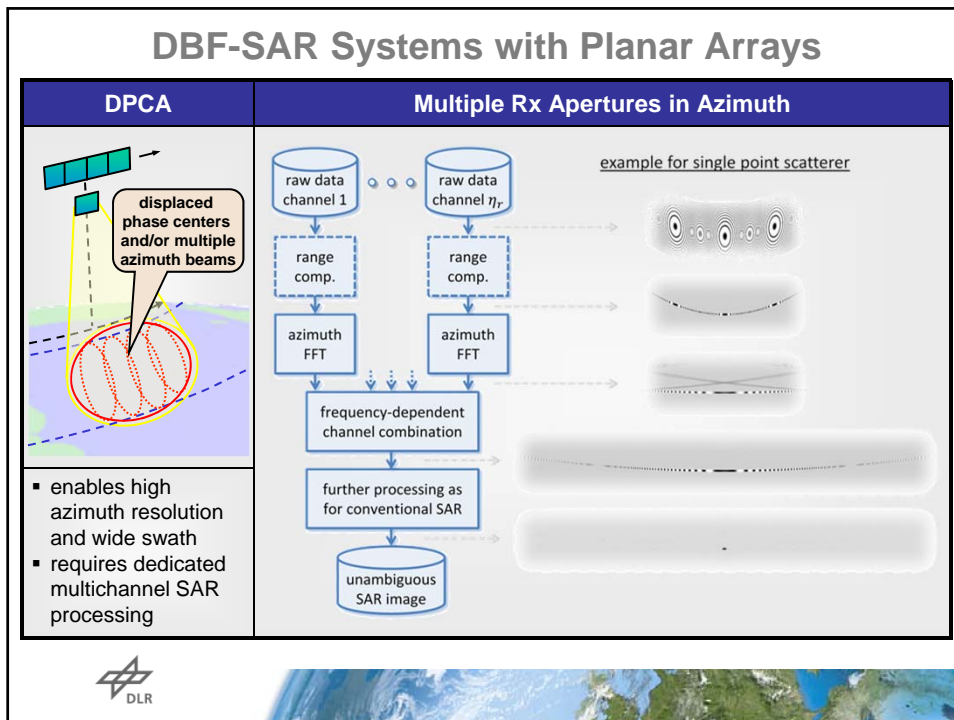
DBF-SAR Systems with Planar Arrays



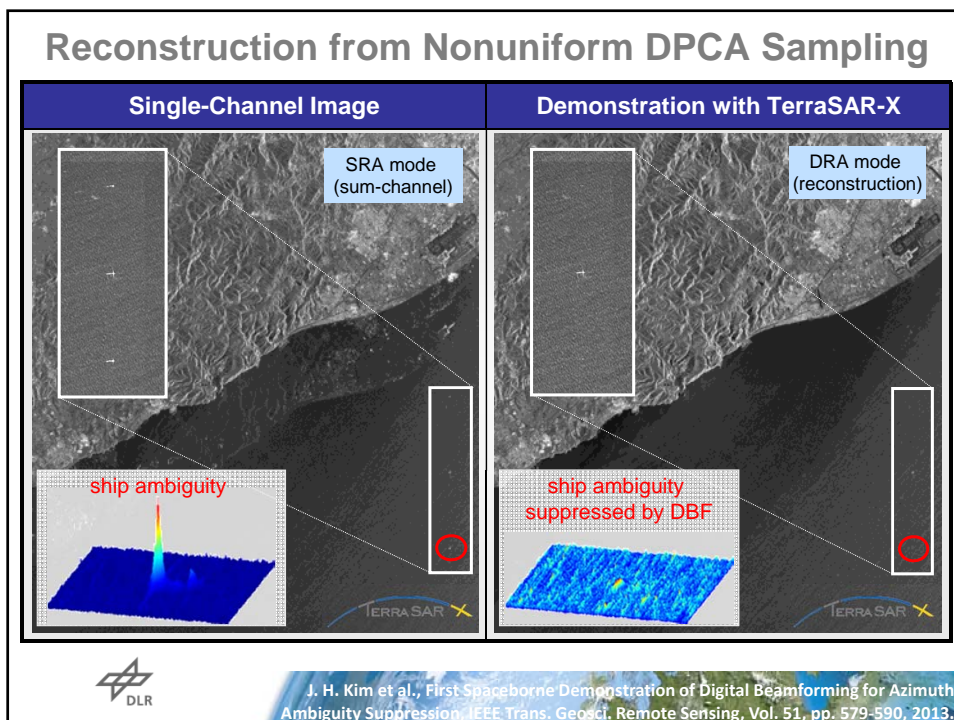
DBF-SAR Systems with Planar Arrays



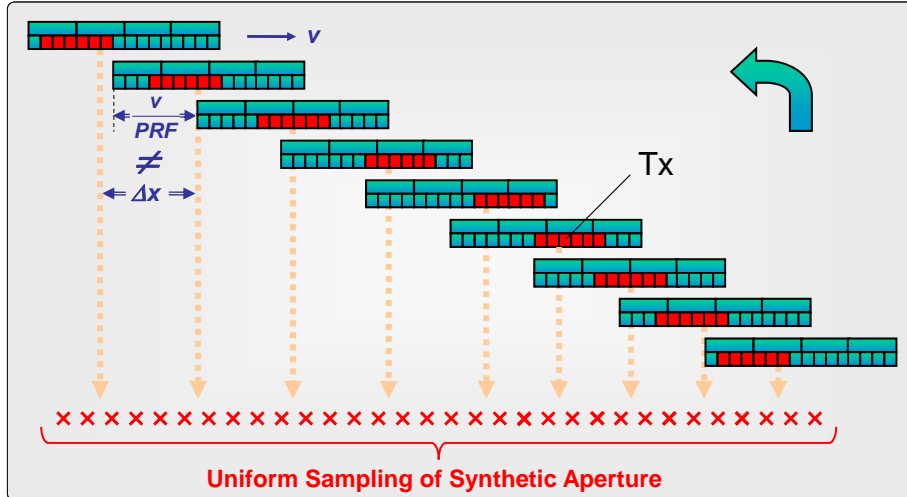
DBF-SAR Systems with Planar Arrays



Reconstruction from Nonuniform DPCA Sampling

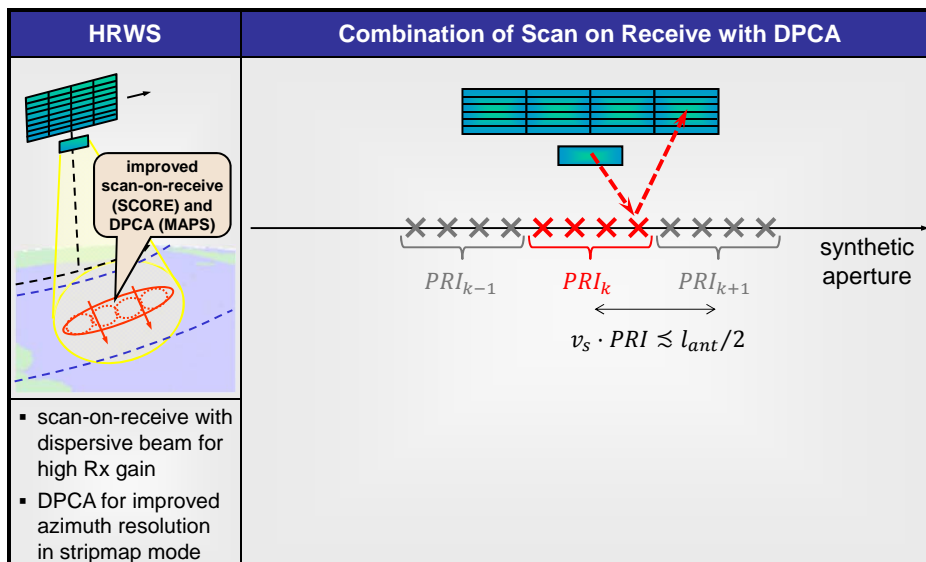


Pulse-to-Pulse Antenna Phase Center Variation



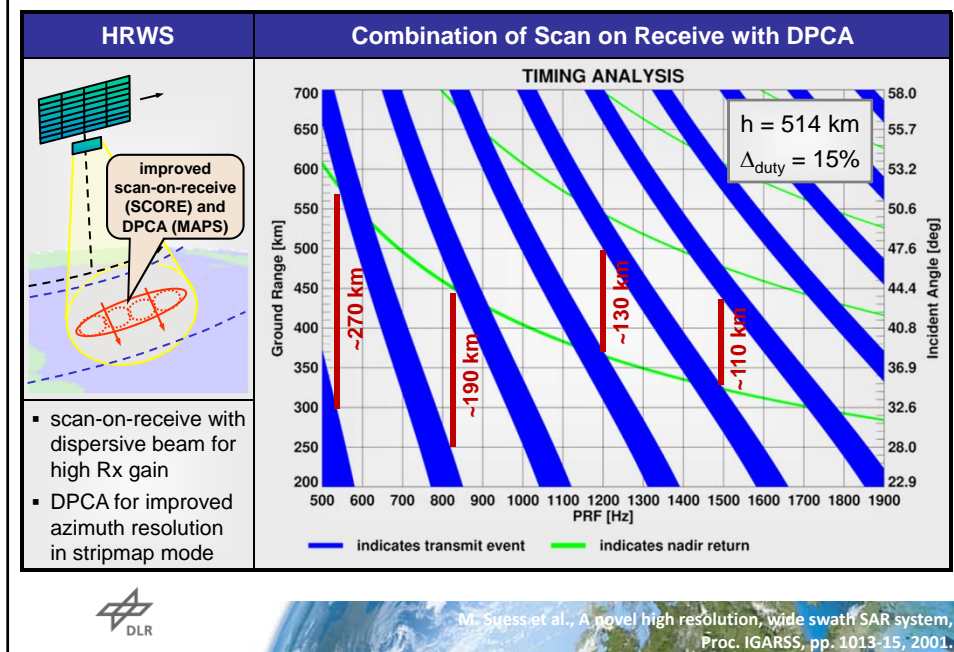
N. Gebert et al., Azimuth Phase Center Adaptation on Transmit for High-Resolution Wide-Swath SAR Imaging, IEEE Geosci. Remote Sens. Letters, Vol. 6, pp. 782-786, 2009.

DBF-SAR Systems with Planar Arrays

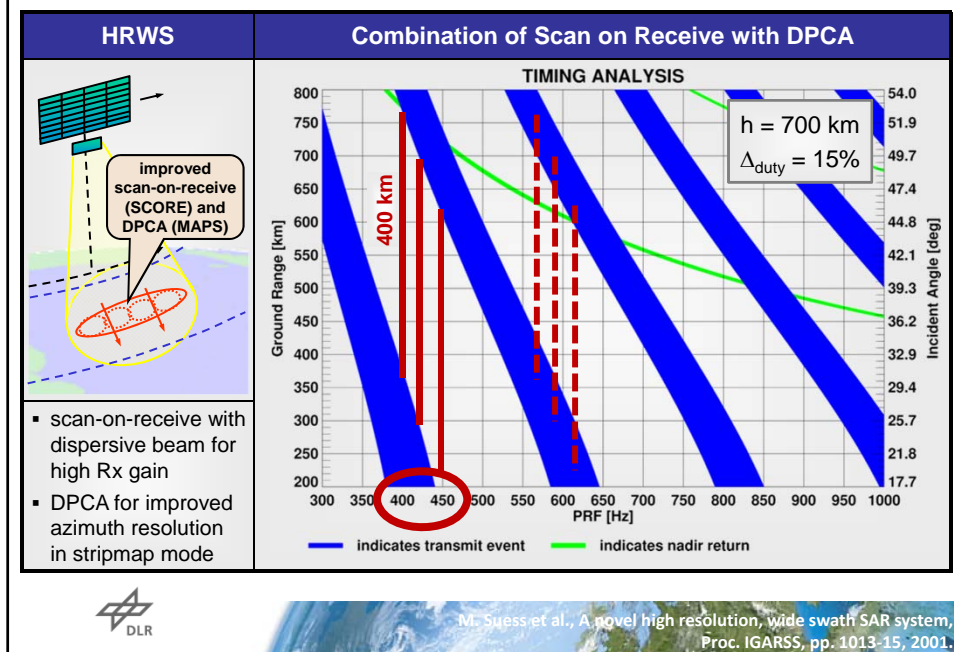


M. Suess et al., A novel high resolution, wide swath SAR system, Proc. IGARSS, pp. 1013-15, 2001.

DBF-SAR Systems with Planar Arrays

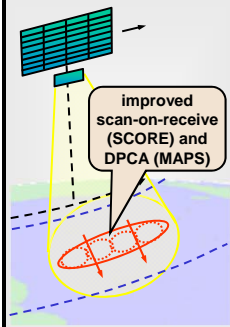


DBF-SAR Systems with Planar Arrays



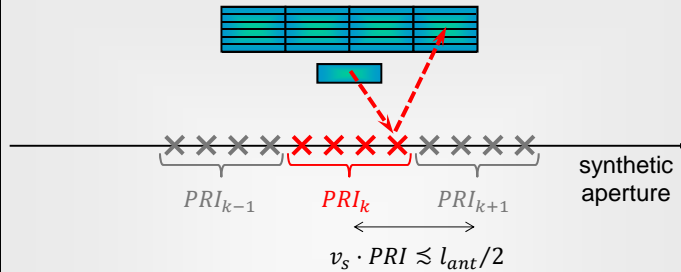
DBF-SAR Systems with Planar Arrays

HRWS



- scan-on-receive with dispersive beam for high Rx gain
- DPCA for improved azimuth resolution in stripmap mode

Combination of Scan on Receive with DPCA



Swath	PRF	l_{ant}
100 km	≈ 1.6 kHz	≥ 10 m
200 km	≈ 800 Hz	≥ 20 m
400 km	≈ 400 Hz	≥ 40 m

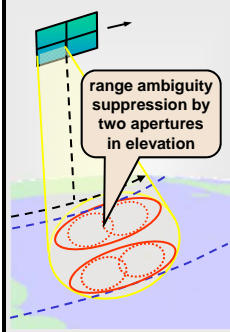
$$l_{ant} \geq \frac{2 \cdot v_s}{PRF}$$



M. Suess et al., A novel high resolution, wide swath SAR system, Proc. IGARSS, pp. 1013-15, 2001.

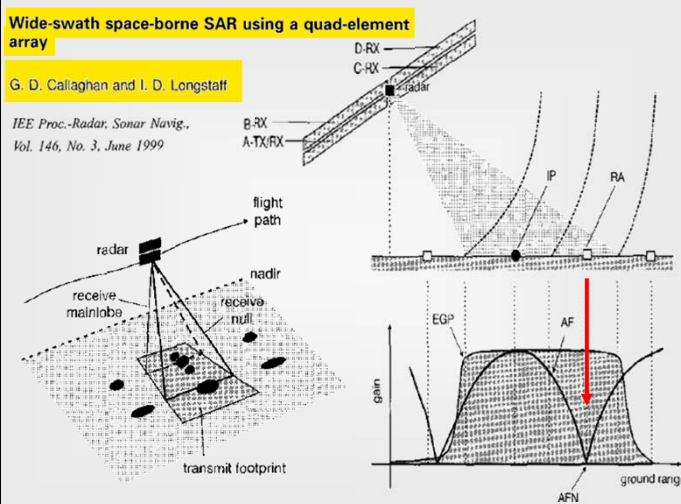
DBF-SAR Systems with Planar Arrays

Quad Array SAR



- good azimuth resolution
- compact antenna
- range gap in the middle of the swath

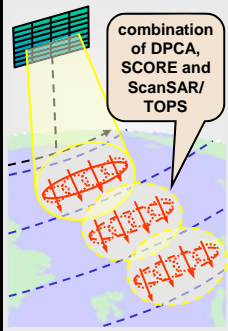
Suppression of Range Ambiguities by Null Steering



G.D. Callaghan et al., Wide-swath space-borne SAR using a quad-element array, IEE Proceedings for Radar, Sonar and Navigation, Vol. 146, pp. 159-165, 1999.

DBF-SAR Systems with Planar Arrays

Burst-DBF-SAR



- enables mapping of ultra-wide swaths with high resolution
- suggested as Sentinel-1 successor system

DPCA in Burst Mode Operation

- Minimum PRF is determined by antenna length:

$$PRF \gtrsim \frac{2 \cdot v_s}{l_{ant}}$$



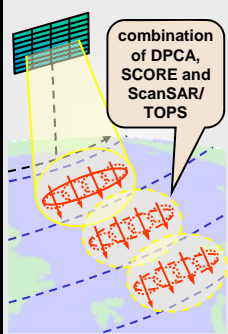
l_{ant}	PRF
10 m	$\gtrsim 1500$ Hz
12.5 m	$\gtrsim 1200$ Hz
15 m	$\gtrsim 1000$ Hz

- Minimum burst number is determined from timing



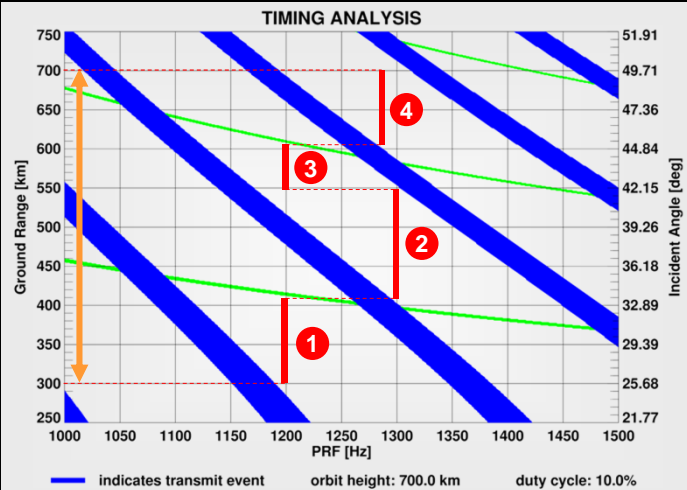
ScanSAR with Planar Array

Burst-DBF-SAR

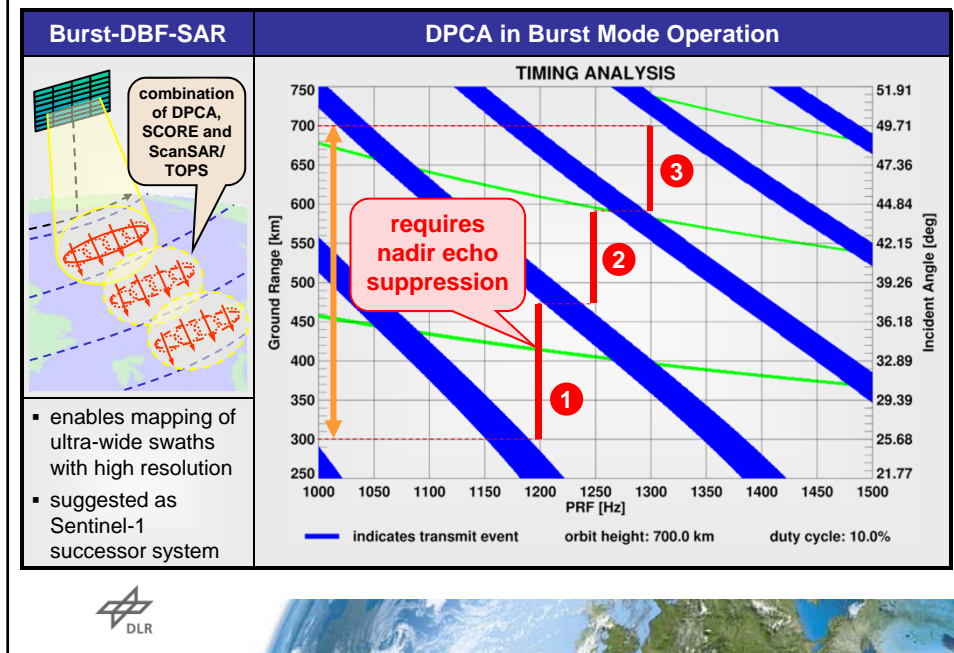


- enables mapping of ultra-wide swaths with high resolution
- suggested as Sentinel-1 successor system

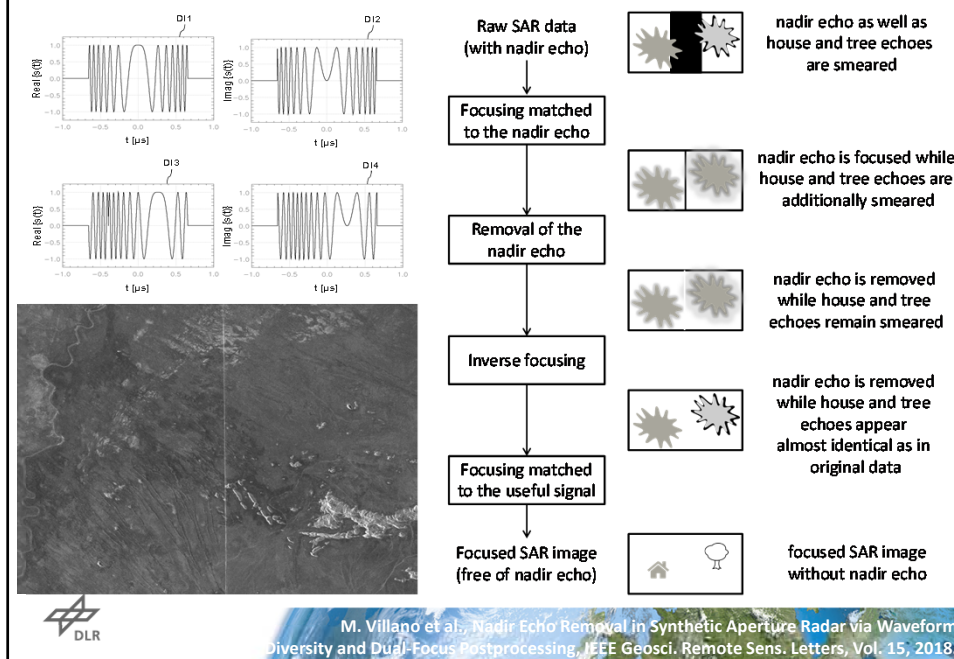
DPCA in Burst Mode Operation



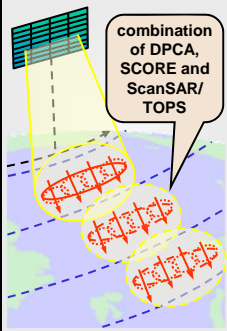
ScanSAR with Planar Array





New Nadir Suppression Technique

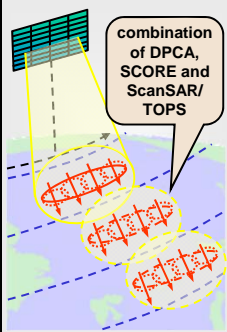
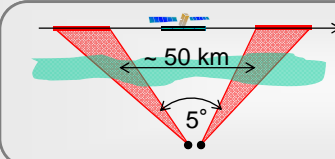




DBF-SAR Systems with Planar Arrays

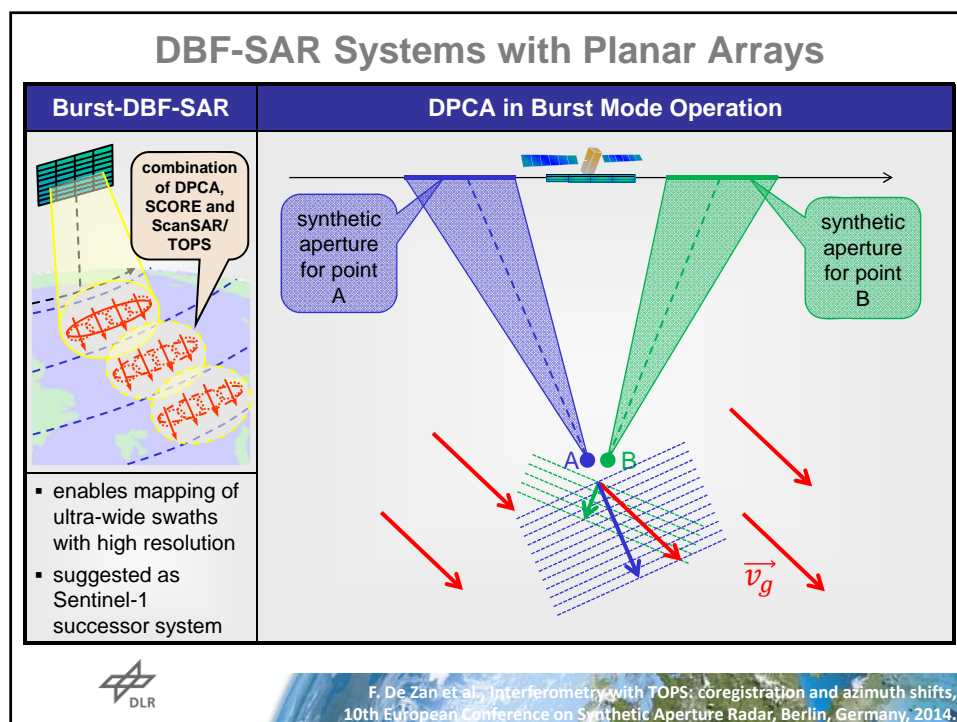
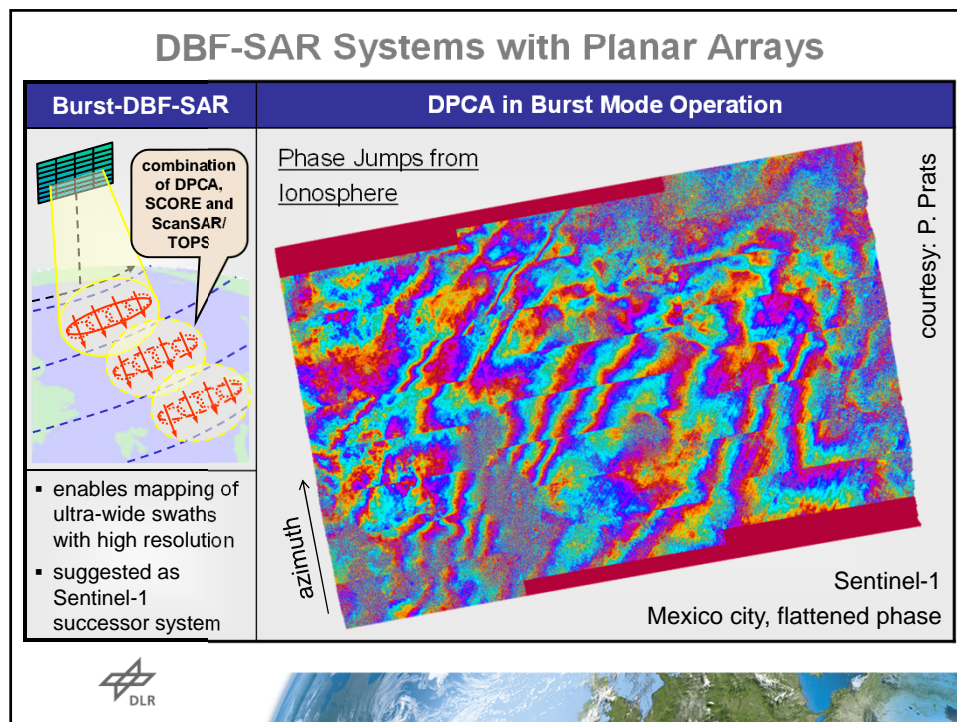
Burst-DBF-SAR	DPCA in Burst Mode Operation								
 <ul style="list-style-type: none"> enables mapping of ultra-wide swaths with high resolution suggested as Sentinel-1 successor system 	<ul style="list-style-type: none"> Minimum PRF is determined by antenna length: <table border="1"> <thead> <tr> <th>l_{ant}</th> <th>PRF</th> </tr> </thead> <tbody> <tr> <td>10 m</td> <td>$\gtrsim 1500$ Hz</td> </tr> <tr> <td>12.5 m</td> <td>$\gtrsim 1200$ Hz</td> </tr> <tr> <td>15 m</td> <td>$\gtrsim 1000$ Hz</td> </tr> </tbody> </table> Minimum burst number is determined from timing: $PRF \gtrsim 1200 \text{ Hz} \rightarrow \begin{cases} N_{burst} = 4 \text{ (with nadir)} \\ N_{burst} = 3 \text{ (w/o nadir)} \end{cases}$ Minimum number of azimuth channels from az. resolution: $N_{az} \gtrsim \frac{l_{ant}}{2\delta_{az}} \cdot (N_{burst} + 1) \xrightarrow[l_{ant} = 12.5 \text{ m}]{N_{burst} = 4} N_{az} \gtrsim 7$ 	l_{ant}	PRF	10 m	$\gtrsim 1500$ Hz	12.5 m	$\gtrsim 1200$ Hz	15 m	$\gtrsim 1000$ Hz
l_{ant}	PRF								
10 m	$\gtrsim 1500$ Hz								
12.5 m	$\gtrsim 1200$ Hz								
15 m	$\gtrsim 1000$ Hz								

DBF-SAR Systems with Planar Arrays

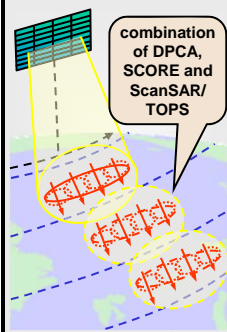
Burst-DBF-SAR	DPCA in Burst Mode Operation															
 <ul style="list-style-type: none"> enables mapping of ultra-wide swaths with high resolution suggested as Sentinel-1 successor system 	<ul style="list-style-type: none"> The high-resolution wide-swath ScanSAR mode may imply a notable squint angle change at the burst borders: <table border="1"> <thead> <tr> <th rowspan="2">Mode</th> <th rowspan="2">Bursts</th> <th rowspan="2">N_{az}</th> <th colspan="3">Δ Squint Angle ($\Delta\psi$)</th> </tr> <tr> <th>L-band</th> <th>C-band</th> <th>X-band</th> </tr> </thead> <tbody> <tr> <td>5 m @ 400 km</td> <td>4</td> <td>7</td> <td>5.1°</td> <td>1.2°</td> <td>0.66°</td> </tr> </tbody> </table> <div style="display: flex; align-items: center; justify-content: center;">  <div style="margin-left: 20px;"> $\Delta\psi \approx \frac{N_{burst}}{2\delta_{az}} \cdot \lambda$ </div> </div> <p><u>Challenges:</u></p> <ul style="list-style-type: none"> azimuth scalloping (AASR, NESZ) line-of-sight variation (interferometry) atmospheric discontinuities (ionosphere) 	Mode	Bursts	N_{az}	Δ Squint Angle ($\Delta\psi$)			L-band	C-band	X-band	5 m @ 400 km	4	7	5.1°	1.2°	0.66°
Mode	Bursts				N_{az}	Δ Squint Angle ($\Delta\psi$)										
		L-band	C-band	X-band												
5 m @ 400 km	4	7	5.1°	1.2°	0.66°											



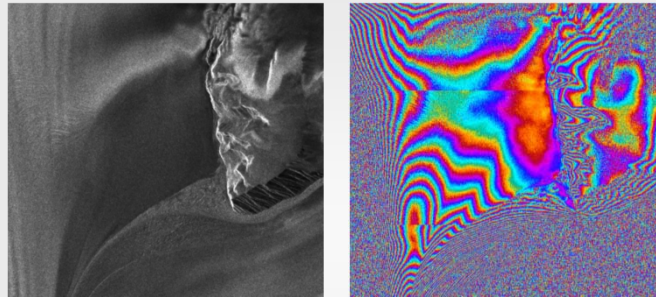
DBF-SAR Systems with Planar Arrays

Burst-DBF-SAR



- enables mapping of ultra-wide swaths with high resolution
- suggested as Sentinel-1 successor system

DPCA in Burst Mode Operation



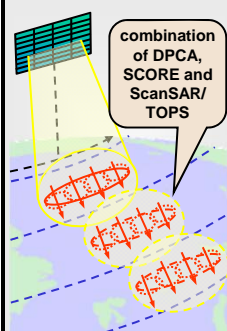
11-day TSX TOPS interferogram over the Lambert glacier, Antarctica. (Left) Reflectivity image and (right) flattened interferogram. The images show three consecutive bursts (9 km per burst in azimuth), where the top-right part is a stable rocky area showing no phase jumps at burst edges. The glacier, on the other hand, shows clear jumps at burst edges. The jumps are legitimate and correspond to the projection of the motion in the LOS direction, being the latter azimuth-dependent. At burst edges the LOS vectors have opposite azimuth directions, and therefore the jumps can be clearly seen. Range is horizontal and azimuth is vertical (from F. De Zan et al, EUSAR 2014).



F. De Zan et al., Interferometry with TOPS: coregistration and azimuth shifts, 10th European Conference on Synthetic Aperture Radar, Berlin, Germany, 2014.

DBF-SAR Systems with Planar Arrays

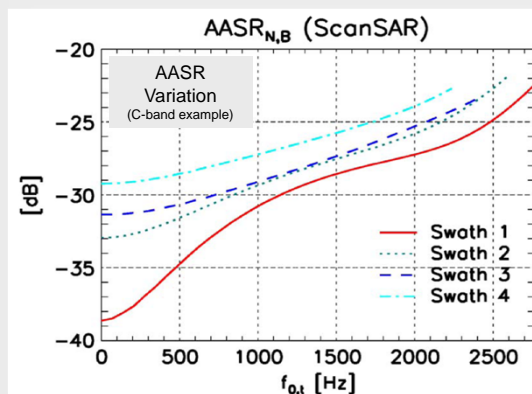
Burst-DBF-SAR



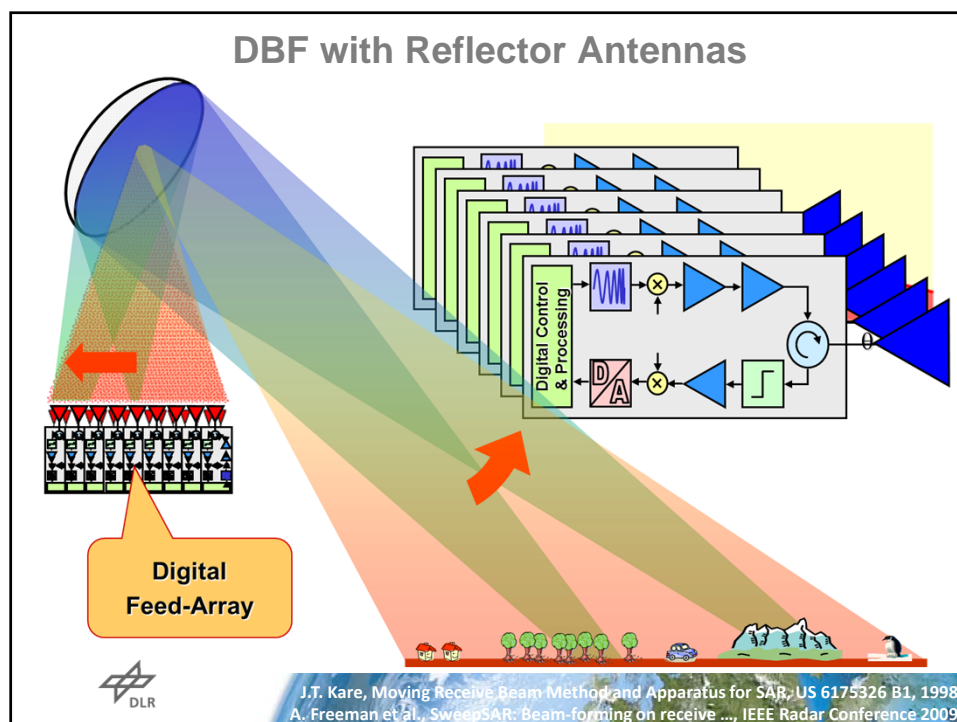
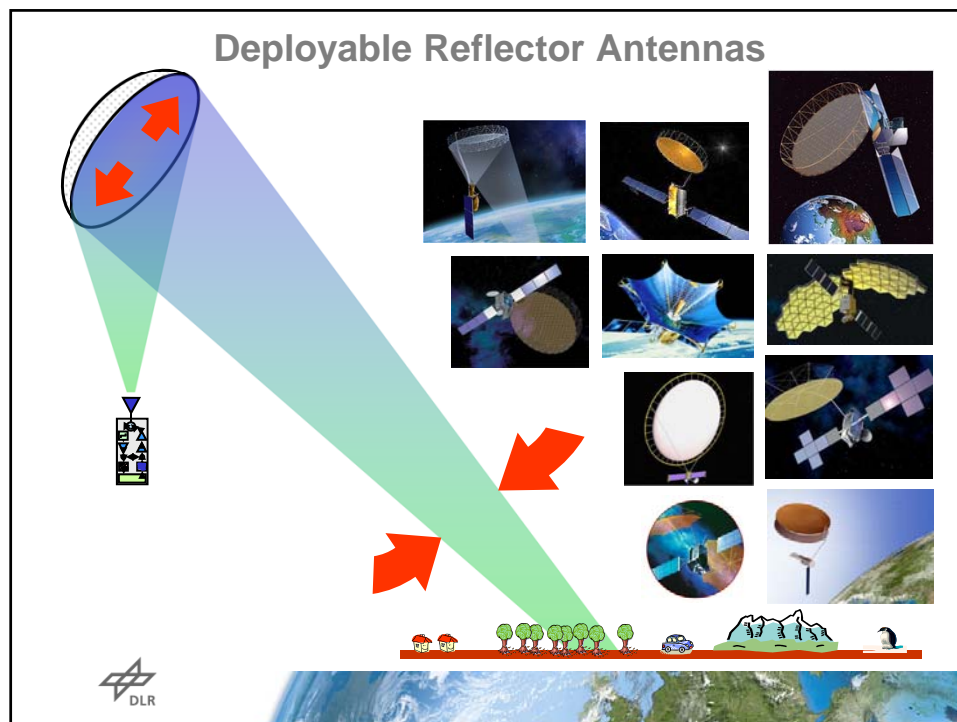
- enables mapping of ultra-wide swaths with high resolution
- suggested as Sentinel-1 successor system

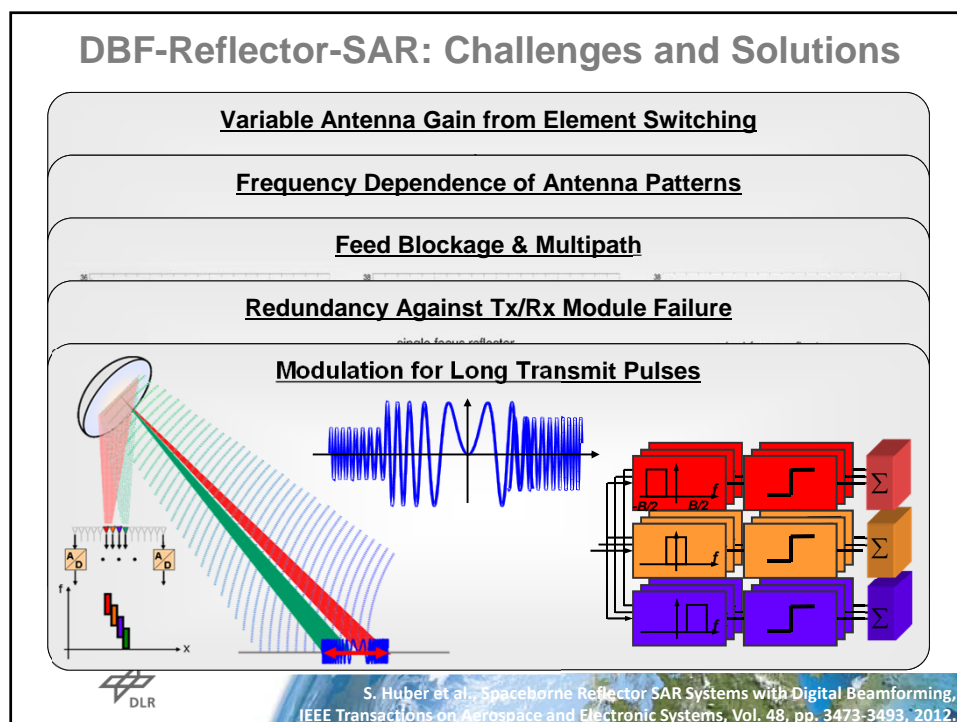
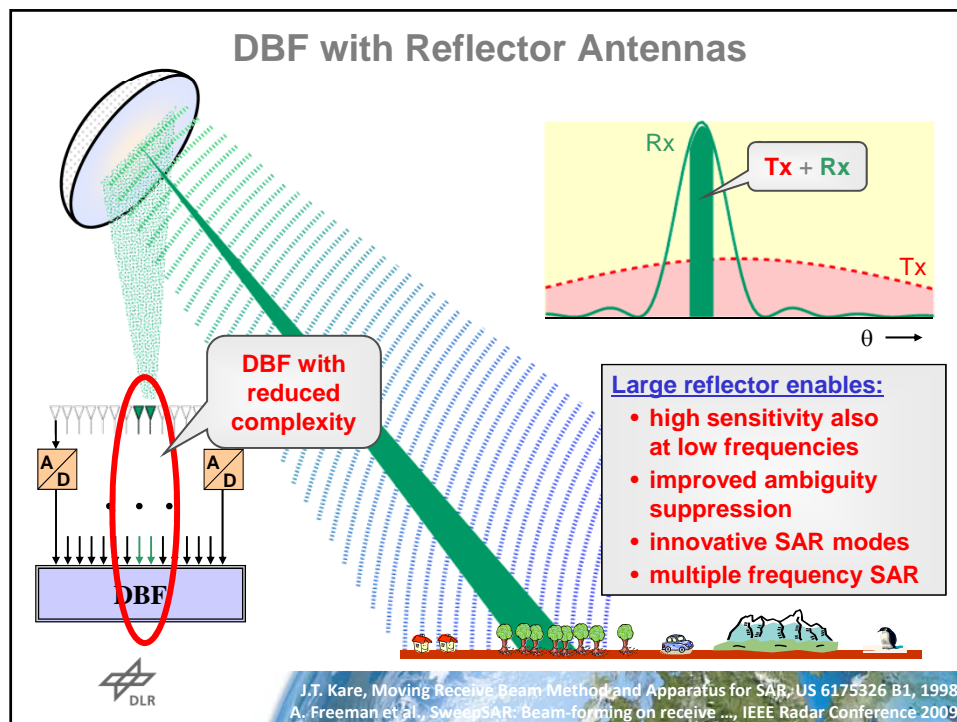
DPCA in Burst Mode Operation

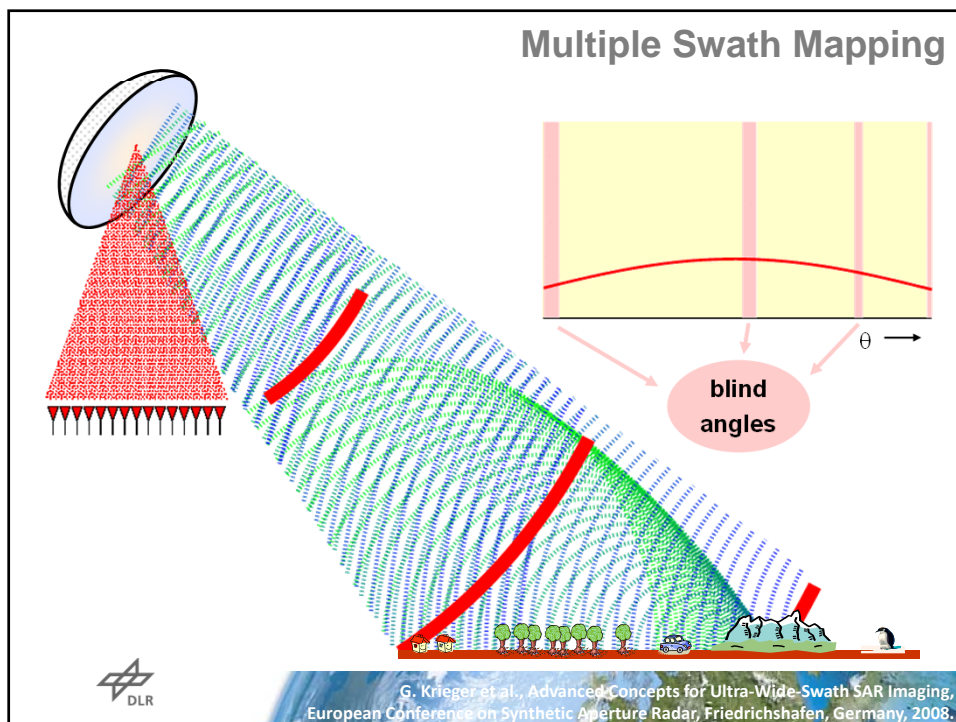
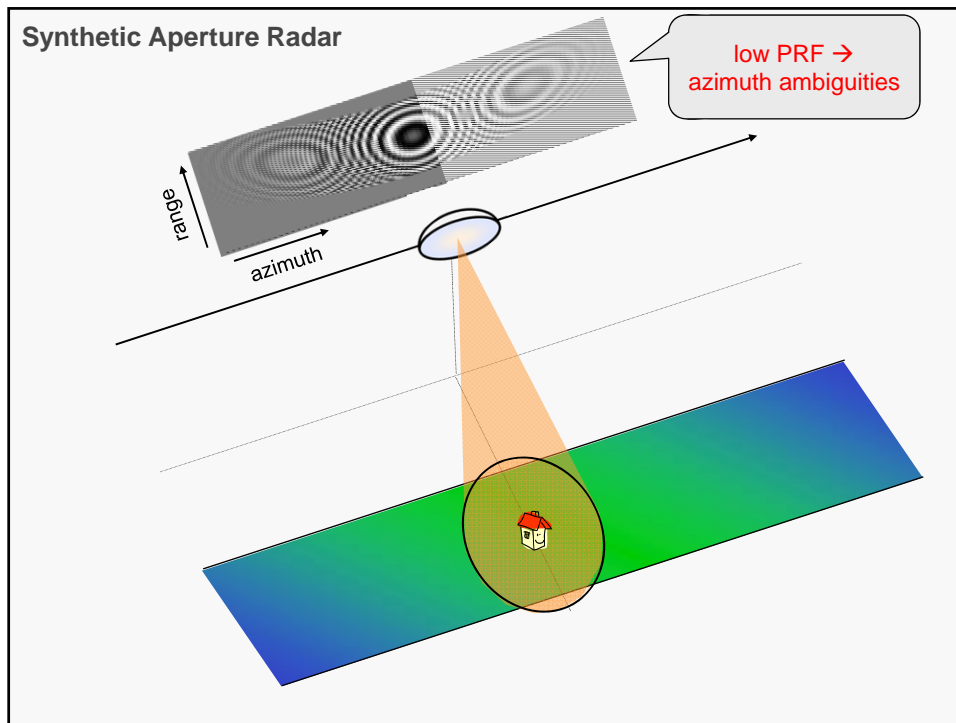
Scalloping in Multichannel ScanSAR mode

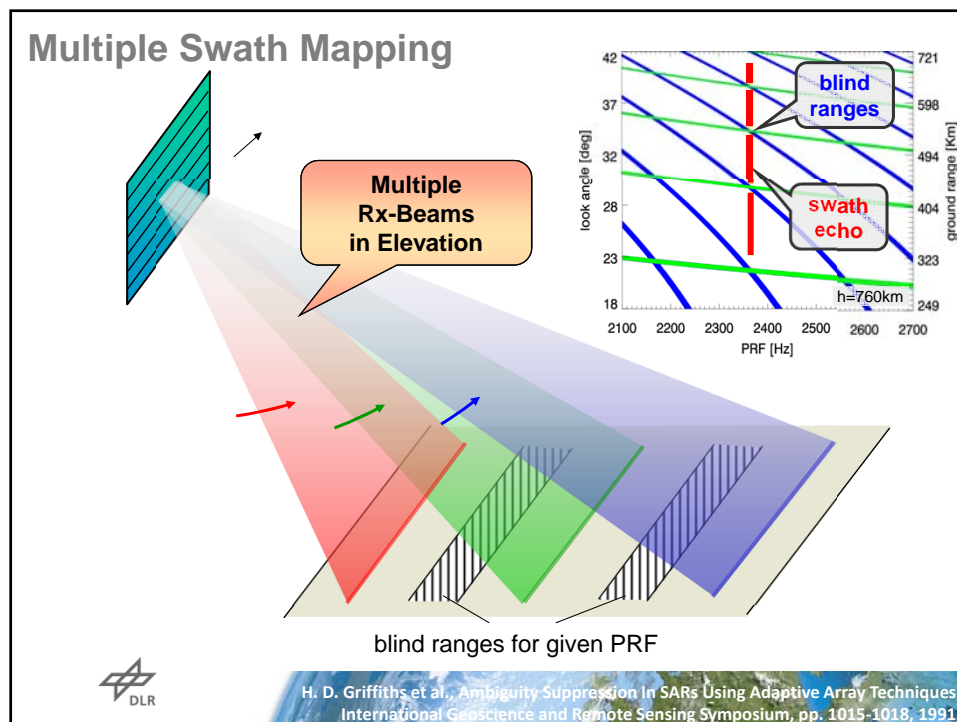
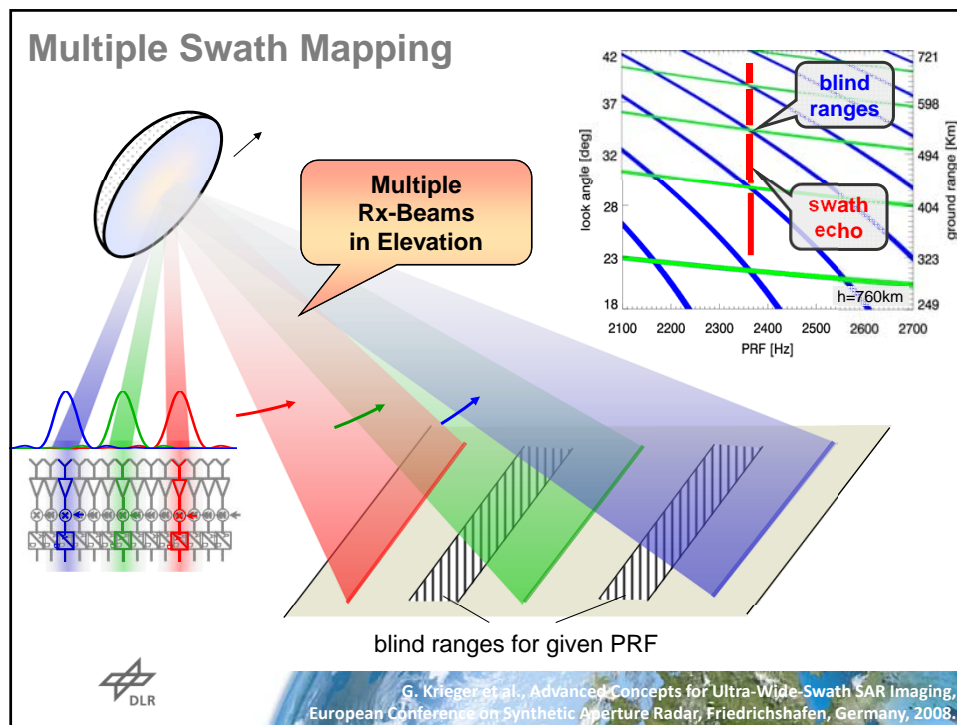


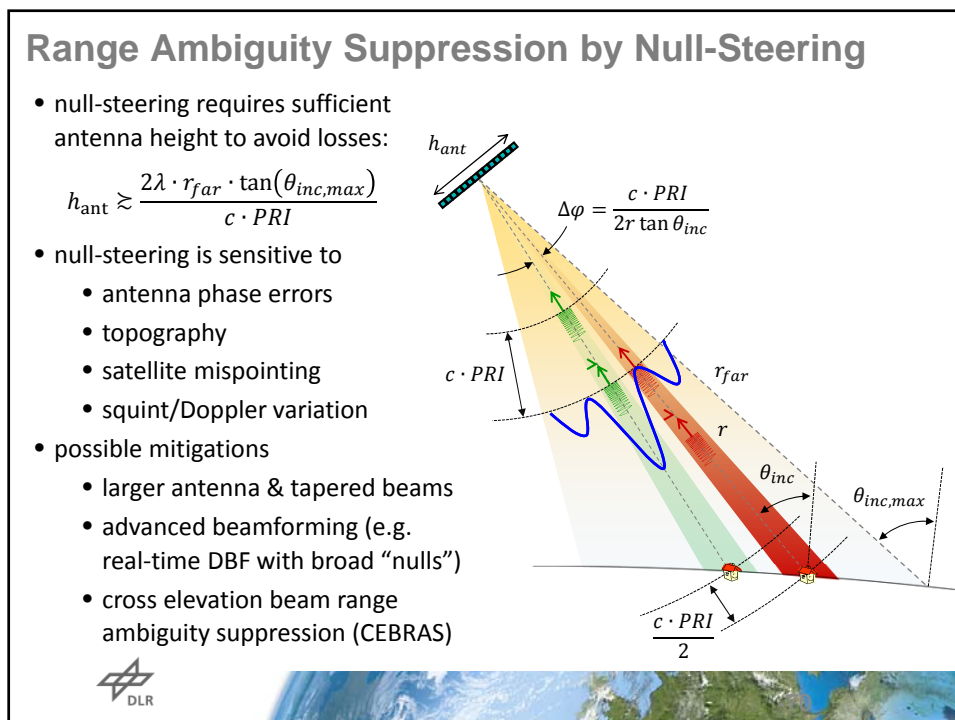
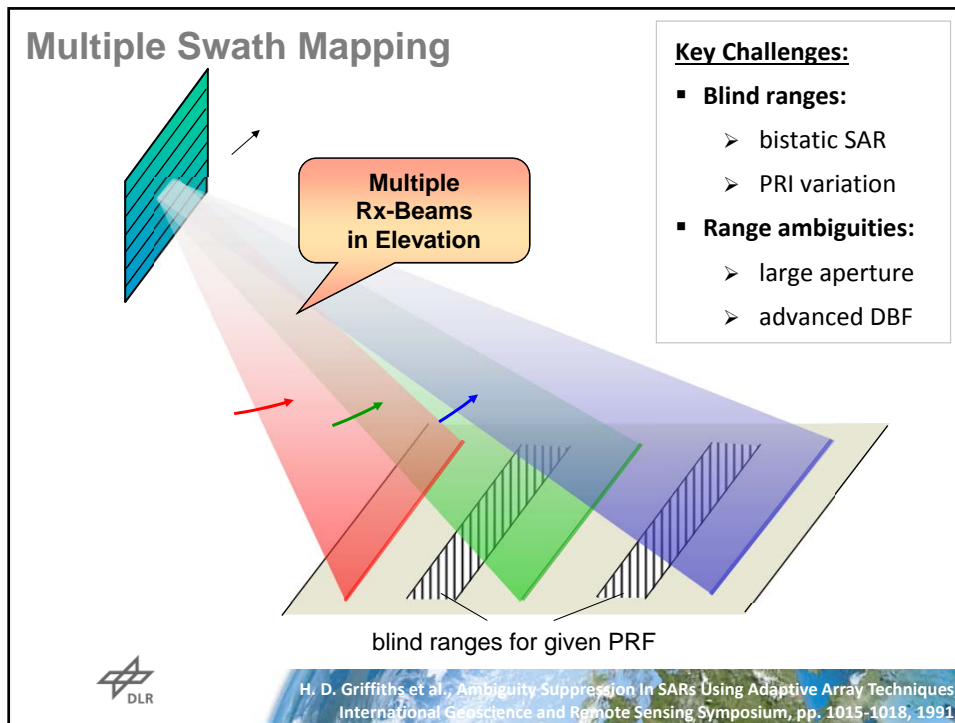
N. Gebert et al., Multichannel Azimuth Processing in ScanSAR and TOPS Mode Operation, IEEE Trans. Geosci. Remote Sens., Vol. 48, pp. 2994-3008, 2010.

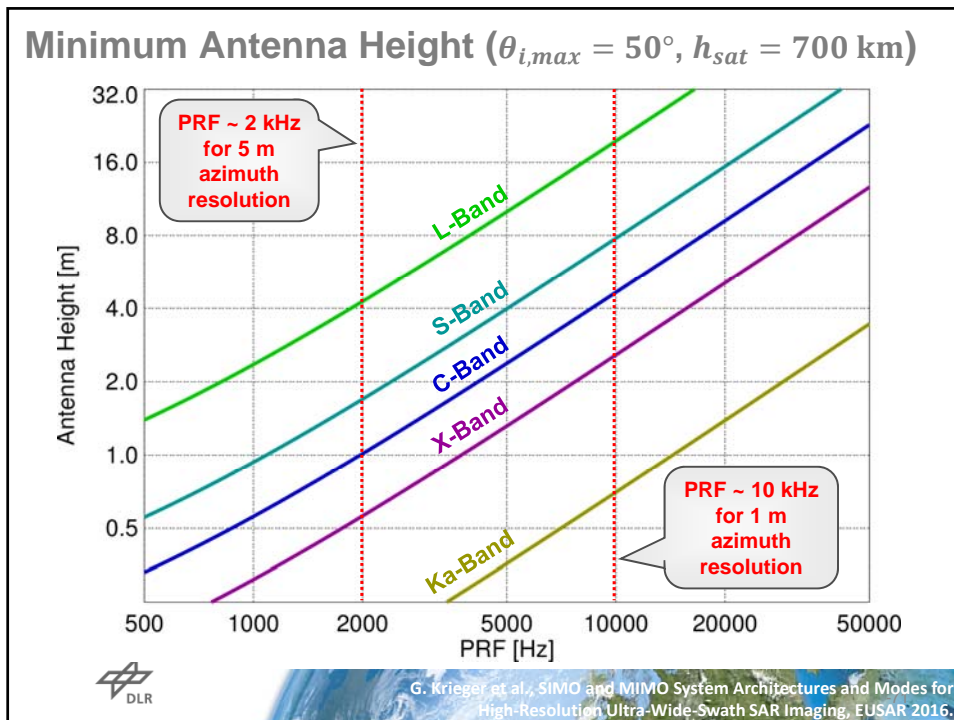












Tx-Rx Separation (Bistatic System)

- Simultaneous transmission and reception avoids blind ranges
- Direct signal can be suppressed by
 - Doppler filter
 - additional mitigation by waveform diversity and/or PRI variation
- Advantages
 - ultra-wide swaths with high resolution
 - compact antennas and satellites
 - no Tx/Rx switches, less losses, FMCW, ...
- Drawbacks
 - requires two satellites (3 for single-pass InSAR)
 - requires accurate time and phase synchronisation

The diagram illustrates a bistatic SAR system with two satellites in orbit. One satellite is the transmitter (Tx) and the other is the receiver (Rx). They illuminate a target area on the ground from different angles, creating overlapping swaths. The ground is shown with a grid, and the swaths are represented by colored cones originating from the satellites. A yellow cone represents the Tx swath, and a blue cone represents the Rx swath. A green cone represents the combined bistatic swath. A red cone represents the direct signal from the Tx to the Rx, which is suppressed.

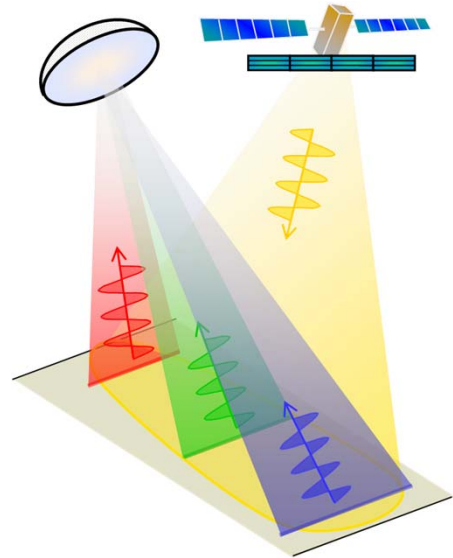
DLR

G. Krieger et al., Potential of digital beamforming in bi- and multistatic SAR, IEEE International Geoscience and Remote Sensing Symposium, pp. 527-529, 2003.

Tx-Rx Separation (Bistatic System)

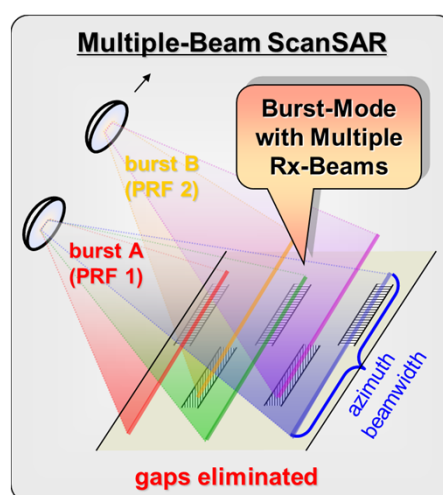
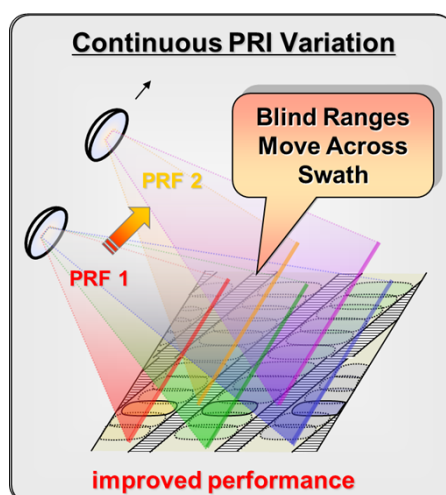
- Simultaneous transmission and reception avoids blind ranges
- Example:

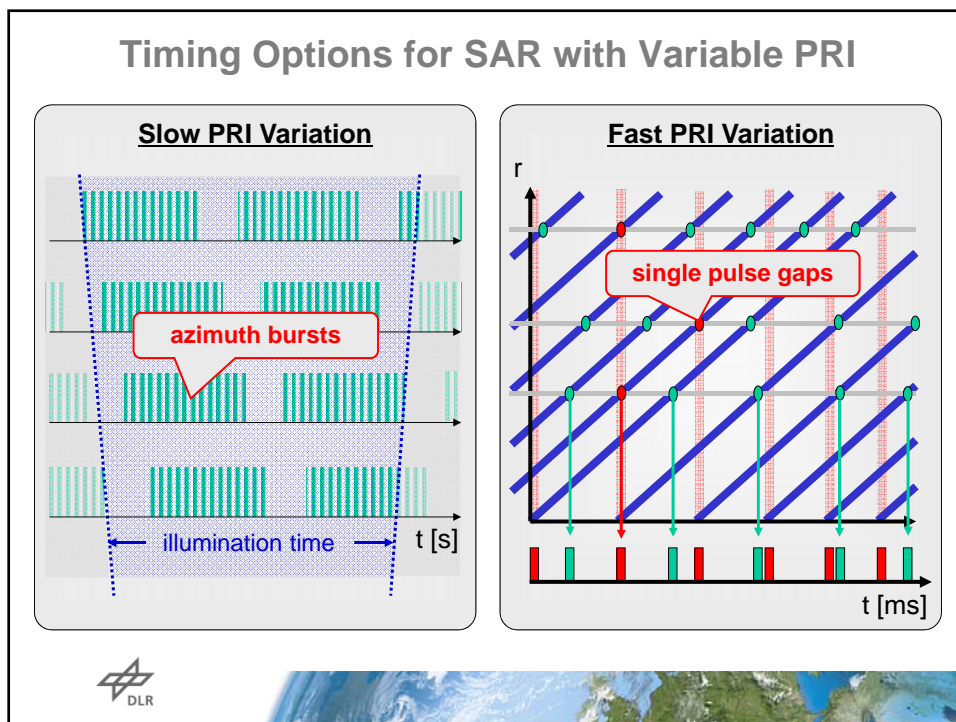
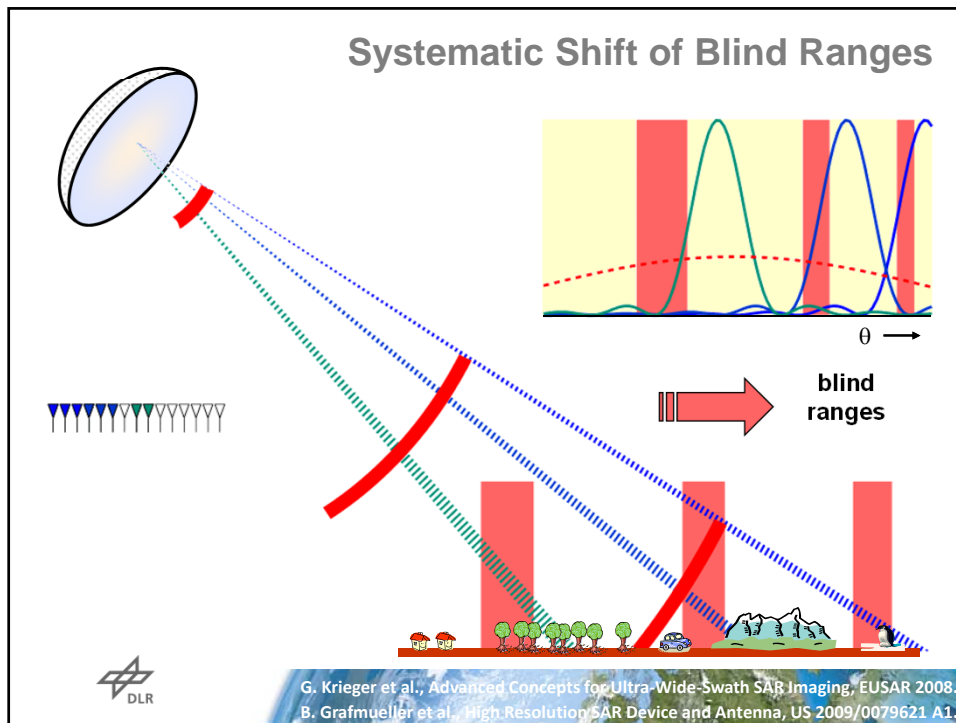
Parameter	Value
Swath	500 km
Azimuth Resolution	3 m
Orbit Height	800 km
PRF	3.5 kHz
Tx Antenna Length	5 m
Tx Antenna Height	> 0.8 m (L-band) > 0.1 m (X-band)
Rx Antenna Length	5 m
Rx Antenna Height	> 5.6 m (L-band) > 0.7 m (X-band)



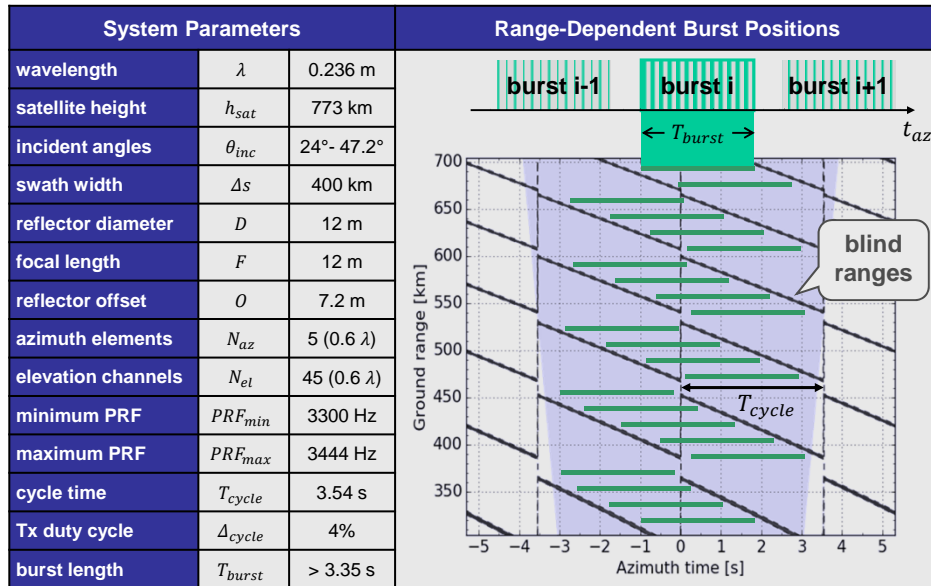
Multi-Beam Concepts for Ultra-Wide-Swath Imaging

- Strategies for Elimination of Blind Ranges -

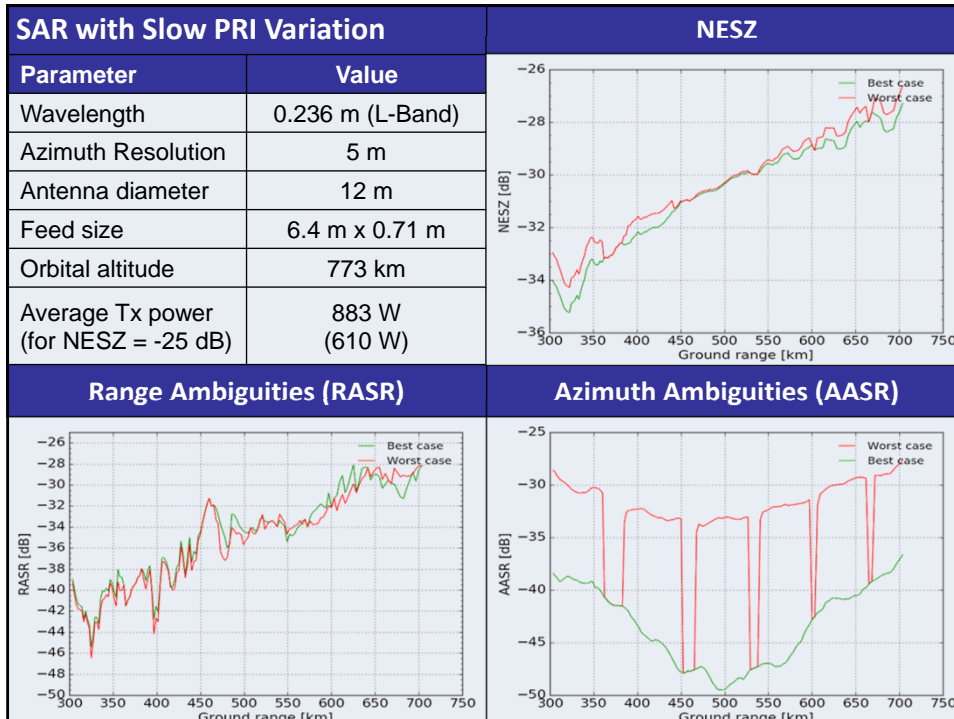




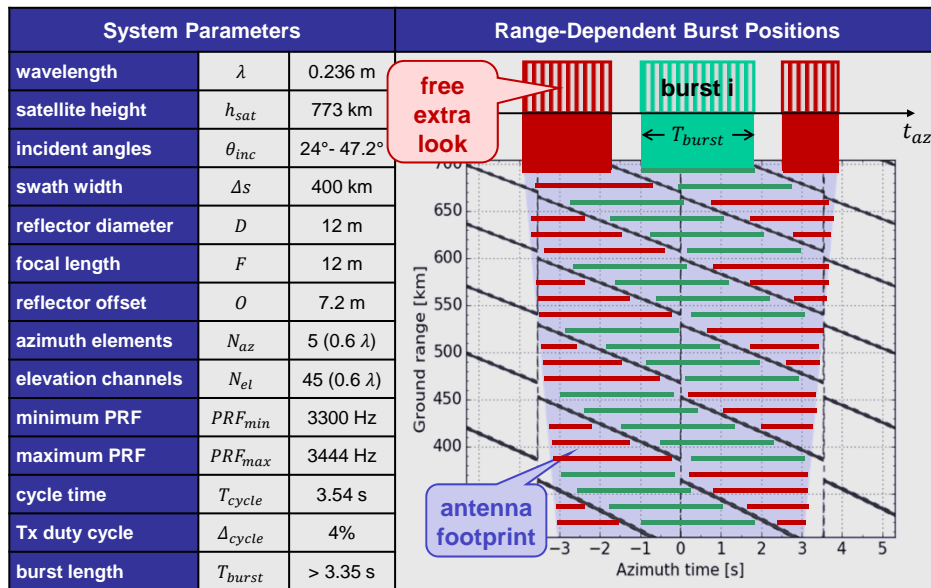
Multiple Elevation Beam SAR with Slow PRI Variation



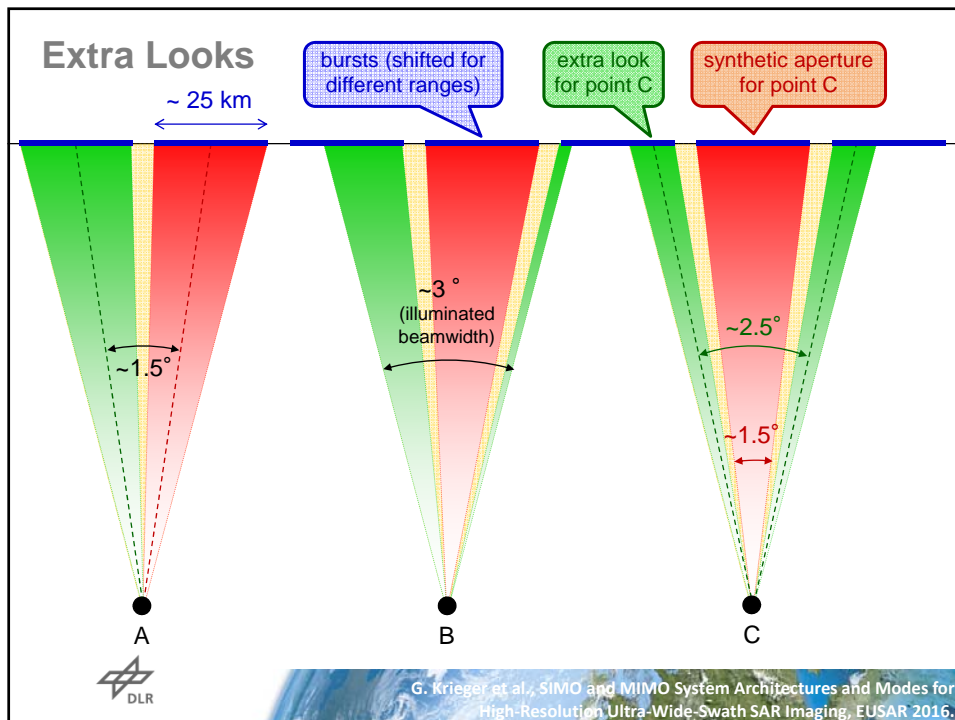
G. Krieger et al., SIMO and MIMO System Architectures and Modes for High-Resolution Ultra-Wide-Swath SAR Imaging, EUSAR 2016.



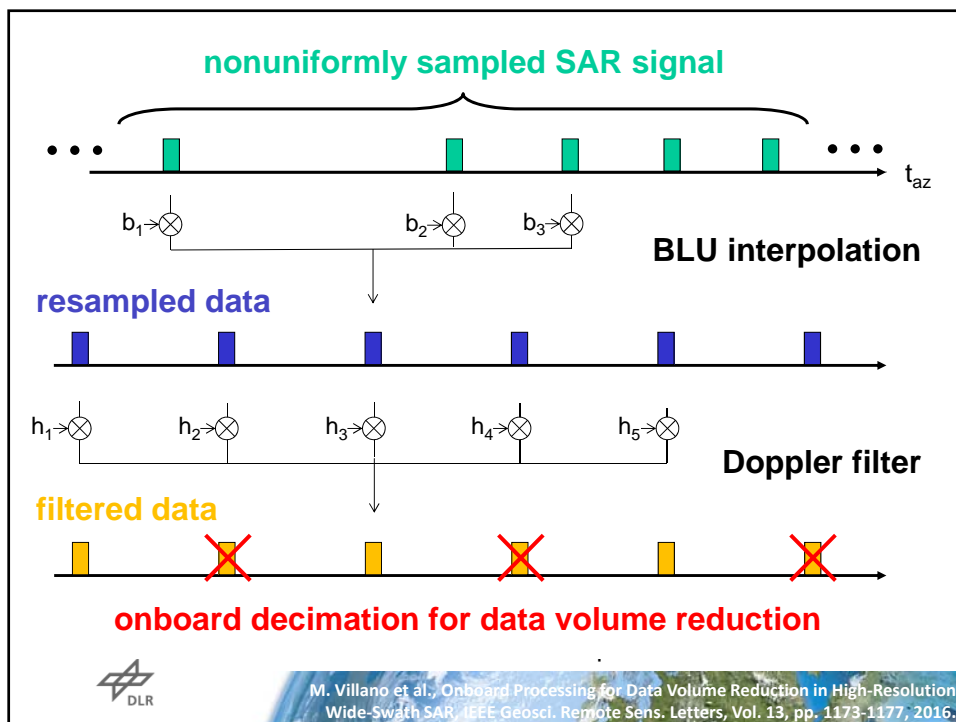
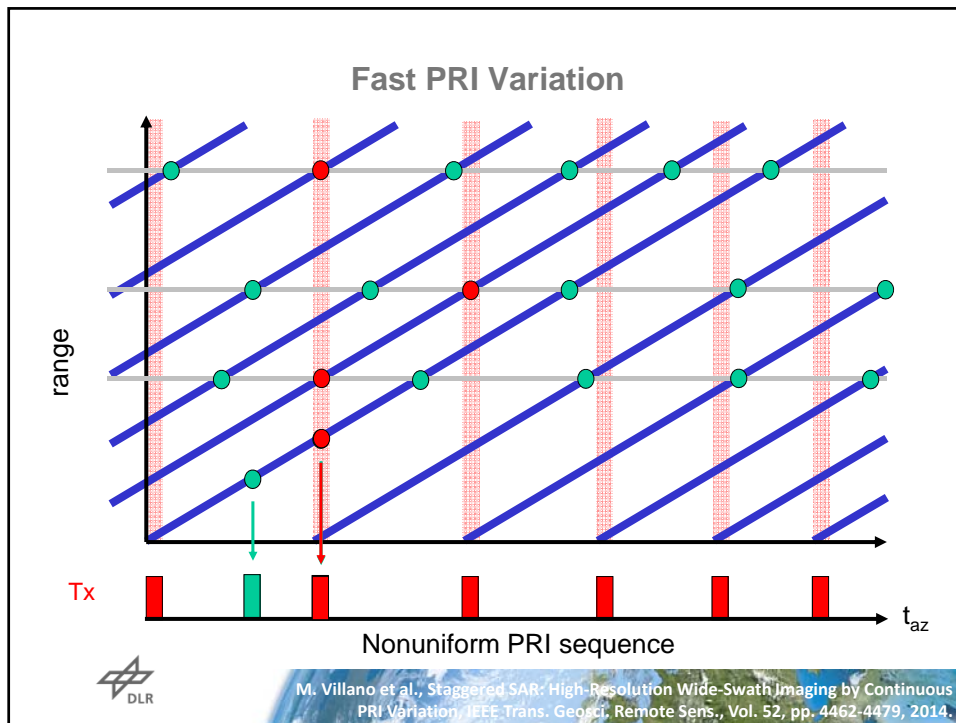
Multiple Elevation Beam SAR with Slow PRI Variation

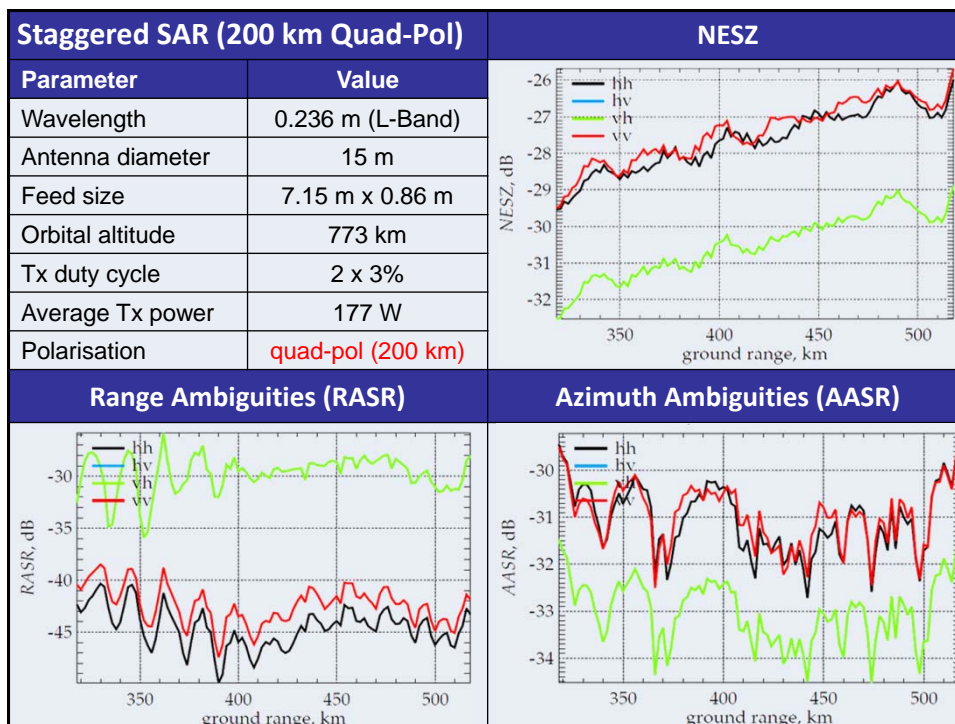
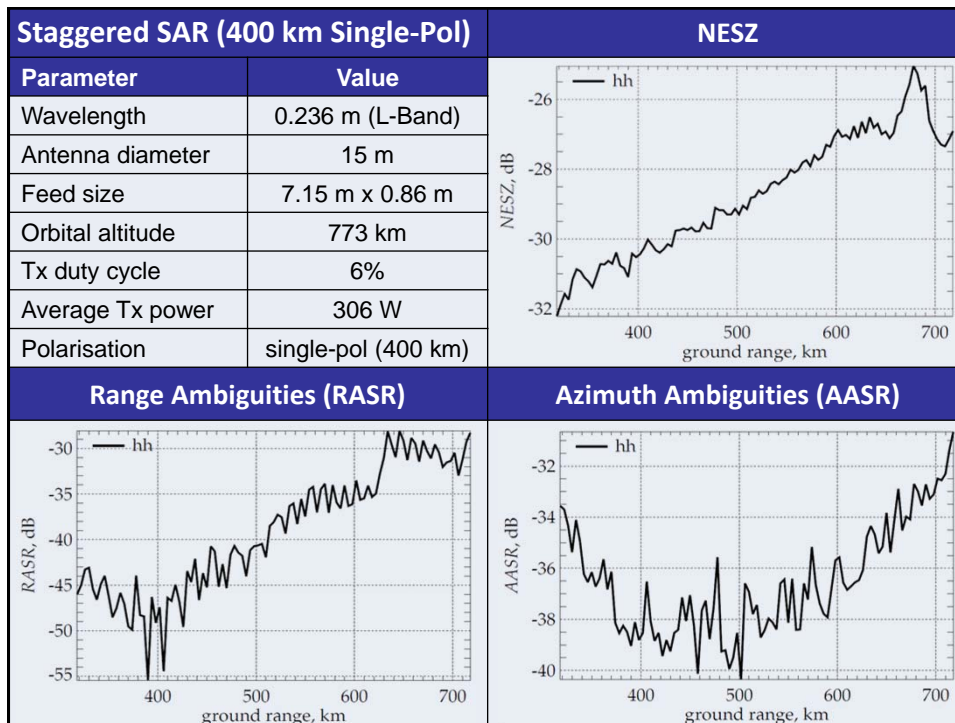


G. Krieger et al., SIMO and MIMO System Architectures and Modes for High-Resolution Ultra-Wide-Swath SAR Imaging, EUSAR 2016.

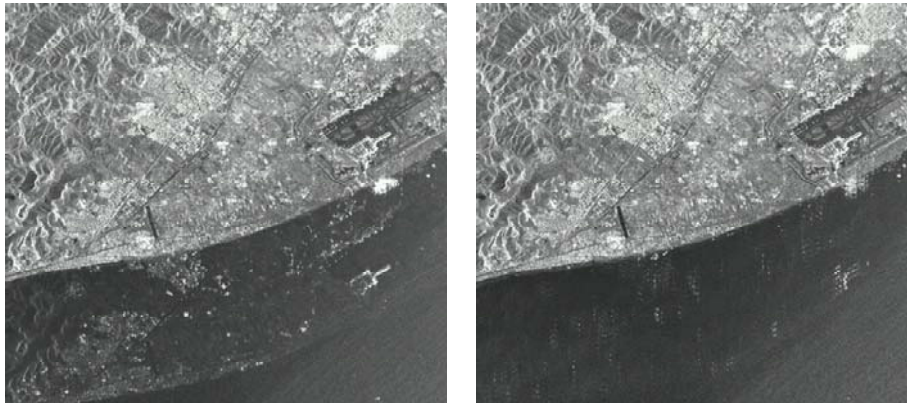


G. Krieger et al., SIMO and MIMO System Architectures and Modes for High-Resolution Ultra-Wide-Swath SAR Imaging, EUSAR 2016.





Smearing of Azimuth Ambiguities in Staggered SAR



Simulation to demonstrate the additional benefits from azimuth ambiguity smearing for a staggered-SAR system, based on a TerraSAR-X image, acquired over Barcelona, Spain. (a) Original image with accentuated azimuth ambiguities. (b) Simulated staggered-SAR image using the more elaborated sequence and best linear interpolation (BLU). (From Villano et al., *Staggered SAR: High-Resolution Wide-Swath Imaging by Continuous PRI Variation*, IEEE Transactions on Geoscience and Remote Sensing, July 2013).



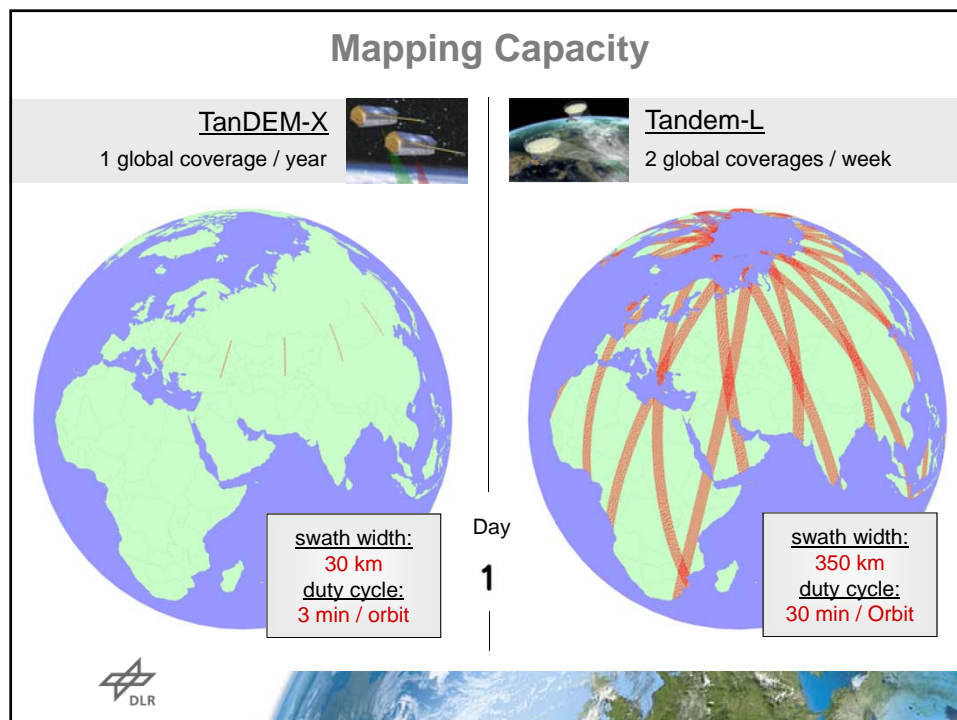
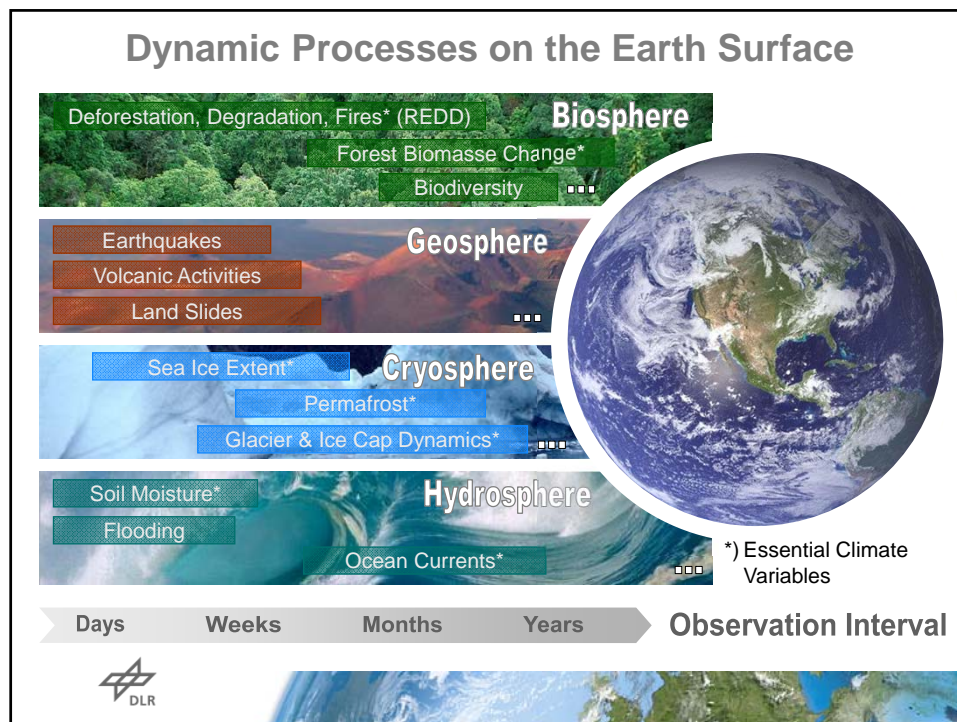
M. Villano et al., Staggered SAR: Performance Analysis and Experiments With Real Data, IEEE Trans. Geosci. Remote Sens., Vol. 55, pp. 6617-6638, 2017.

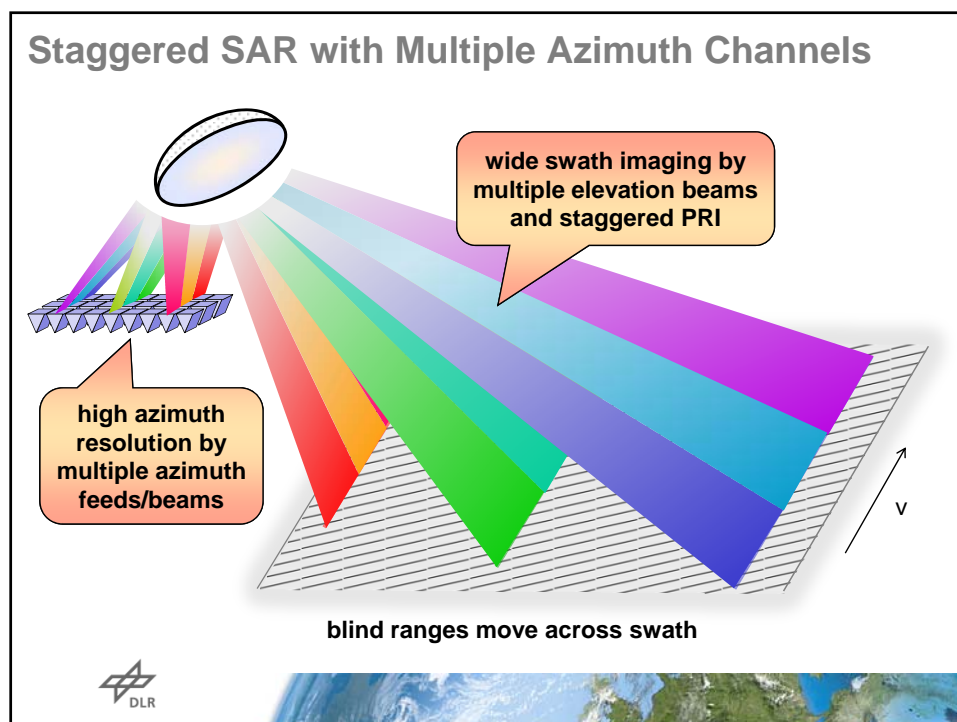
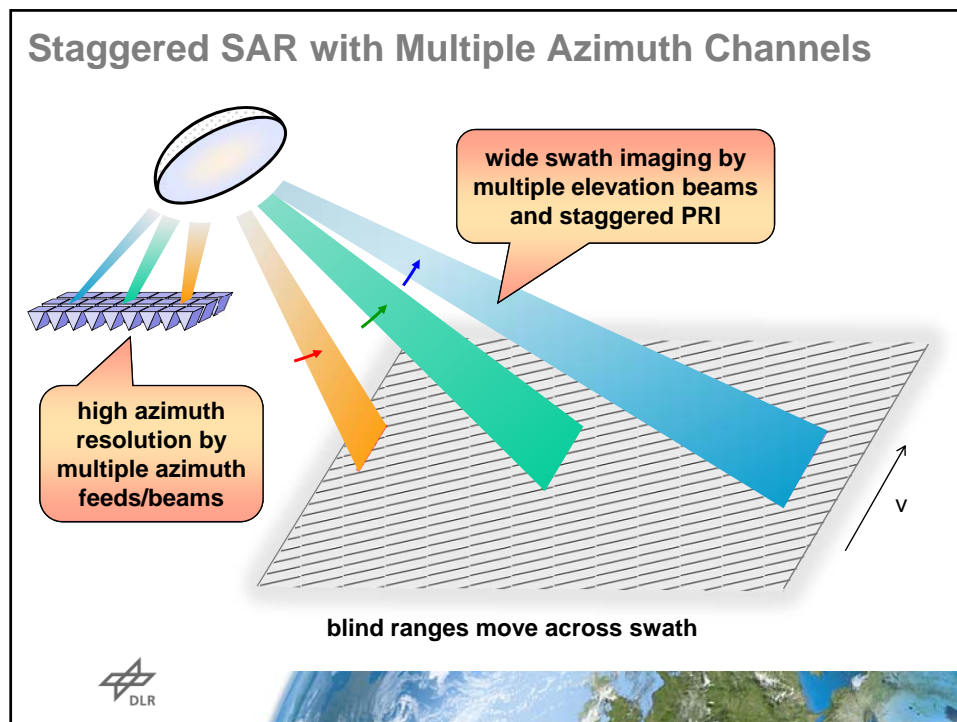
Tandem-L

Systematic Monitoring of
Earth System Dynamics



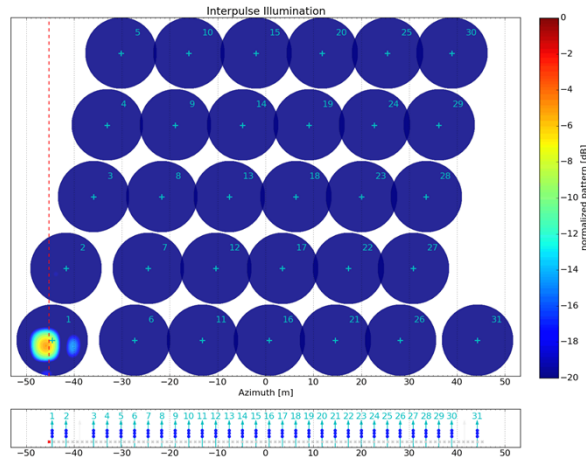
A. Moreira et al., Tandem-L: A Highly Innovative Bistatic SAR Mission for Global Observation of Dynamic Processes on the Earth's Surface, IEEE Geoscience and Remote Sensing Magazine, Vol. 3, pp. 8-23, 2015.





Staggered SAR with Multiple Azimuth Channels

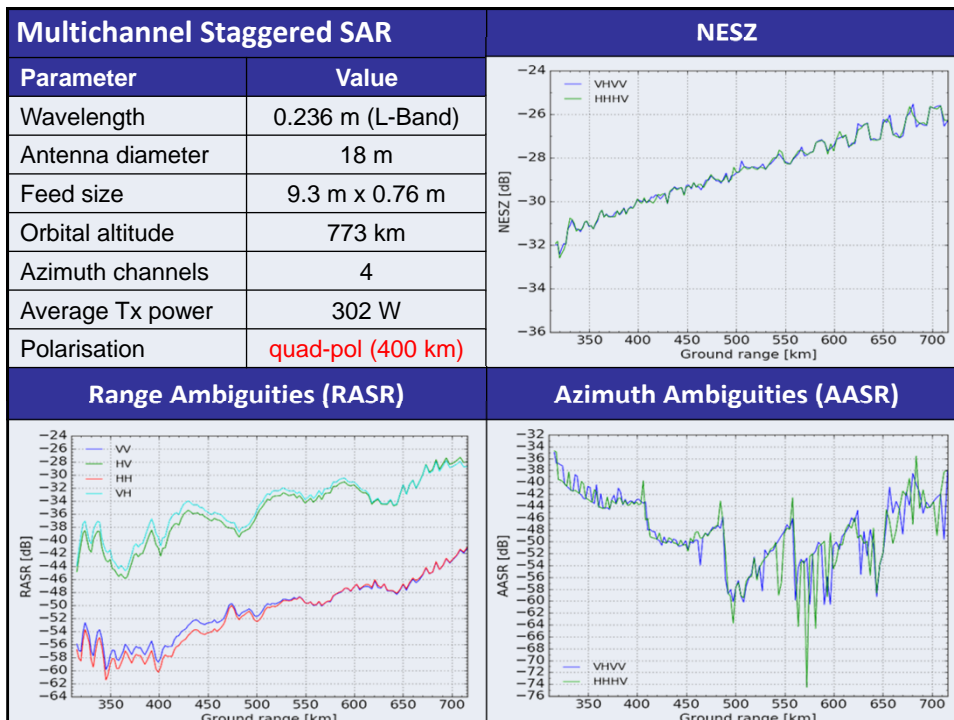
- Requires combination of
 - multi-channel reconstruction
 - staggered SAR interpolation
- Novel virtual beam synthesis technique
- Key idea: multichannel SAR signal resampling to uniform grid using
 - multiple Rx pulses (time-variant interpolation)
 - adaptive beams (time-variant aperture tapering)



F. Queiroz de Almeida et al, "Multichannel staggered SAR azimuth sample regularization", Proc. EUSAR, June 2016 (TGRS paper in print)



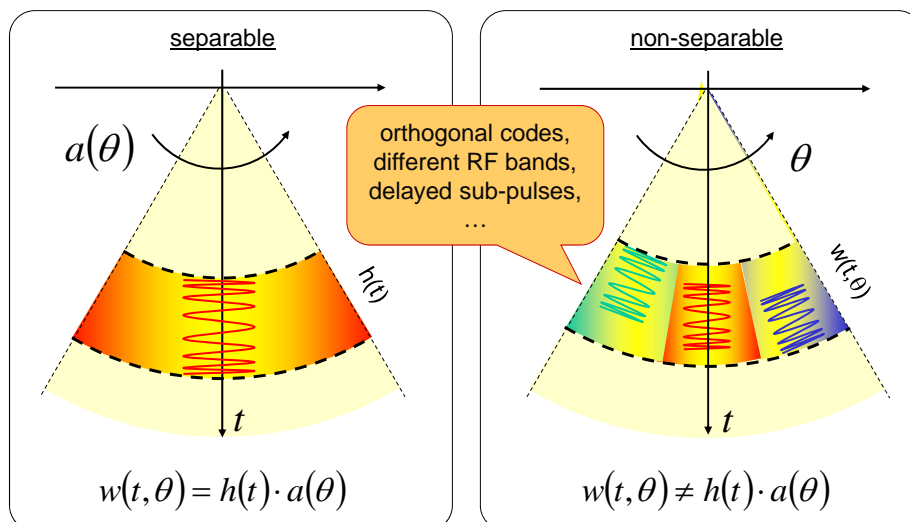
F. Queiroz de Almeida et al., Multichannel Staggered SAR Azimuth Processing, IEEE Trans. Geosci. Remote Sens., Vol. 56, pp. 2772-2788, 2018.



MIMO SAR

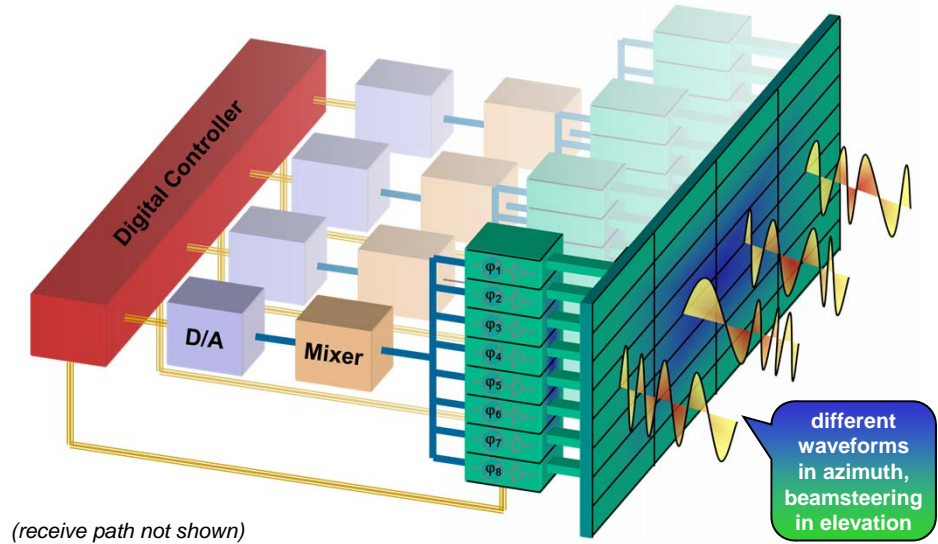


Spatiotemporally Non-Separable Waveform Encoding



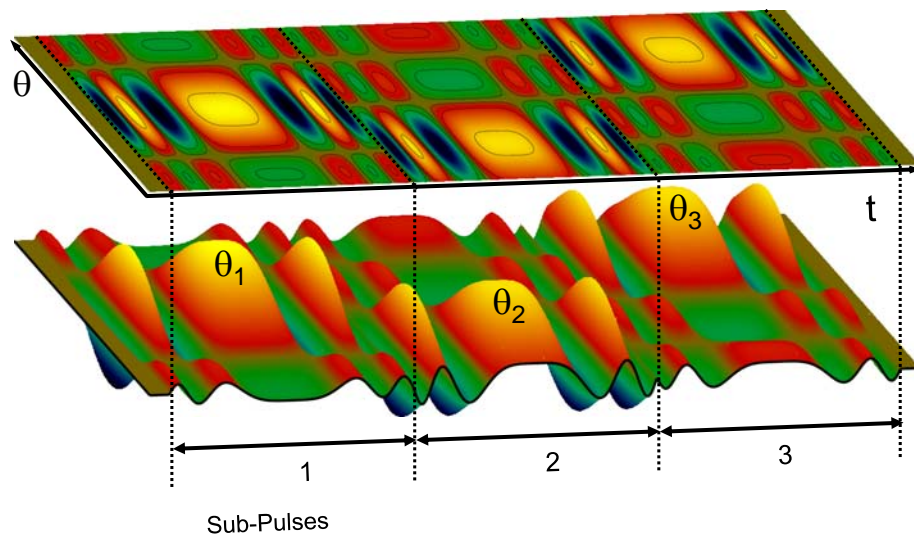
G. Krieger et al., Multidimensional Waveform Encoding: A New DBF Technique for SAR Remote Sensing, IEEE Trans. Geosci. Remote Sens., Vol. 46, pp. 31-46, 2008.

Multidimensional Waveforms: Possible Implementation



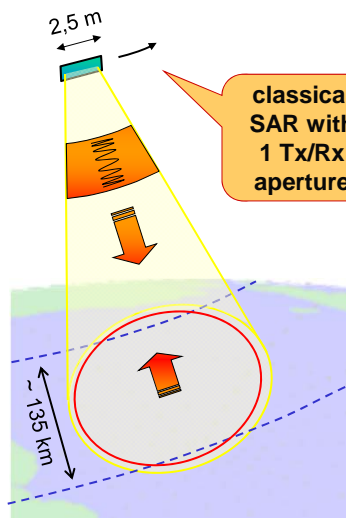
G. Krieger et al., Multidimensional Waveform Encoding: A New DBF Technique for SAR Remote Sensing, IEEE Trans. Geosci. Remote Sens., Vol. 46, pp. 31-46, 2008.

Non-Separable Waveform: Example with 3 Sub-Pulses



G. Krieger et al., Multidimensional Waveform Encoding: A New DBF Technique for SAR Remote Sensing, IEEE Trans. Geosci. Remote Sens., Vol. 46, pp. 31-46, 2008.

High-Resolution Wide-Swath SAR Imaging (X-Band)

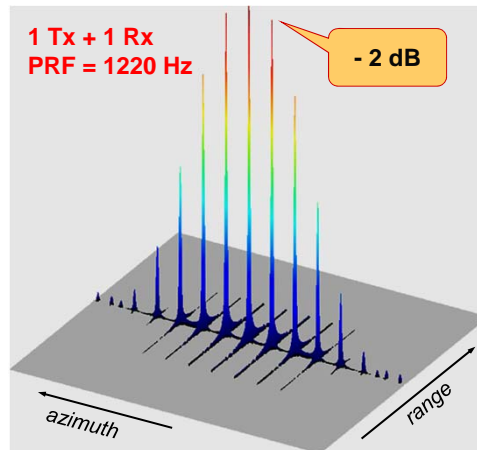


classical
SAR with
1 Tx/Rx
aperture

Point Target Response

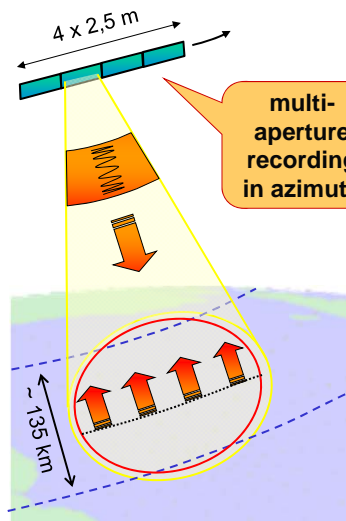
1 Tx + 1 Rx
PRF = 1220 Hz

- 2 dB



G. Krieger et al., Multidimensional Waveform Encoding: A New DBF Technique for SAR Remote Sensing, IEEE Trans. Geosci. Remote Sens., Vol. 46, pp. 31-46, 2008.

Displaced Phase Center Antenna (DPCA) Technique

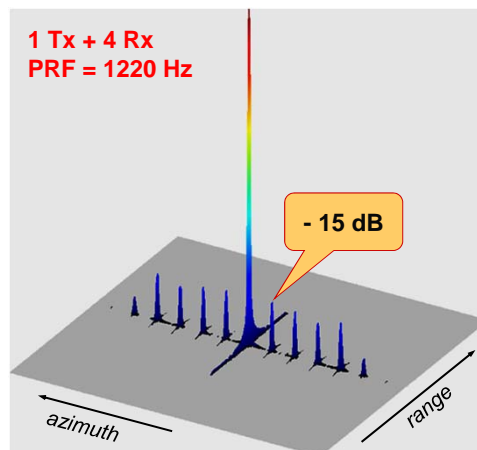


multi-
aperture
recording
in azimuth

Point Target Response

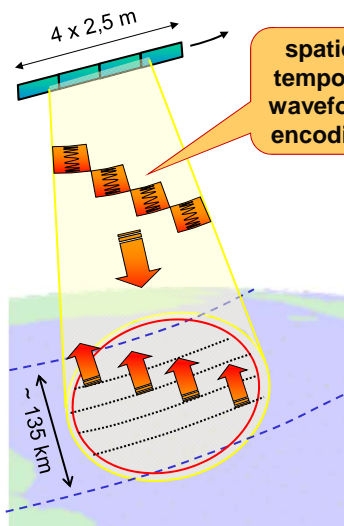
1 Tx + 4 Rx
PRF = 1220 Hz

- 15 dB



G. Krieger et al., Multidimensional Waveform Encoding: A New DBF Technique for SAR Remote Sensing, IEEE Trans. Geosci. Remote Sens., Vol. 46, pp. 31-46, 2008.

Multidimensional Waveform Encoding (MIMO SAR)

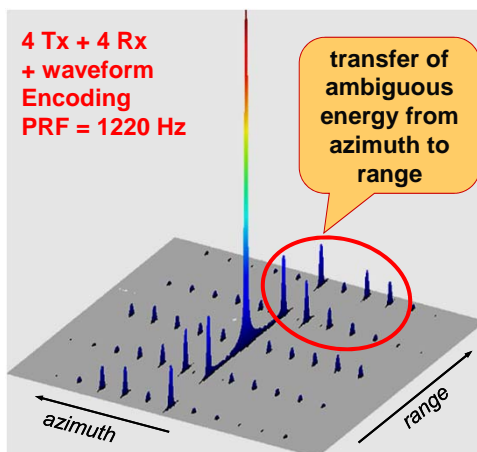


spatio-temporal waveform encoding

Point Target Response

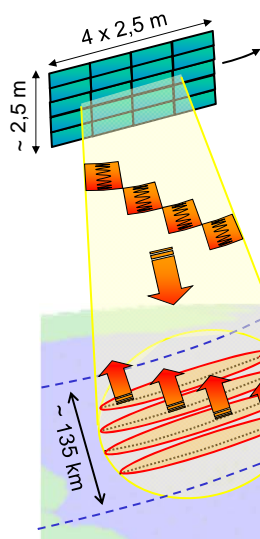
4 Tx + 4 Rx
+ waveform Encoding
PRF = 1220 Hz

transfer of ambiguous energy from azimuth to range



G. Krieger et al., Multidimensional Waveform Encoding: A New DBF Technique for SAR Remote Sensing, IEEE Trans. Geosci. Remote Sens., Vol. 46, pp. 31-46, 2008.

Multidimensional Waveform Encoding (MIMO SAR)

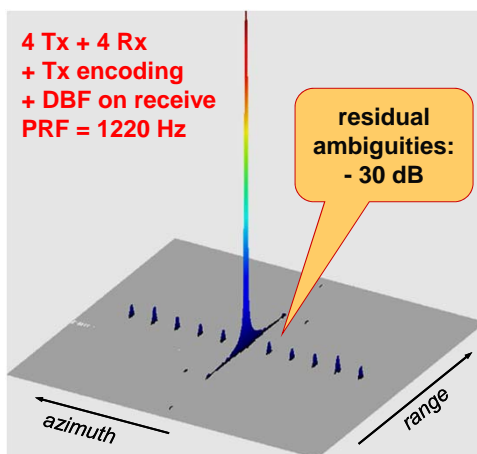


DBF on receive in elevation

Point Target Response

4 Tx + 4 Rx
+ Tx encoding
+ DBF on receive
PRF = 1220 Hz

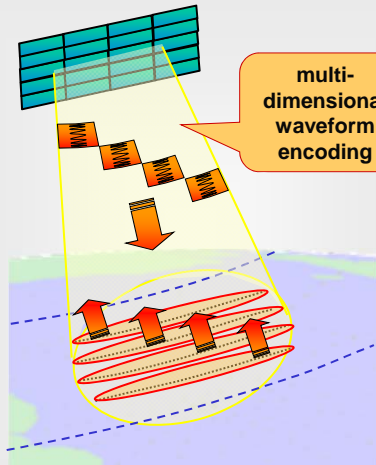
residual ambiguities:
- 30 dB



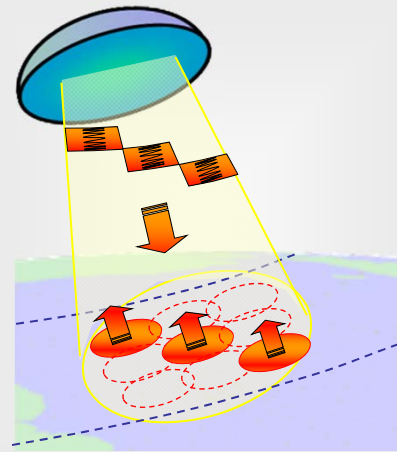
G. Krieger et al., Multidimensional Waveform Encoding: A New DBF Technique for SAR Remote Sensing, IEEE Trans. Geosci. Remote Sens., Vol. 46, pp. 31-46, 2008.

MIMO-SAR with Reflector Antennas

Direct Radiating Arrays

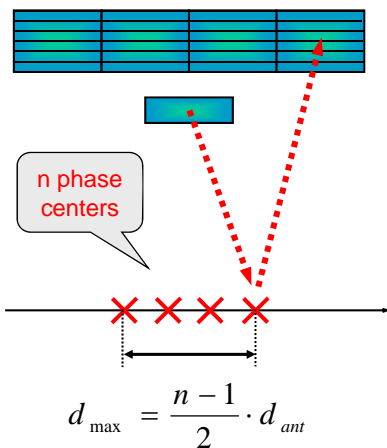


Reflectors with Digital Feed Array

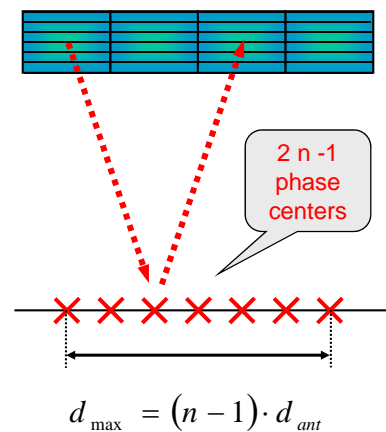


Additional Azimuth Phase Centers for Improved SAR Imaging & GMTI

Classic HRWS



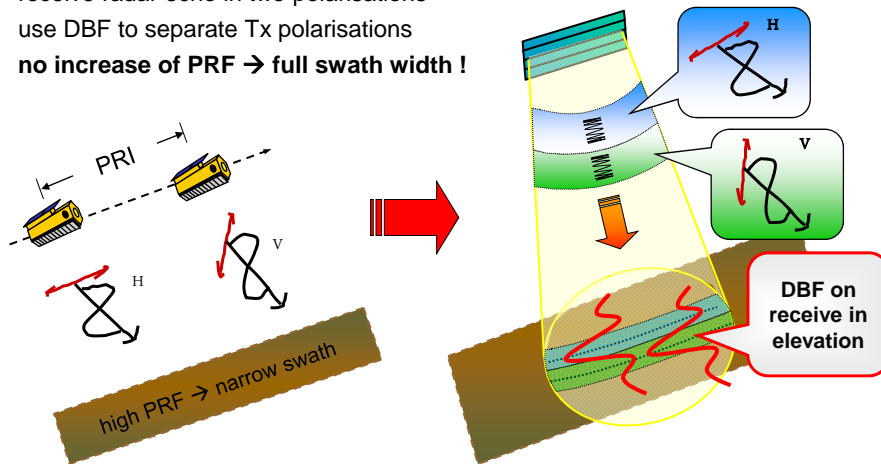
Waveform Encoding



G. Krieger et al., Multidimensional Waveform Encoding: A New DBF Technique for SAR Remote Sensing, IEEE Trans. Geosci. Remote Sens., Vol. 46, pp. 31-46, 2008.

Fully Polarimetric Waveform Encoding

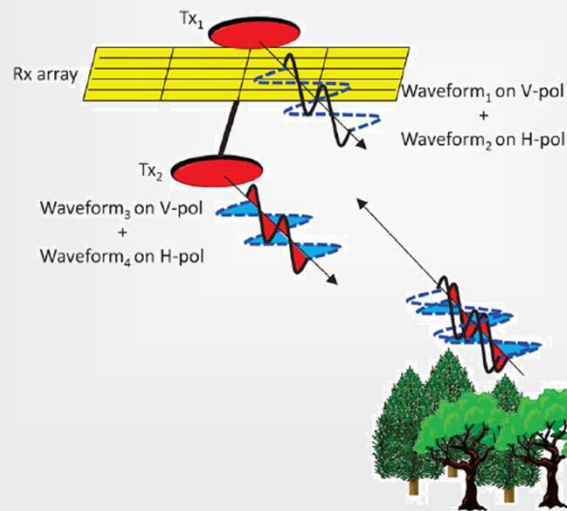
- transmit two sub-pulses with H and V → two polarisations in each Tx pulse !
- receive radar echo in two polarisations
- use DBF to separate Tx polarisations
- **no increase of PRF → full swath width !**



G. Krieger et al., Multidimensional waveform encoding for synthetic aperture radar remote sensing, Proc. IET Int. Conf. Radar Syst., Edinburgh, U.K., pp. 1–5, 2007.

Spaceborne MIMO Synthetic Aperture Radar for Multimodal Operation

Jung-Hyo Kim, Marwan Younis, *Senior Member, IEEE*,
Alberto Moreira, *Fellow, IEEE*, and Werner Wiesbeck, *Fellow, IEEE*



Orthogonal Waveforms for MIMO-SAR (Examples from Recent IEEE Publications)

$$\int s_i(t)s_j^*(t+\tau)dt = 0, i \neq j, \forall \tau \in \mathbf{R}, i, j = 1, 2, \dots, L.$$

WQ Wang, IEEE AC 2007



$$S_i(f) \cdot S_j^*(f) = 0 \quad \forall \quad f \in \mathbf{R}$$

→ no coherence for interferometry, polarimetry,
azimuth ambiguity suppression, GMTI, ...



W. Wang, Applications of MIMO Technique for Aerospace Remote Sensing,
2007 IEEE Aerospace Conference, Big Sky, MT, 2007, pp. 1-10.

Orthogonal Waveforms for MIMO-SAR (Examples from Recent IEEE Publications)

$$\int s_i(t)s_j^*(t+\tau)dt = 0, i \neq j, \forall \tau \in \mathbf{R}, i, j = 1, 2, \dots, L.$$

WQ Wang, IEEE AC 2007

$$\int_0^{T_s} s_m(t)s_n^*(t)dt = \begin{cases} c_m, & m = n \\ 0, & m \neq n \end{cases}$$

WQ Wang, IEEE TGRS 2011

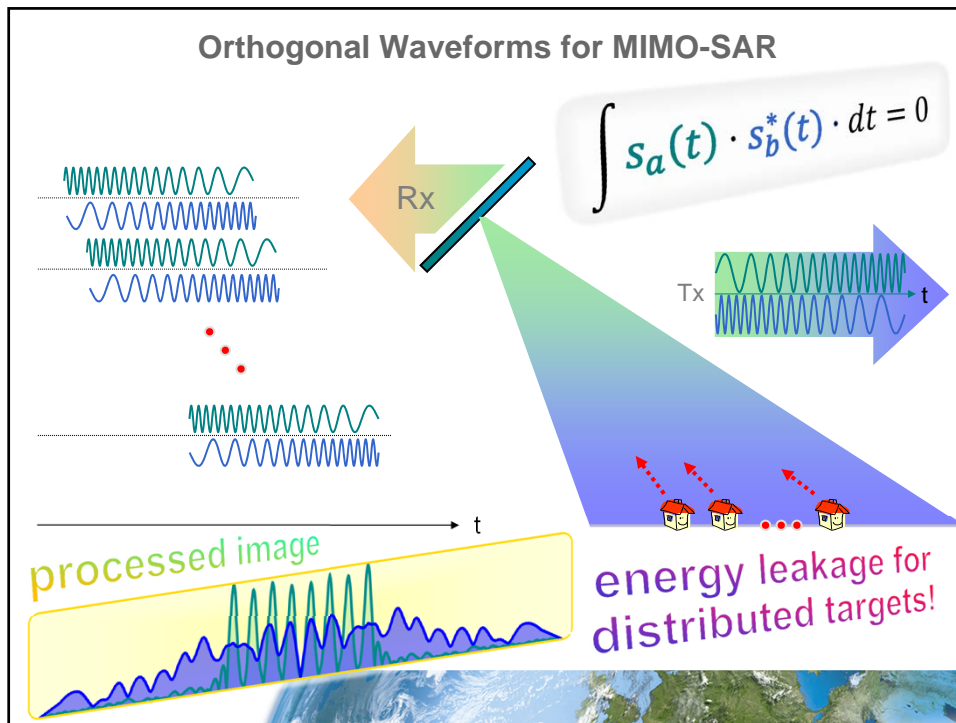
$$\int_{T_p} s_m(t)s_n^*(t)dt = \delta_{mn}, \quad (m, n) \in [1, 2, 3, \dots, K]$$

$= \delta_{mn}?$

WQ Wang, IEEE GRSL 2012



W. Wang, Applications of MIMO Technique for Aerospace Remote Sensing,
2007 IEEE Aerospace Conference, Big Sky, MT, 2007, pp. 1-10.



Orthogonal Waveforms for MIMO-SAR: Up & Down-Chirps

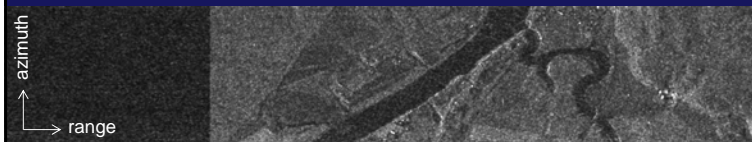
Original Scene



Matched Filter Result (only matched channel present)

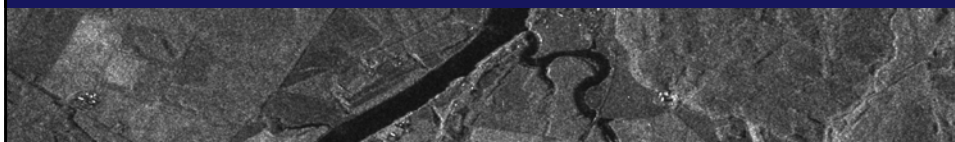


Matched Filter Result (also orthogonal channel present)

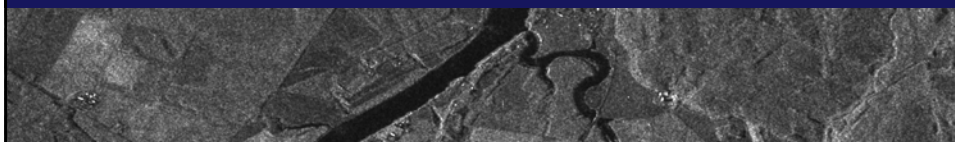


Orthogonal Waveforms for MIMO-SAR: Up & Down-Chirps

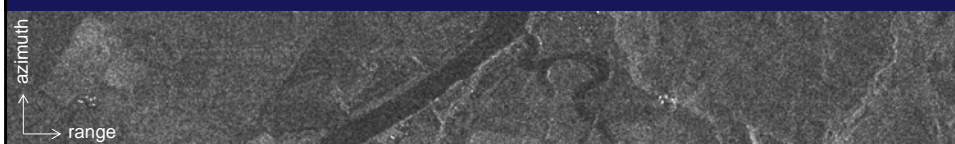
Original Scene



Matched Filter Result (only matched channel present)

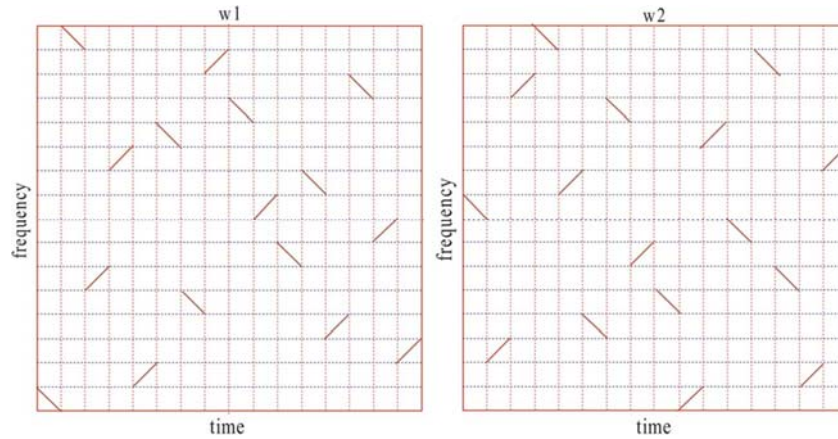


Matched Filter Result (also orthogonal channel present)



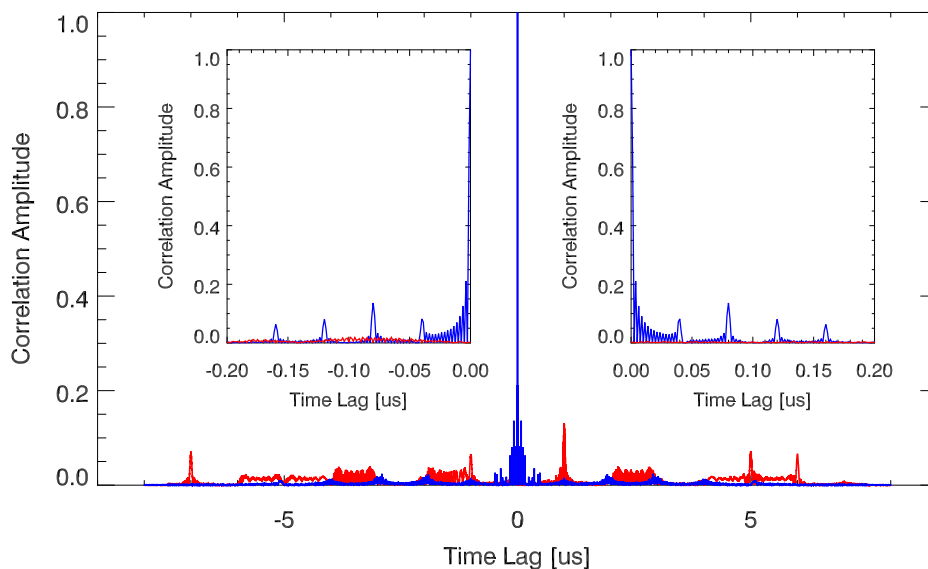
MIMO SAR OFDM Chirp Waveform Diversity Design With Random Matrix Modulation

Wen-Qin Wang, *Member, IEEE*



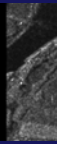
W. Q. Wang, MIMO SAR OFDM Chirp Waveform Diversity Design With Random Matrix Modulation, IEEE Trans. Geosci. Remote Sens., Vol. 53, pp. 1615-1625, 2015.

Autocorrelation and Crosscorrelation

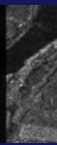
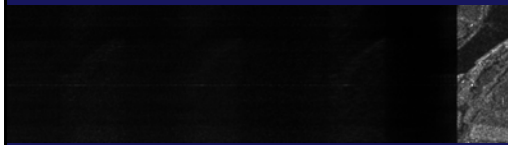


Orthogonal Waveforms for MIMO-SAR: Wen-Qin Wang 2015

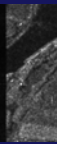
Original Scene



Matched Filter Result (only matched channel present)



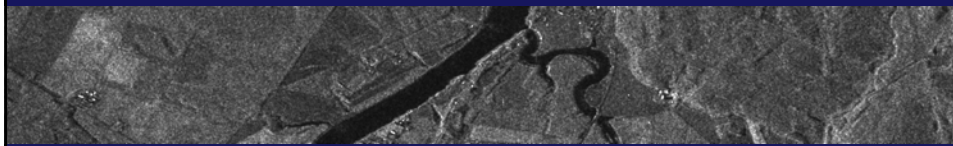
Matched Filter Result (also orthogonal channel present)



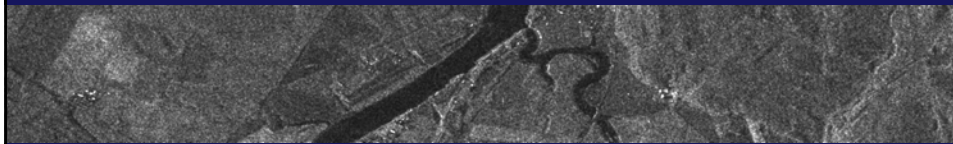
azimuth
→ range

Orthogonal Waveforms for MIMO-SAR: Wen-Qin Wang 2015

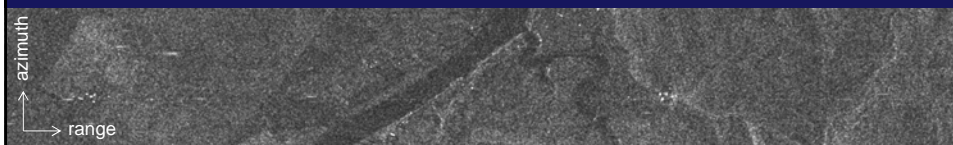
Original Scene



Matched Filter Result (only matched channel present)



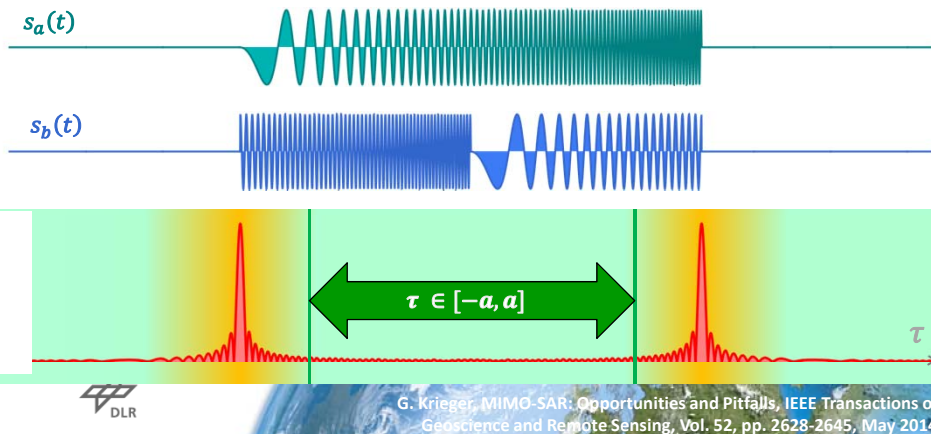
Matched Filter Result (also orthogonal channel present)



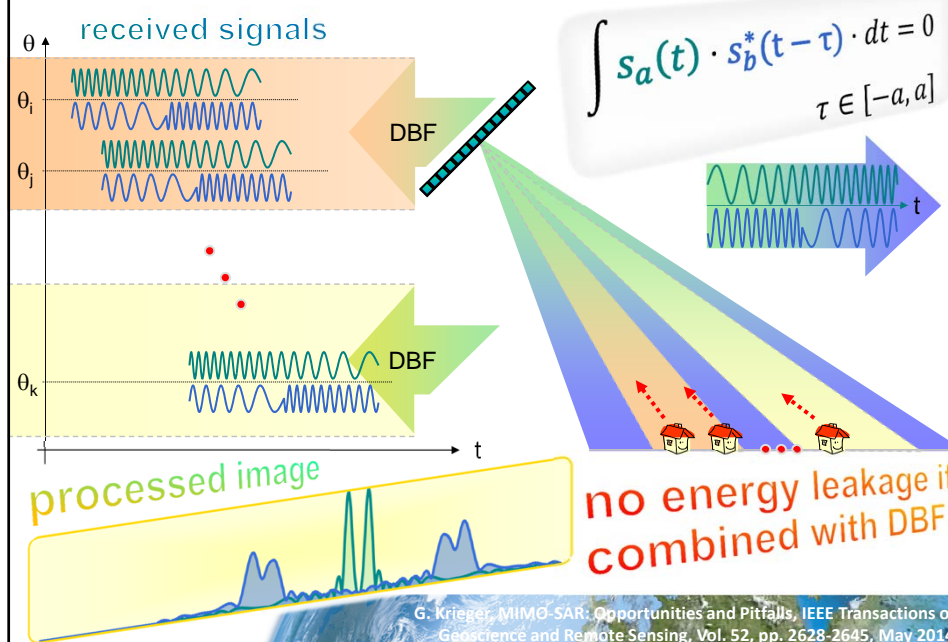
azimuth
→ range

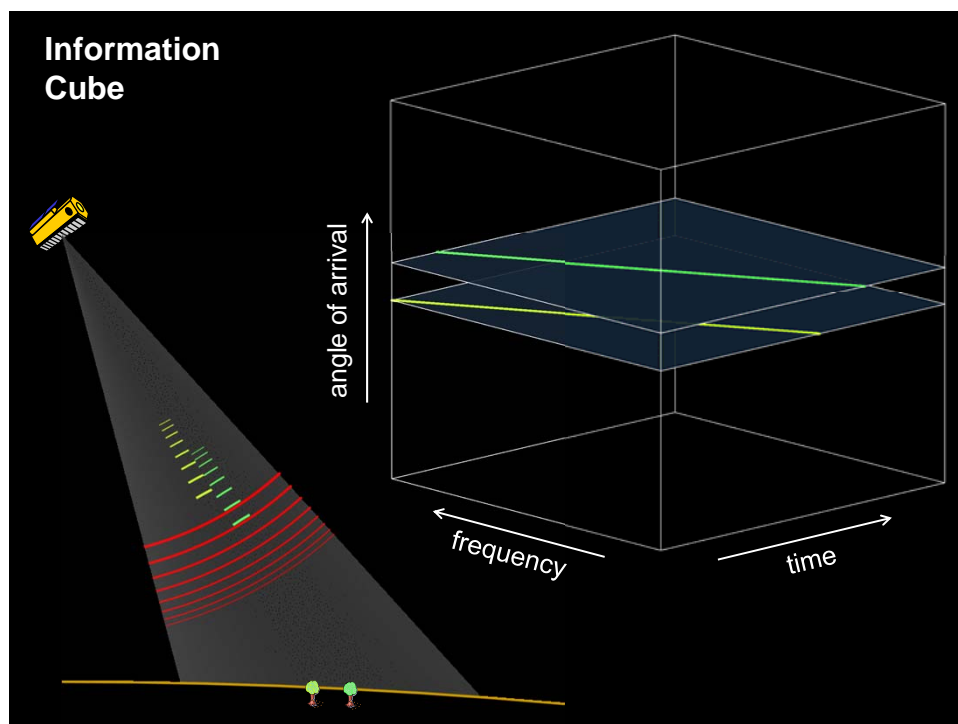
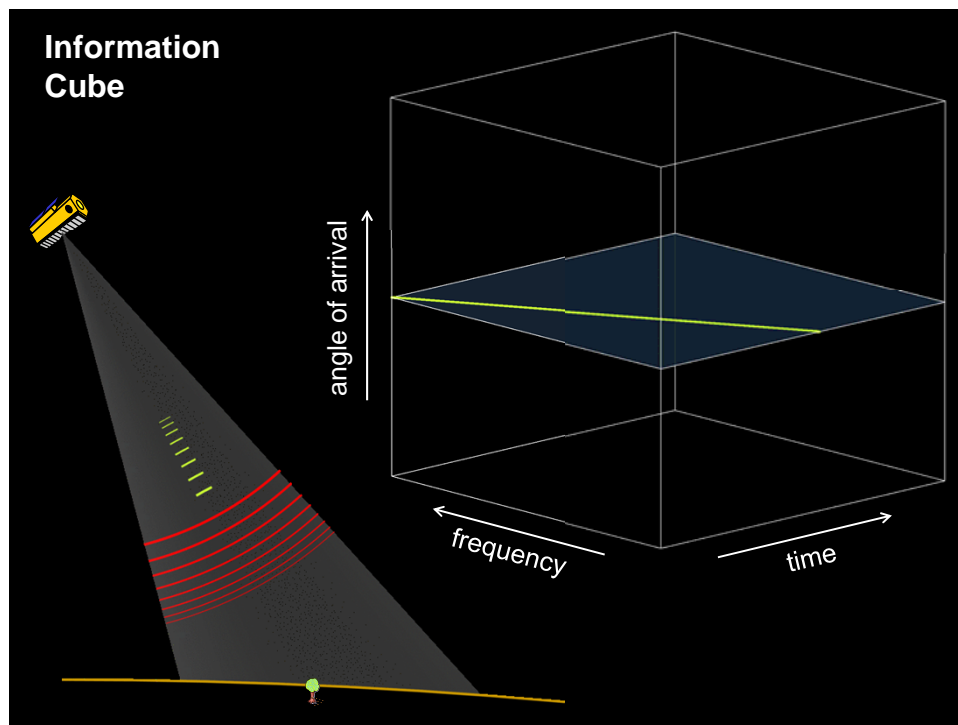
Short-Term Shift-Orthogonal Waveforms for MIMO-SAR

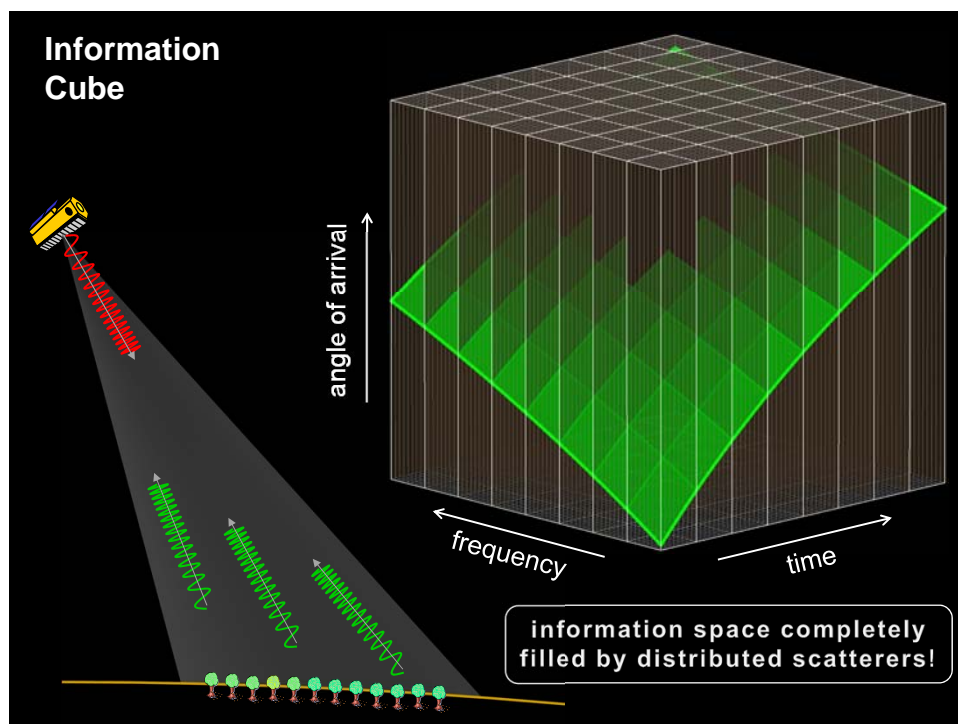
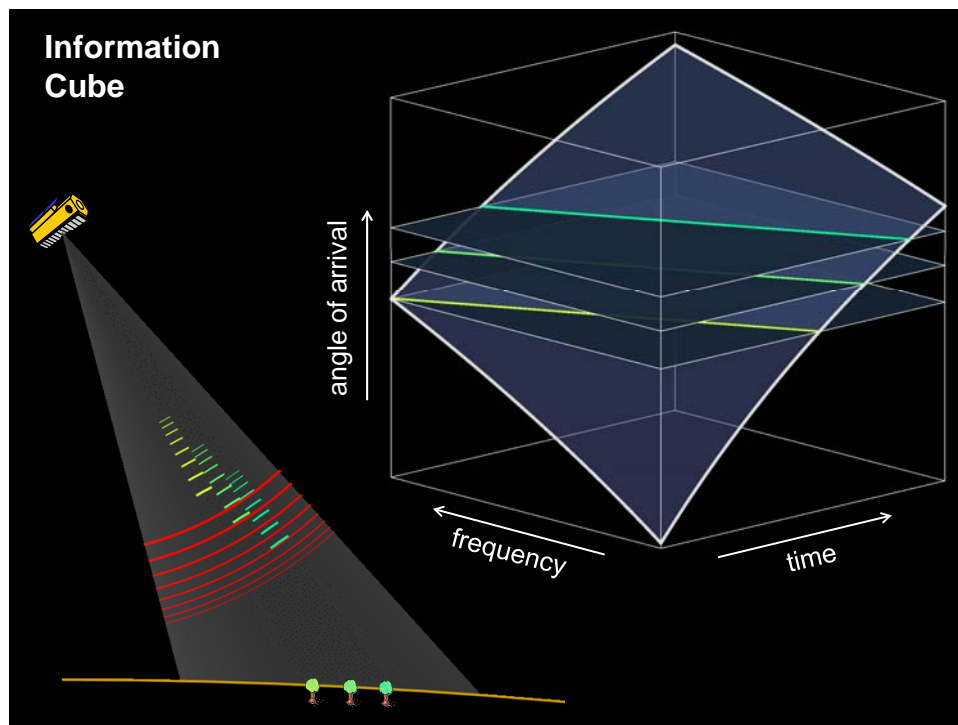
$$\int s_a(t) \cdot s_b^*(t - \tau) \cdot dt = 0 \quad \forall \quad \tau \in [-a, a]$$

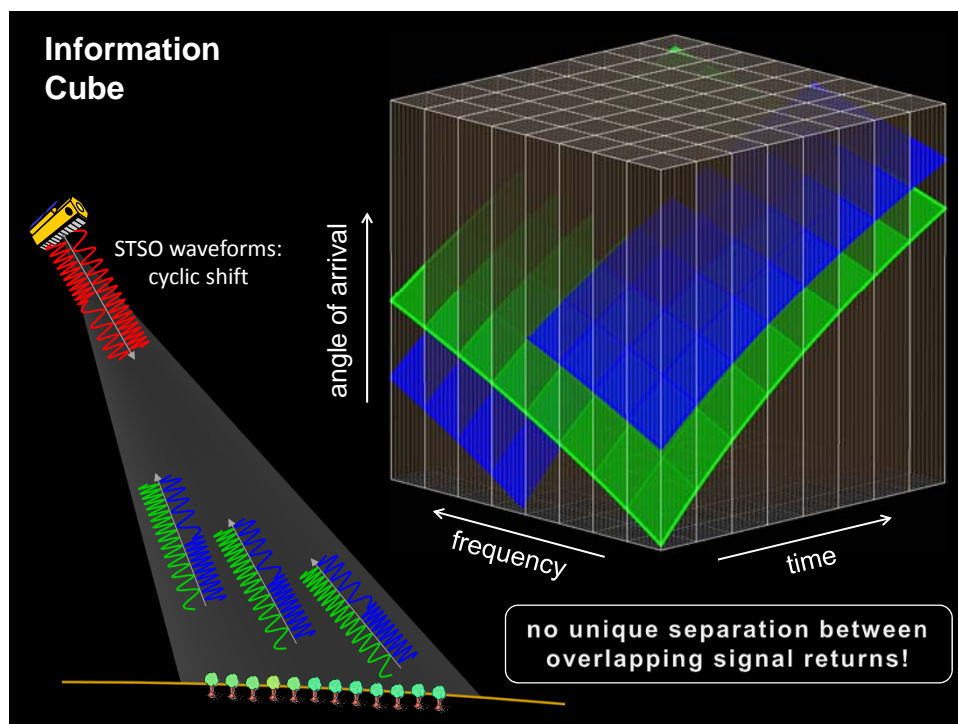
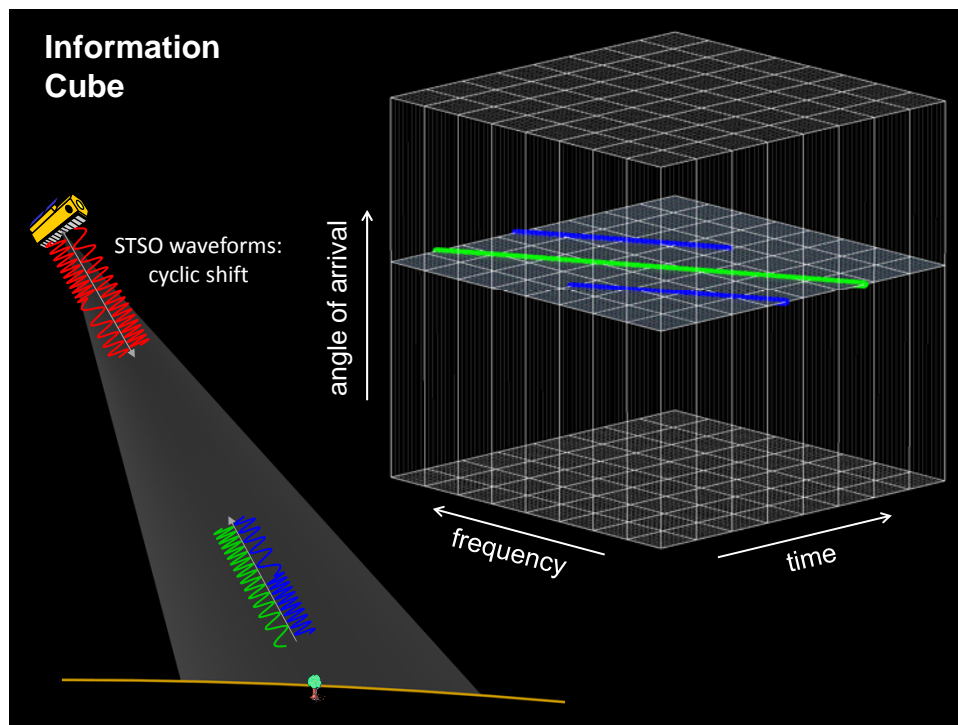


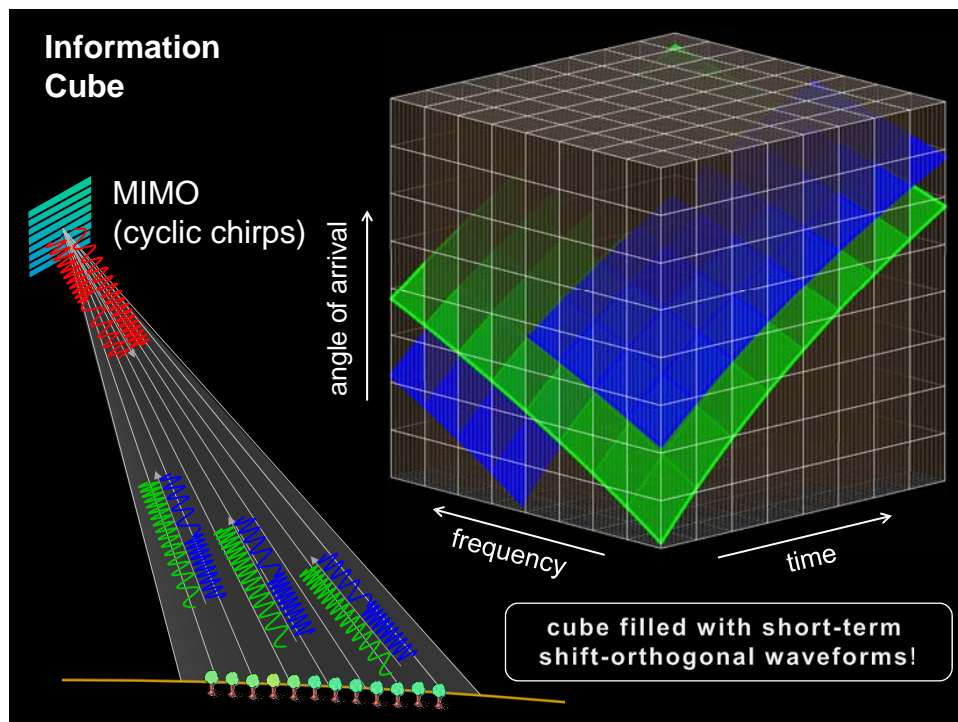
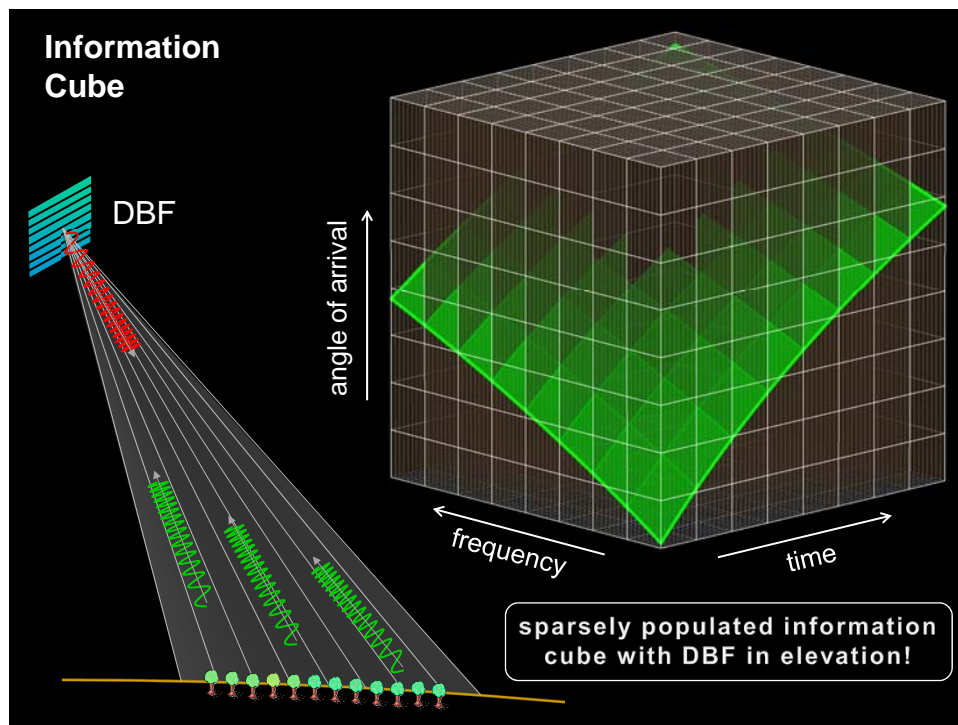
Short-Term Shift-Orthogonal Waveforms for MIMO-SAR

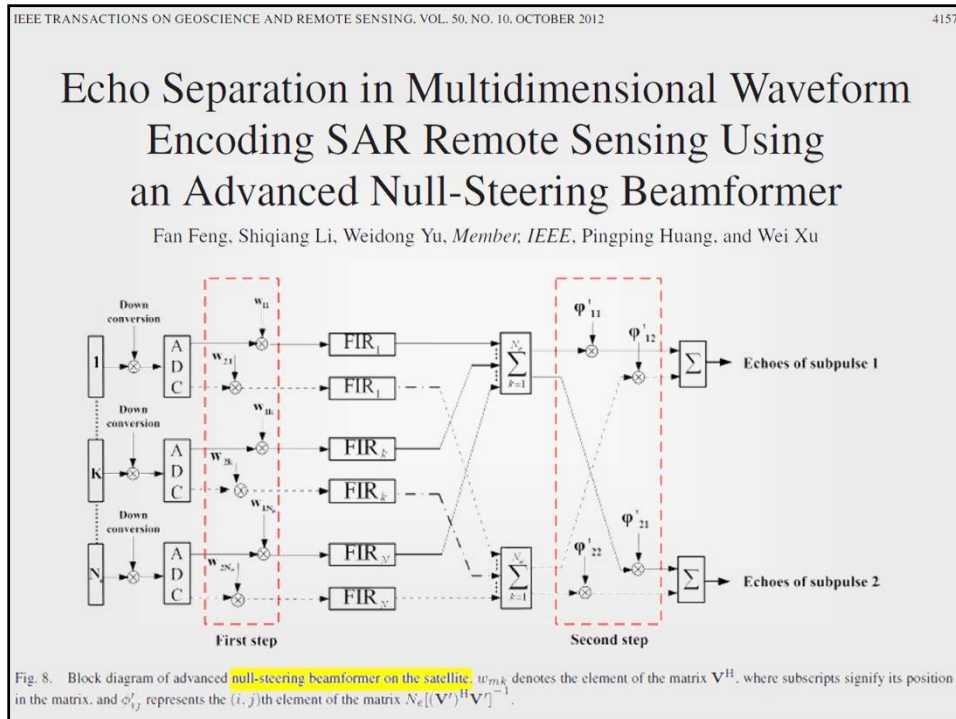
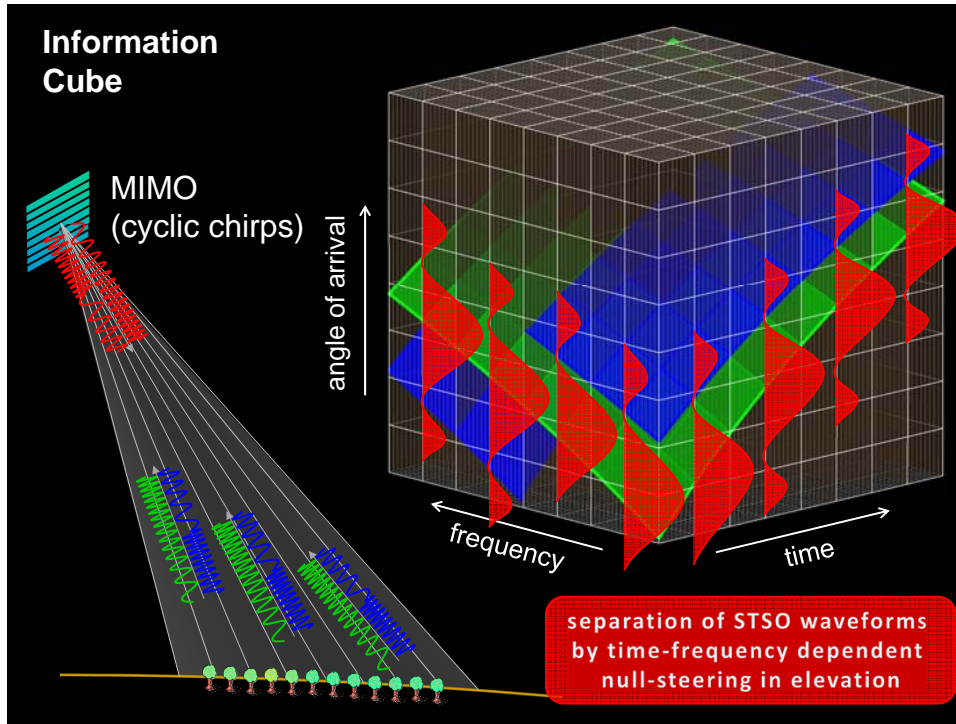






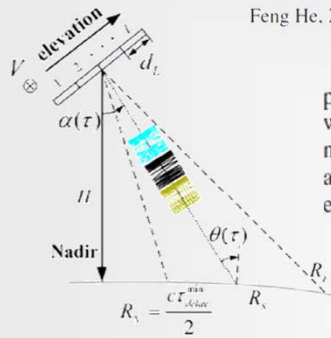






Digital Beamforming on Receive in Elevation for Multidimensional Waveform Encoding SAR Sensing

Feng He, Xile Ma, Zhen Dong, and Diannong Liang



In this letter, the performance of the separation approach employing *a posteriori* DBF in elevation is investigated in detail. It was originally suggested in [2] and was employed in [9] with a novel full polarimetric SAR mode. This way, useful information about the spatial structure in elevation will be preserved to enable flexible and adaptive beamforming on the ground. An

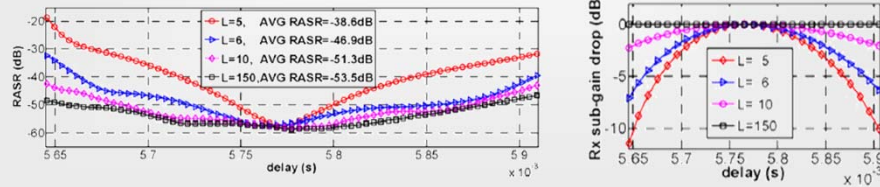
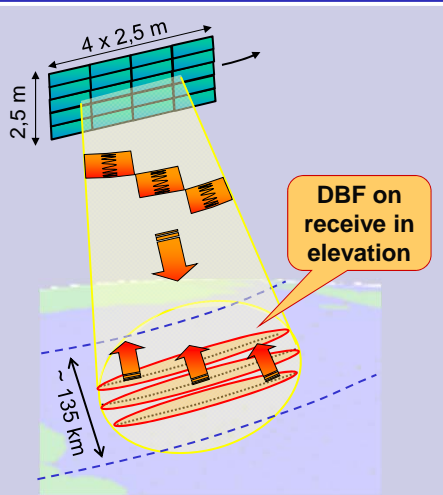


Fig. 3. RASR versus ground delay employing different elevation subapertures.

A Closer Look to Null-Steering

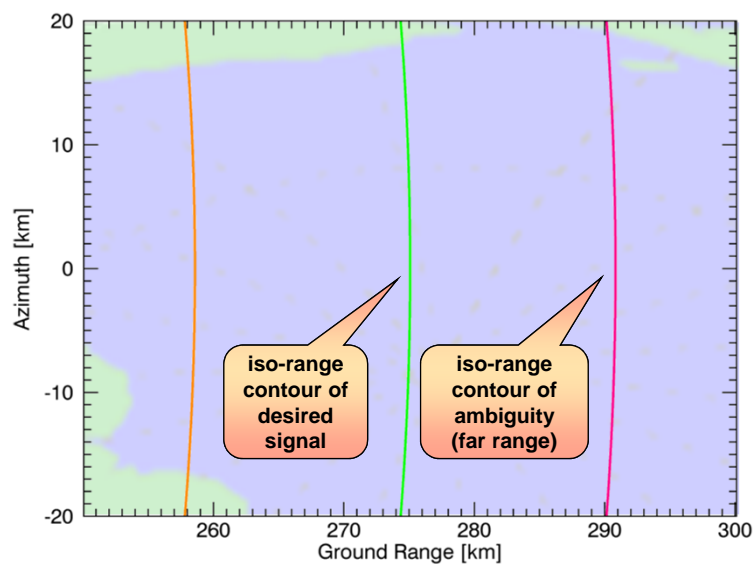


Example 1: Range Ambiguities for Planar Array

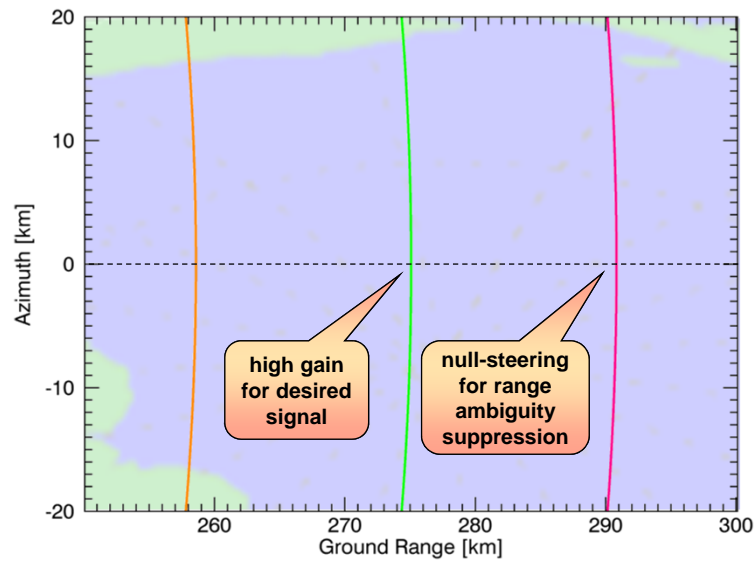
Antenna height	h_{ant}	2.5 m	
Antenna height	l_{ant}	4 x 2.5 m	
Wavelength	λ	0.031 m	
Satellite height	z_{sat}	576 km	
Height offset	dh	1.5 km	
Satellite velocity	v_{sat}	7.5 km/s	
Earth radius	r_e	6378 km	
Look angle	θ_{look}	32.4°	
Sub-pulse delay	$\Delta\tau$	50 μ s	



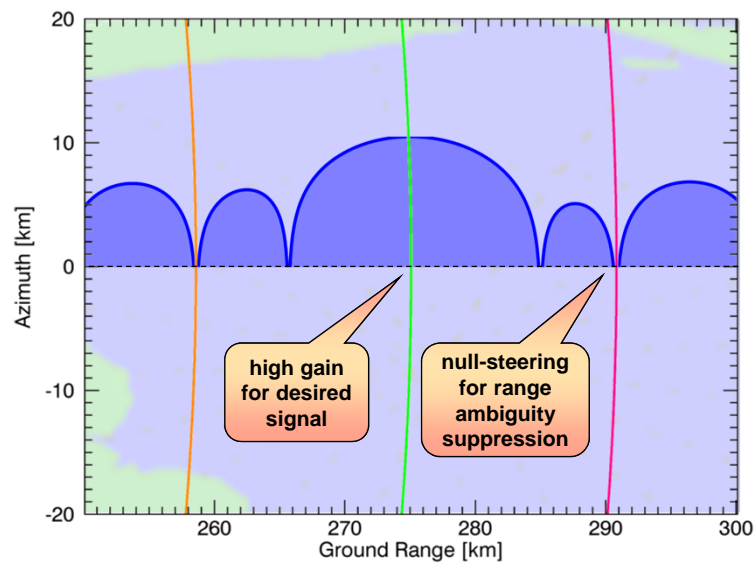
Iso-Range Contours on Earth Surface



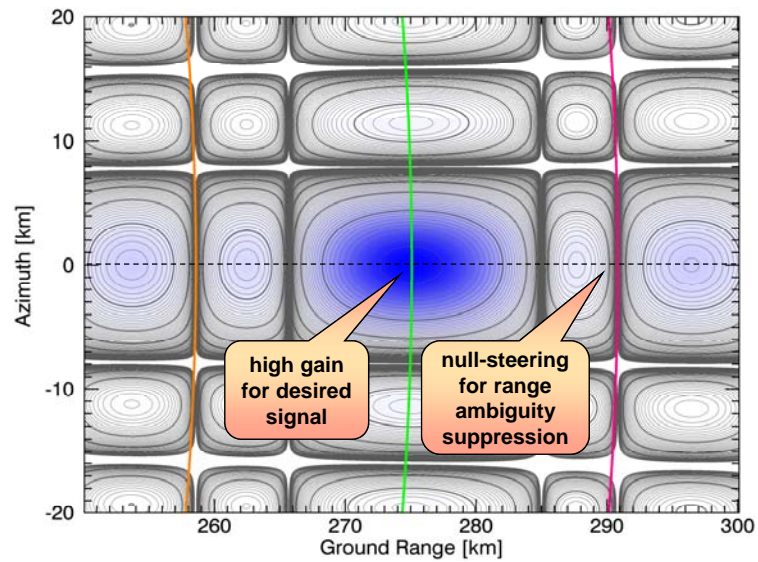
Null-Steering in Elevation for Zero-Doppler Position



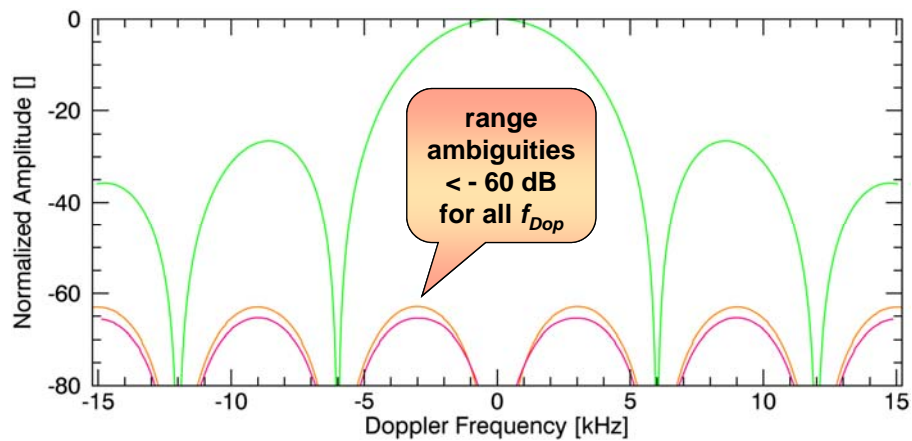
Null-Steering in Elevation for Zero-Doppler Position



Null-Steering in Elevation: 2-D Pattern on Ground



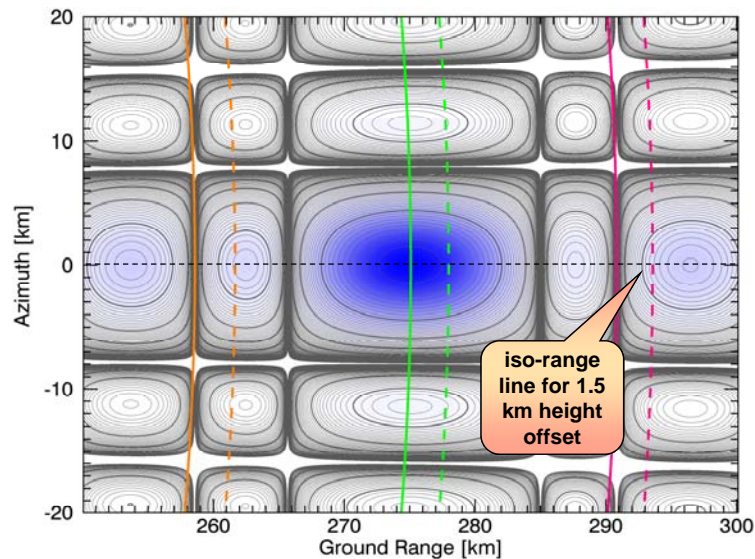
Null-Steering in Elevation: Azimuth Patterns



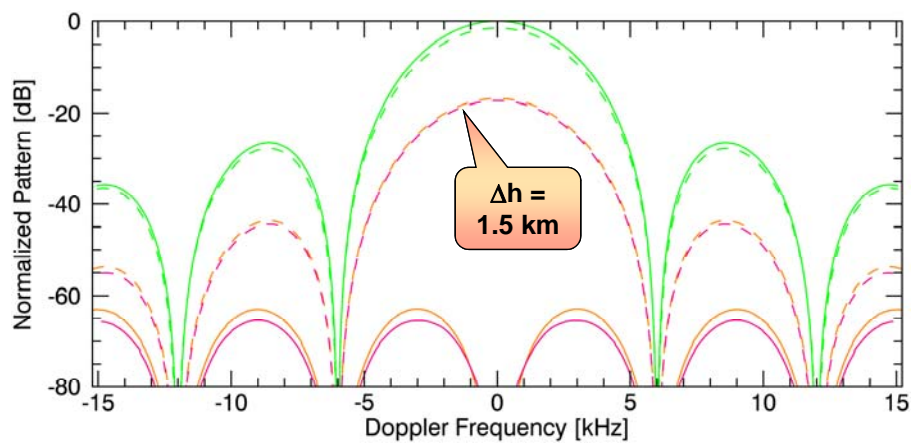
- At nominal height:
- high gain for desired signal
 - excellent suppression of ambiguities



Null-Steering in Elevation: Impact of Topography



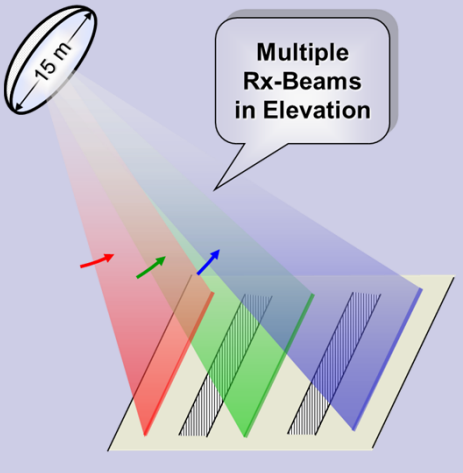
Null-Steering in Elevation: Impact of Topography



Height of 1.5 km has: ☐ minor impact on main beam ($< 1.5 \text{ dB}$)
☐ strong impact on nulling ($-60 \rightarrow -17 \text{ dB}$)

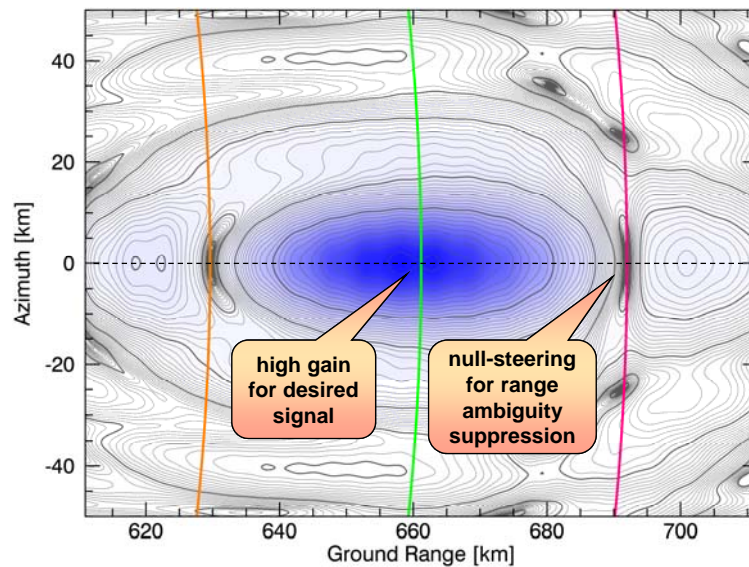


Example 2: Range Ambiguities for Reflector DBF

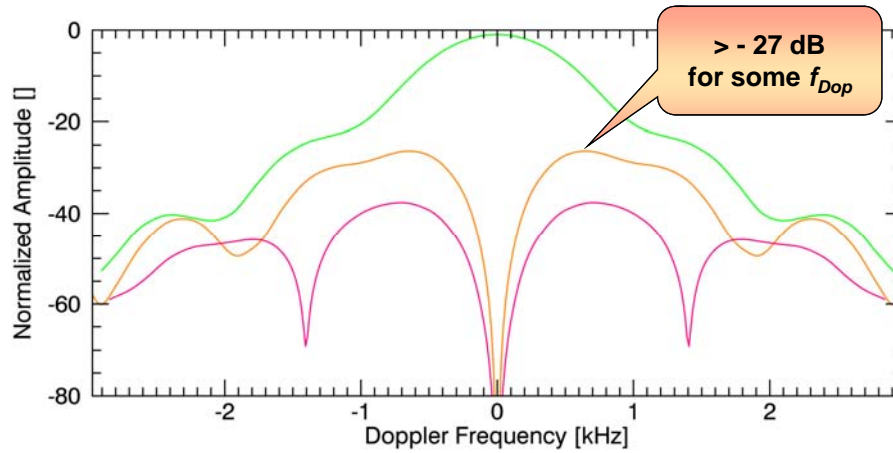
Antenna diameter	d_{ant}	15 m	 <p>Multiple Rx-Beams in Elevation</p>
Feed elements	n_{el}	32	
Wavelength	λ	0.236 m	
Satellite height	z_{sat}	745 km	
Height offset	dh	3 km	
Satellite velocity	v_{sat}	7 km/s	
Earth radius	r_e	6378 km	
Steering angle	θ_{steer}	7.864°	
PRI	$\Delta\tau$	150 μ s	



Null-Steering in Elevation: Pattern in Ground Plane



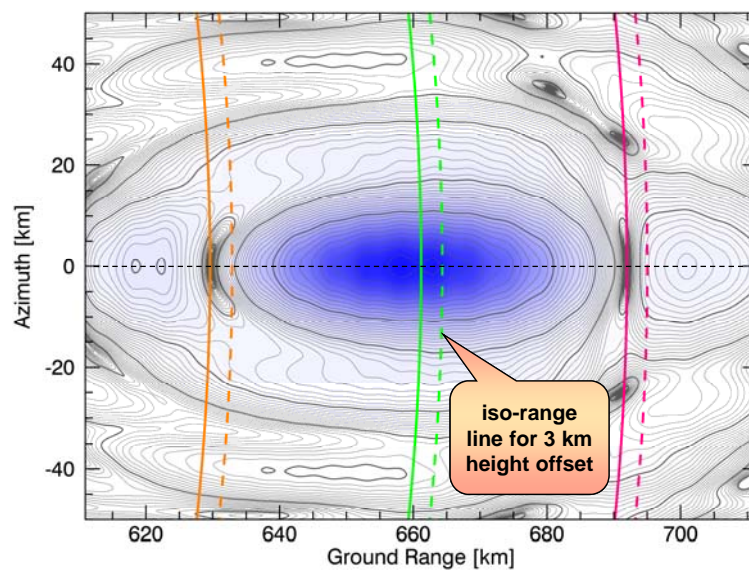
Null-Steering in Elevation: Azimuth Patterns



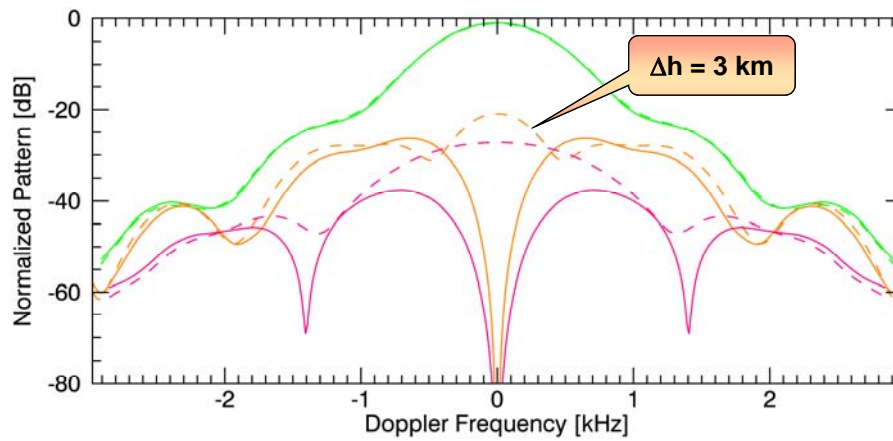
- At nominal height:
- only -27 dB suppression for some f_{Dop}
 - challenges fully polarimetric mode



Null-Steering in Elevation: Impact of Topography



Null-Steering in Elevation: Impact of Topography



- Height of 3 km has:
- ☐ negligible impact on main beam
 - ☐ strong impact on nulling

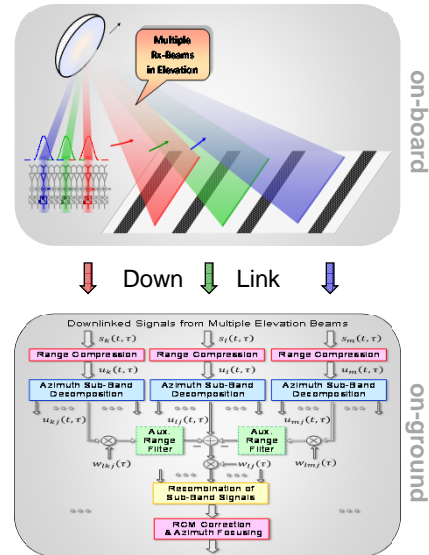


CEBRAS

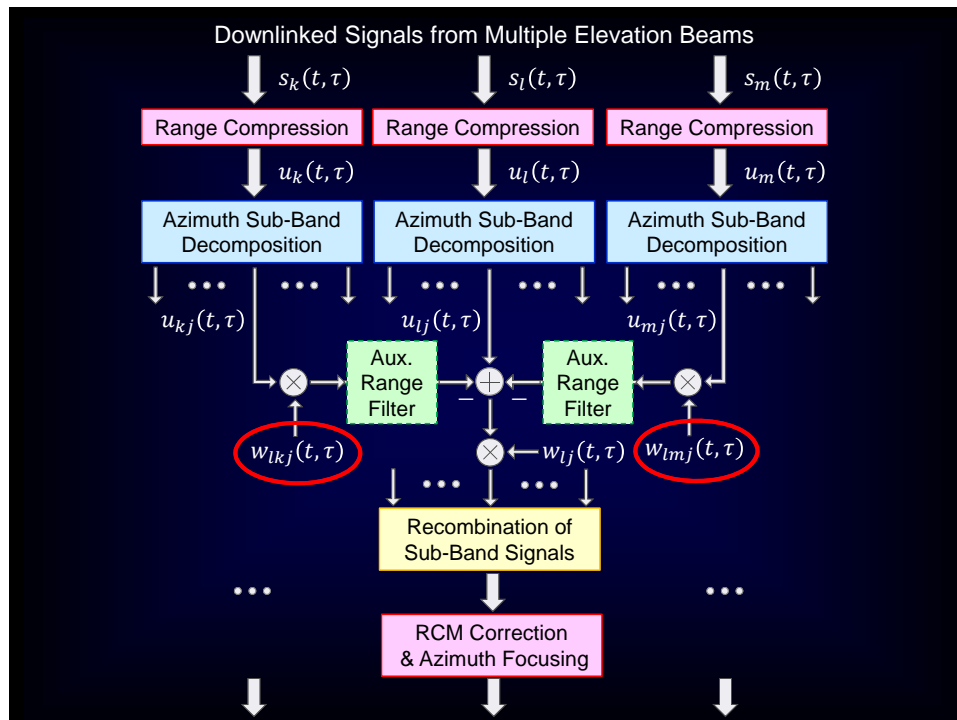


Cross Elevation Beam Range Ambiguity Suppression

- On-board scan-on-receive with multiple elevation beams
 - ❑ dispersive beams to account for extended pulses
 - ❑ beams follow topography (MVDR beamformer and coarse DEM)
- On-ground range ambiguity suppression by combining beam signals
 - ❑ beamforming in range-Doppler domain to account for topography changes in azimuth (based on high-res. DEM)
 - ❑ can take into account auxiliary data (platform orientation, calibration data, refined beam patterns,)



G. Krieger et al., CEBRAS: Cross-elevation beam range ambiguity suppression for high-resolution wide-swath and MIMO-SAR imaging, IGARSS 2015.



Beamforming Weights: Simple Solution

- Cancellation weights can be approximated by

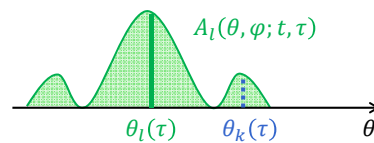
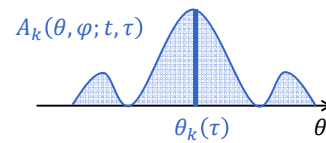
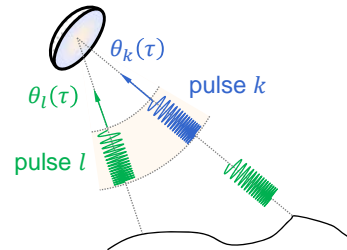
$$w_{lkj}(t, \tau) = \frac{A_l(\theta_l(\tau + \tau_{kl}, f_j), \varphi_l(\tau + \tau_{kl}, f_j); t, \tau)}{A_k(\theta_k(\tau, f_j), \varphi_k(\tau, f_j); t, \tau)}$$

with $\theta_k(\tau) = \theta_l(\tau + \tau_{kl})$

- Computation of beamforming weights

$w_{lkj}(\tau)$ requires knowledge about

- complex antenna patterns after real-time scan-on-receive beamforming $A_{\{k,l\}}(\theta, \varphi; t, \tau)$
- antenna look angles $\theta_{\{k,l\}}$ and azimuth angles $\varphi_{\{k,l\}}$ of arriving wavefronts (derived from DEM together with a posteriori satellite attitude and position estimates)



G. Krieger et al., CEBRAS: Cross-elevation beam range ambiguity suppression for high-resolution wide-swath and MIMO-SAR imaging, IGARSS 2015.

Estimation of Antenna Patterns / Cancellation Weights

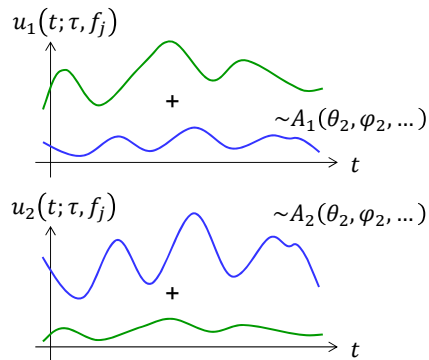
- Option 1: A Priori Antenna Model
 - employ 2-D model for computation of beam patterns
 - accuracy may be challenging for reflector system
- Option 2: Calibration Data Takes
 - illuminate with low PRI and receive with multiple beams
 - topography can be emulated by varying beam trigger times
- Option 3: Cross-Correlation
 - cross-correlate signals from multiple beams
 - prone to „self-cancellation“
- Option 4: Blind Source Separation
 - unmix signals as in cocktail party effect
 - requires use of higher-order statistics



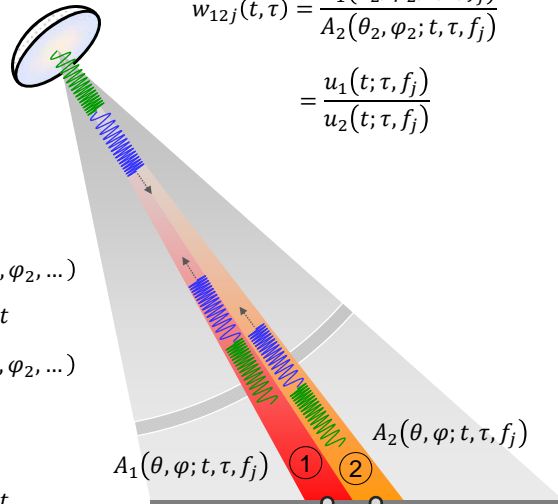
G. Krieger et al., CEBRAS: Cross-elevation beam range ambiguity suppression for high-resolution wide-swath and MIMO-SAR imaging, IGARSS 2015.

Option 2: Dedicated Calibration Data Takes

- Acquire multi-beam data without range ambiguities
 - MIMO-SAR: employ e.g. single Tx channel/sub-pulse



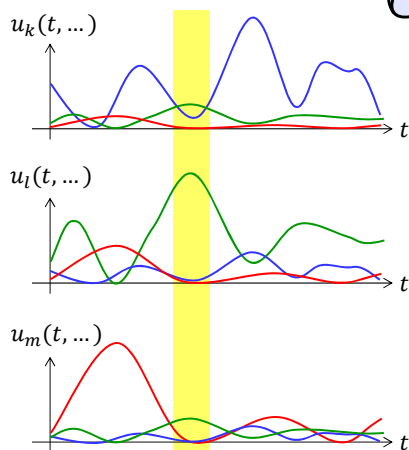
$$w_{12j}(t, \tau) = \frac{A_1(\theta_2, \varphi_2; t, \tau, f_j)}{A_2(\theta_2, \varphi_2; t, \tau, f_j)} = \frac{u_1(t; \tau, f_j)}{u_2(t; \tau, f_j)}$$



G. Krieger et al., CEBRAS: Cross-elevation beam range ambiguity suppression for high-resolution wide-swath and MIMO-SAR imaging, IGARSS 2015.

Option 3: Pattern Ratios from Cross-Correlation

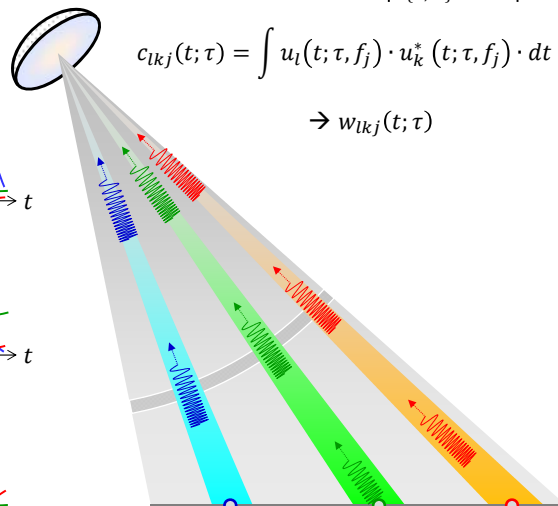
- Operate SAR in nominal multiple beam mode



for all t where $|u_l(t, \dots)| \gg |u_{\{k,m\}}(t, \dots)|$ do

$$c_{lkj}(t; \tau) = \int u_l(t; \tau, f_j) \cdot u_k^*(t; \tau, f_j) \cdot dt$$

$$\rightarrow w_{lkj}(t; \tau)$$

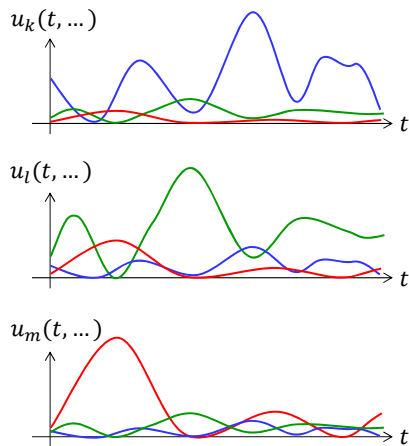


G. Krieger et al., CEBRAS: Cross-elevation beam range ambiguity suppression for high-resolution wide-swath and MIMO-SAR imaging, IGARSS 2015.

Option 4: Blind Source Separation

- Operate SAR in nominal multiple beam mode

$$\begin{bmatrix} u_1(t; \dots) \\ \vdots \\ u_N(t; \dots) \end{bmatrix} = \begin{bmatrix} a_{11} & \dots & a_{1N} \\ \vdots & \ddots & \vdots \\ a_{N1} & \dots & a_{NN} \end{bmatrix} \cdot \begin{bmatrix} s_1(t; \dots) \\ \vdots \\ s_N(t; \dots) \end{bmatrix}$$

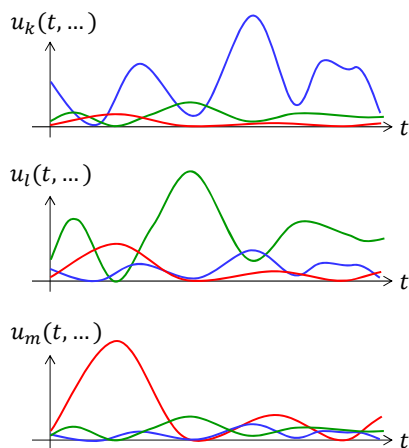


G. Krieger et al., CEBRAS: Cross-elevation beam range ambiguity suppression for high-resolution wide-swath and MIMO-SAR imaging, IGARSS 2015.

Option 4: Blind Source Separation

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- Each recorded signal can be regarded as a linear superposition of statistically independent source signals
- Independent component analysis can be used to separate the source signals
 - entropy maximization
 - minimize mutual information
 - higher-order decorrelation (cumulants)
 - infomax
 - ...

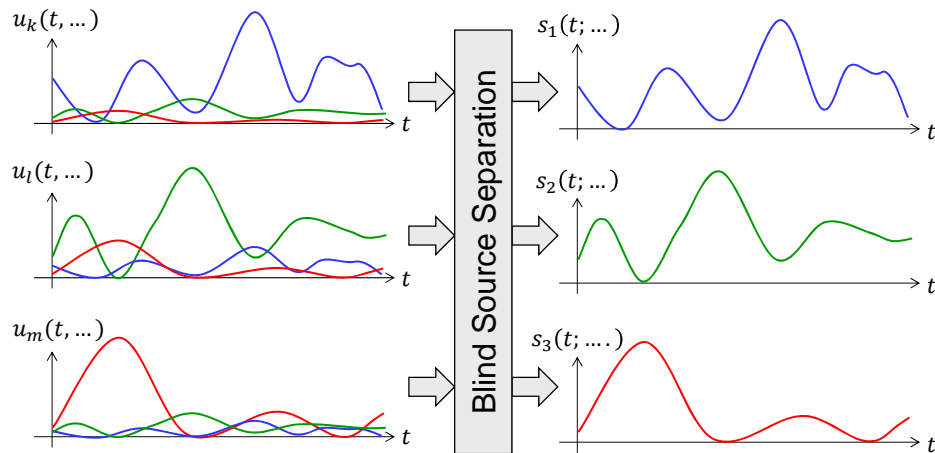


G. Krieger et al., CEBRAS: Cross-elevation beam range ambiguity suppression for high-resolution wide-swath and MIMO-SAR imaging, IGARSS 2015.

Option 4: Blind Source Separation

- Operate SAR in nominal multiple beam mode

$$\begin{bmatrix} u_1(t; \dots) \\ \vdots \\ u_N(t; \dots) \end{bmatrix} = \begin{bmatrix} a_{11} & \dots & a_{1N} \\ \vdots & \ddots & \vdots \\ a_{N1} & \dots & a_{NN} \end{bmatrix} \cdot \begin{bmatrix} s_1(t; \dots) \\ \vdots \\ s_N(t; \dots) \end{bmatrix}$$

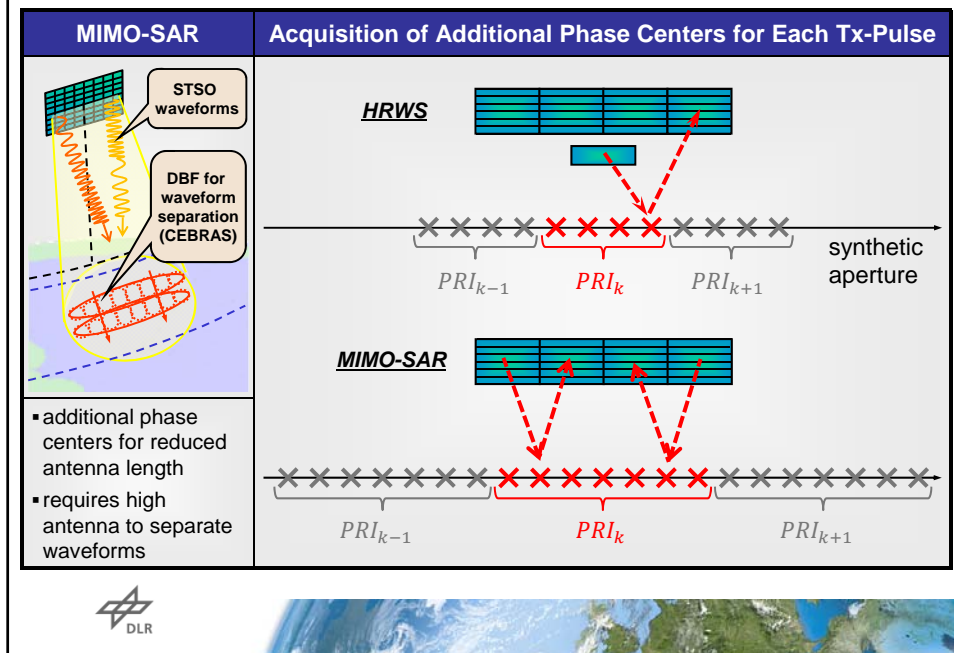


G. Krieger et al., CEBRAS: Cross-elevation beam range ambiguity suppression for high-resolution wide-swath and MIMO-SAR imaging, IGARSS 2015.

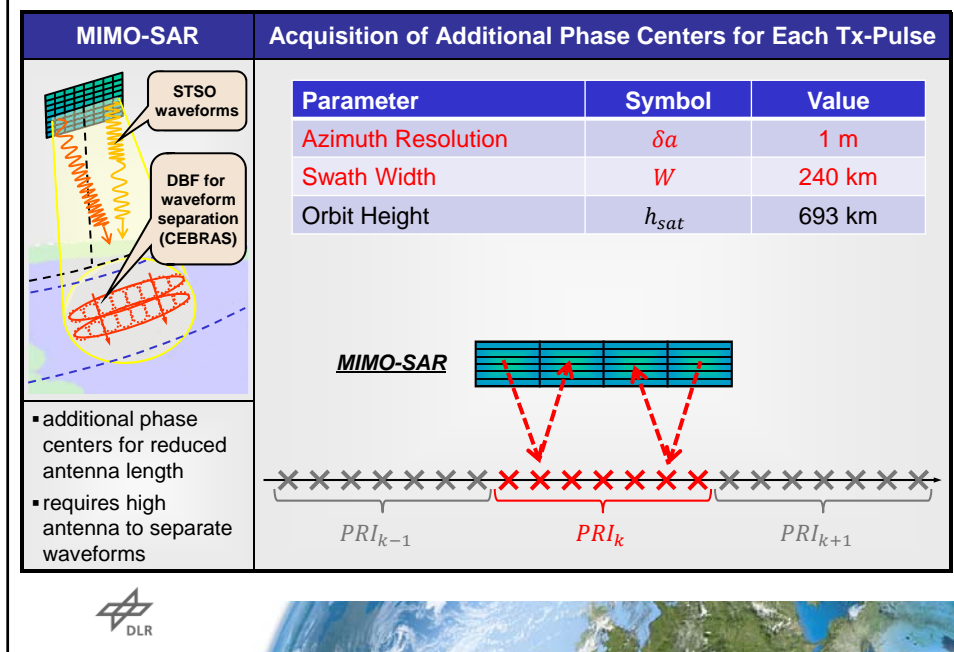
MIMO SAR Design Example



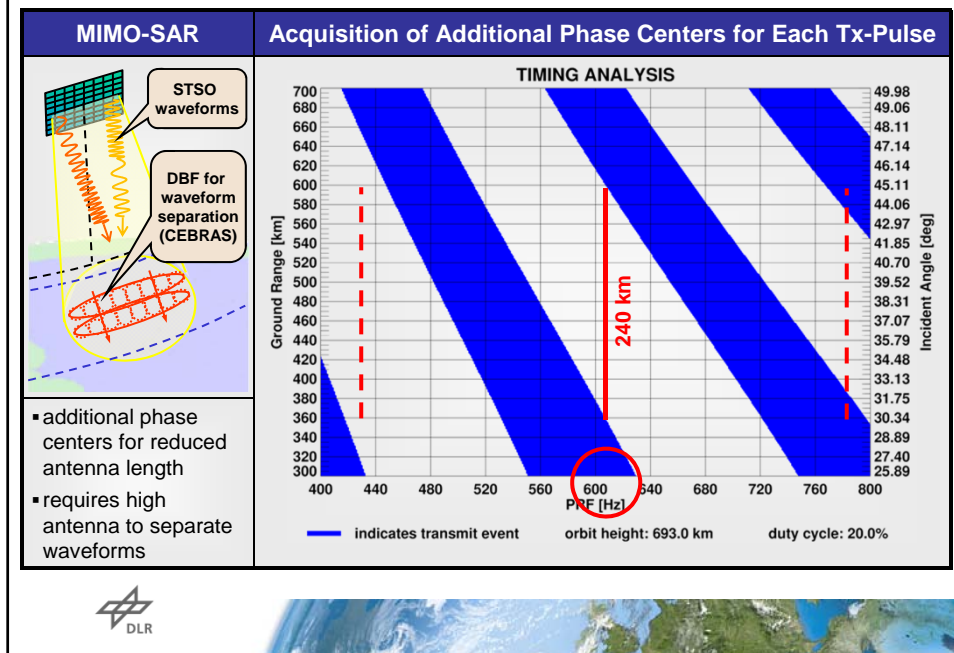
MIMO-SAR Systems with Planar Arrays



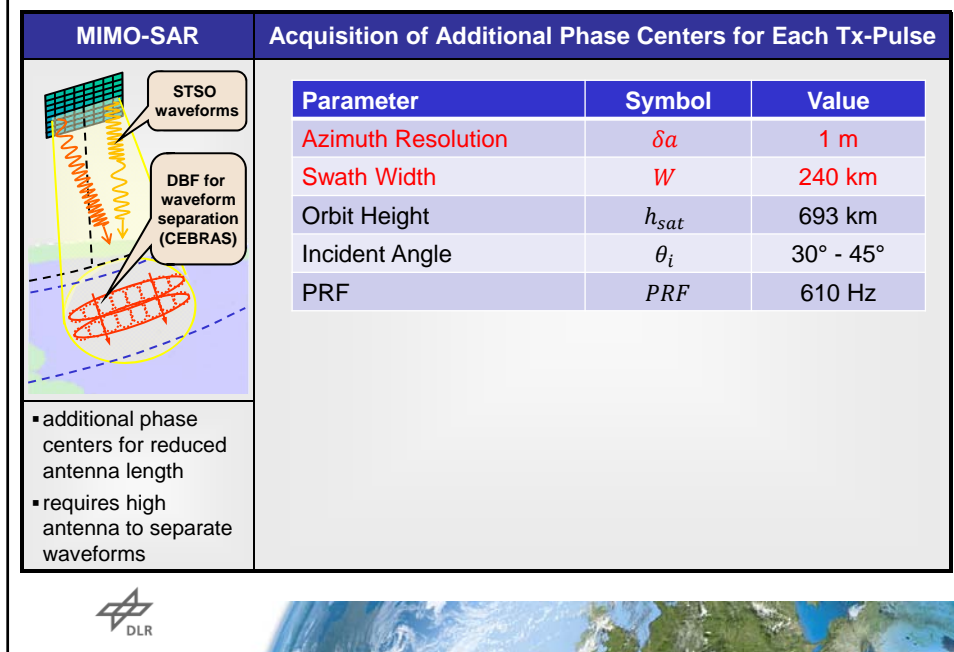
MIMO-SAR Systems with Planar Arrays



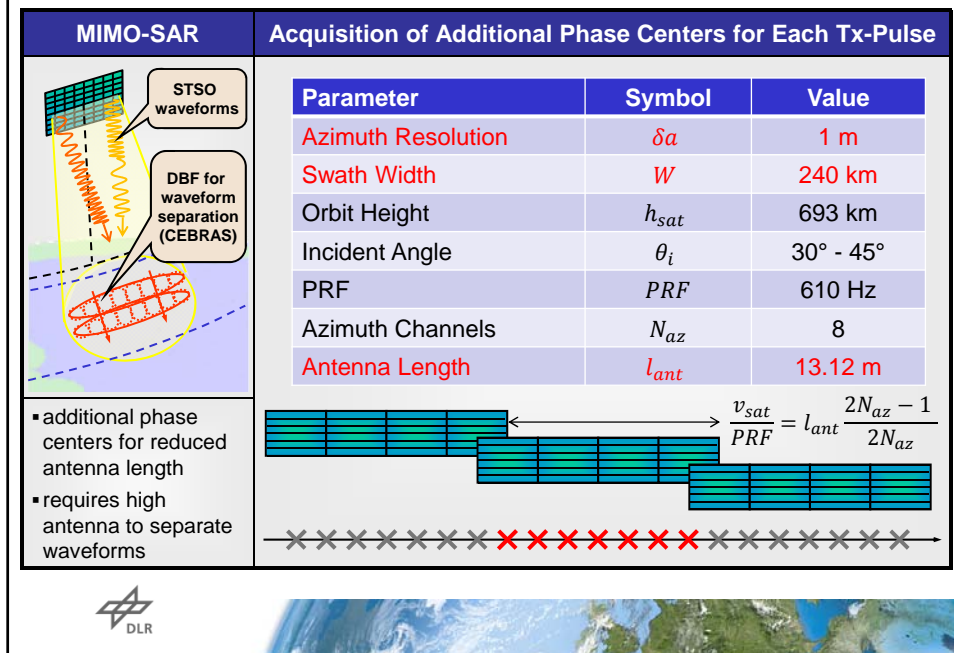
MIMO-SAR Systems with Planar Arrays



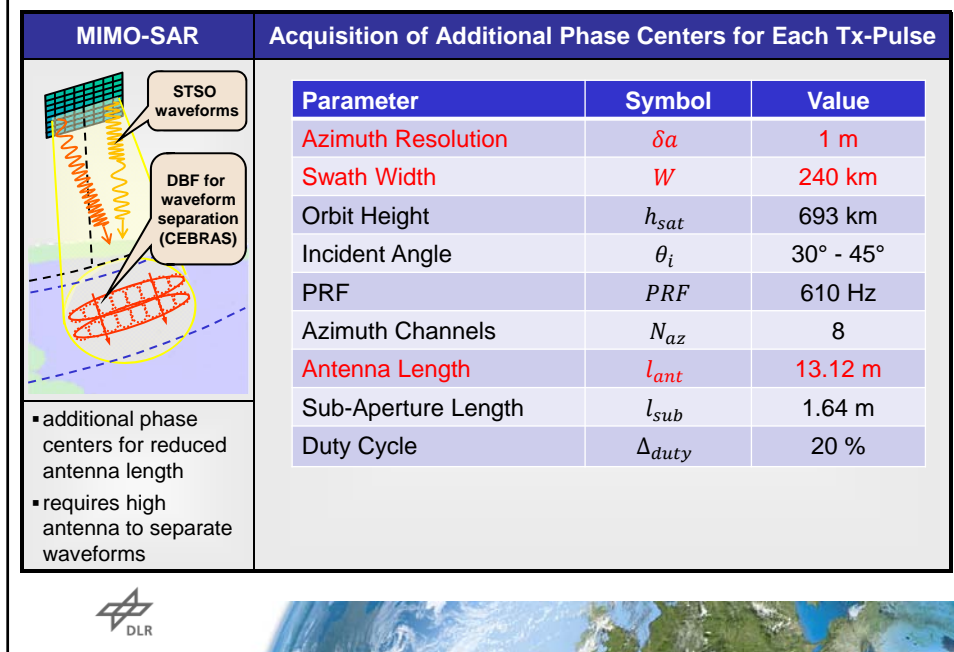
MIMO-SAR Systems with Planar Arrays



MIMO-SAR Systems with Planar Arrays

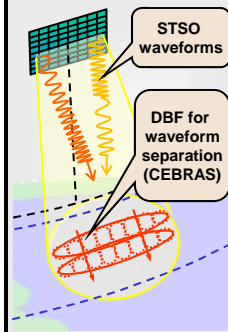


MIMO-SAR Systems with Planar Arrays



MIMO-SAR Systems with Planar Arrays

MIMO-SAR



- additional phase centers for reduced antenna length
- requires high antenna to separate waveforms

Acquisition of Additional Phase Centers for Each Tx-Pulse

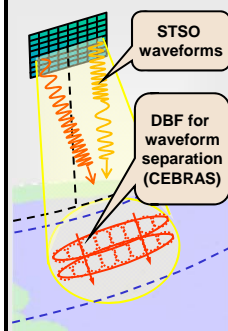
Parameter	Symbol	Value
Azimuth Resolution	δa	1 m
Swath Width	W	240 km
Orbit Height	h_{sat}	693 km
Incident Angle	θ_i	30° - 45°
PRF	PRF	610 Hz
Azimuth Channels	N_{az}	8
Antenna Length	l_{ant}	13.12 m
Sub-Aperture Length	l_{sub}	1.64 m
Duty Cycle	Δ_{duty}	20 %
STSO Interval	τ_{STSO}	164 μ s

$$\tau_{STSO} = (\Delta_{duty}/2) \cdot PRI$$



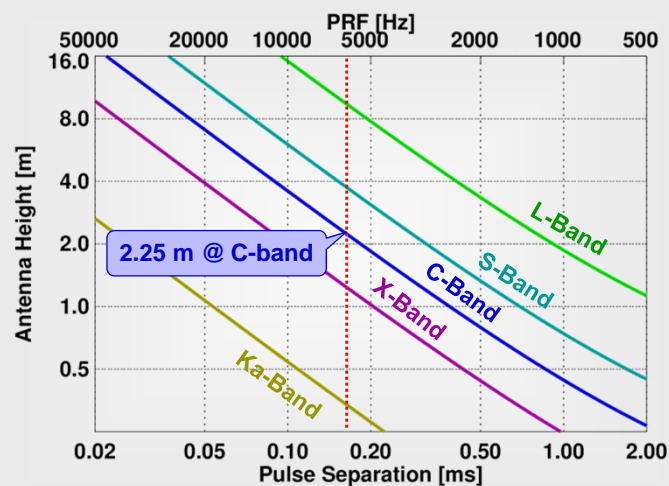
MIMO-SAR Systems with Planar Arrays

MIMO-SAR

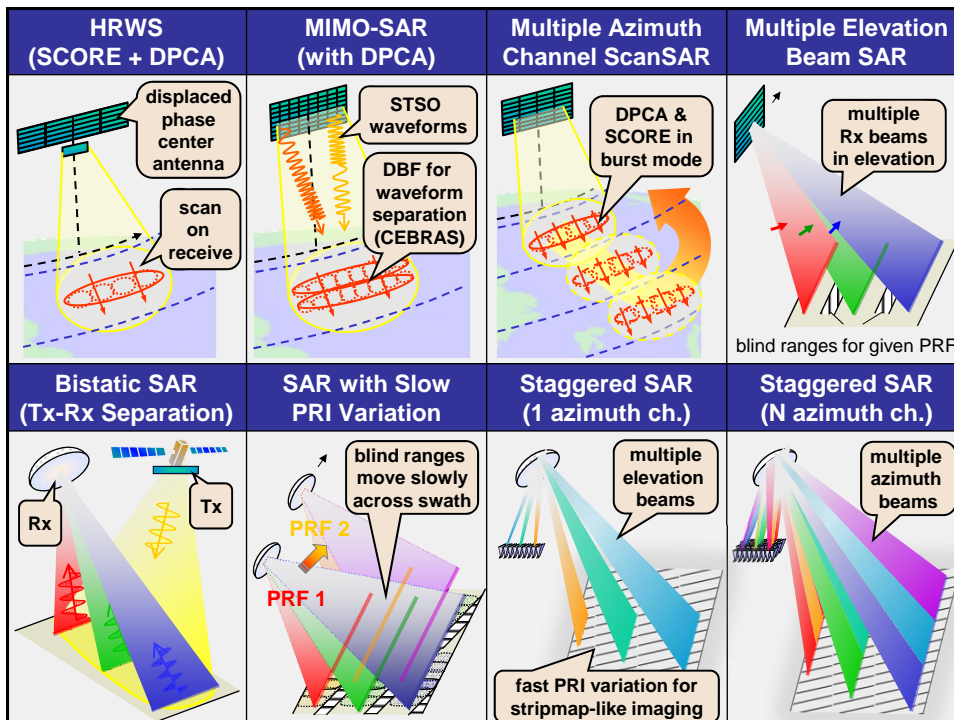
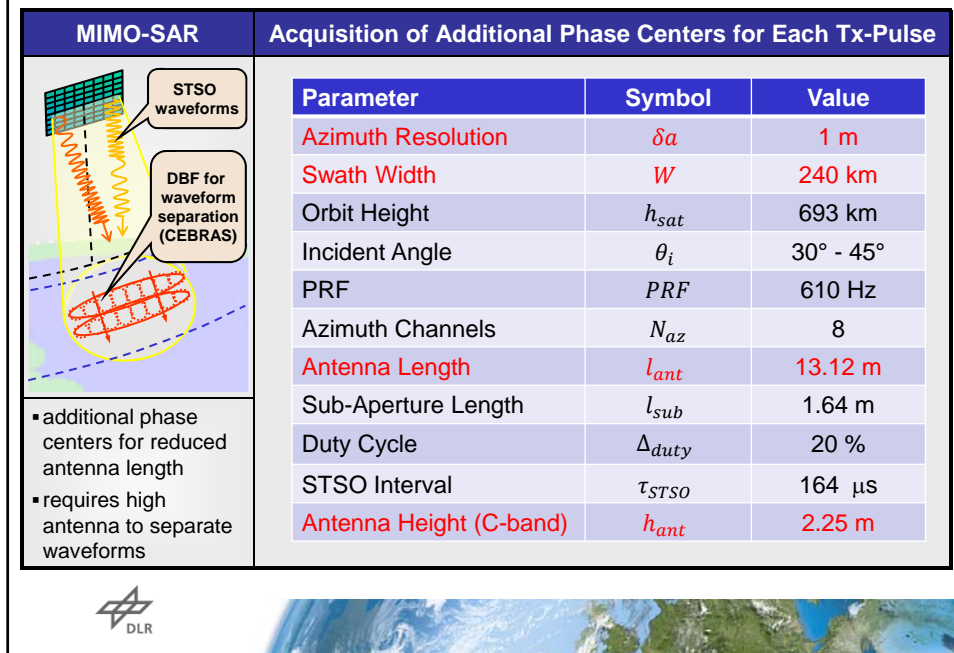


- additional phase centers for reduced antenna length
- requires high antenna to separate waveforms

Acquisition of Additional Phase Centers for Each Tx-Pulse



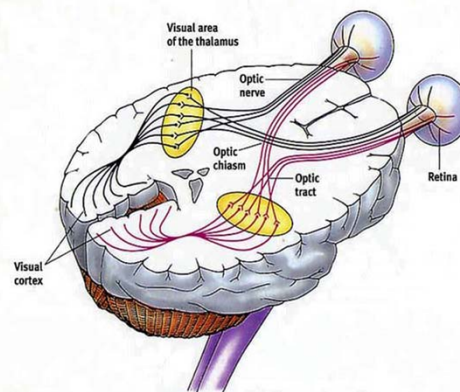
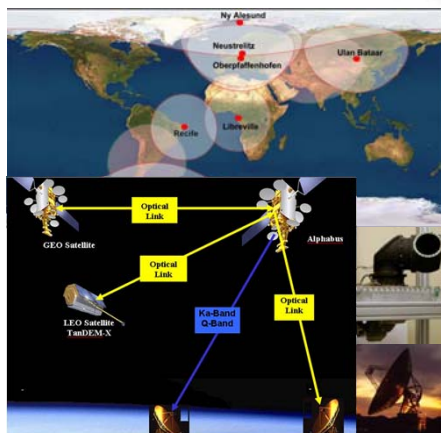
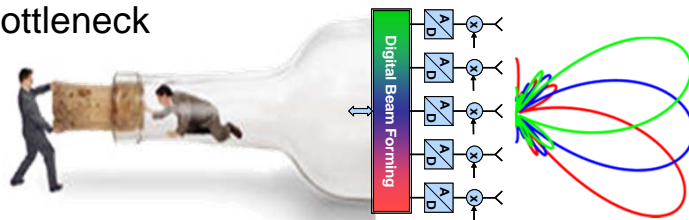
MIMO-SAR Systems with Planar Arrays

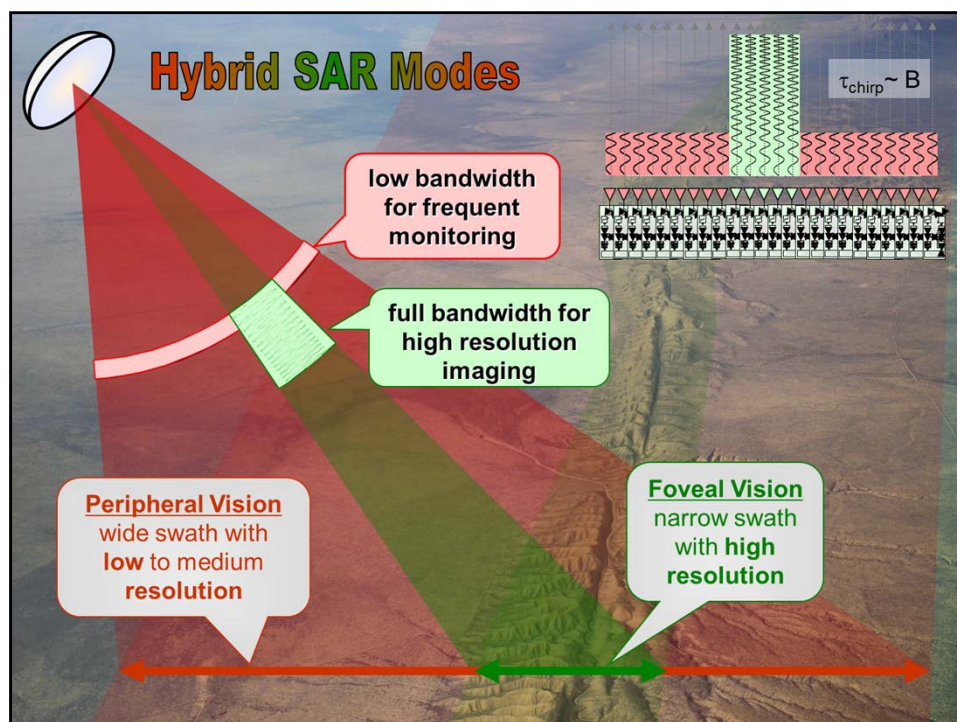
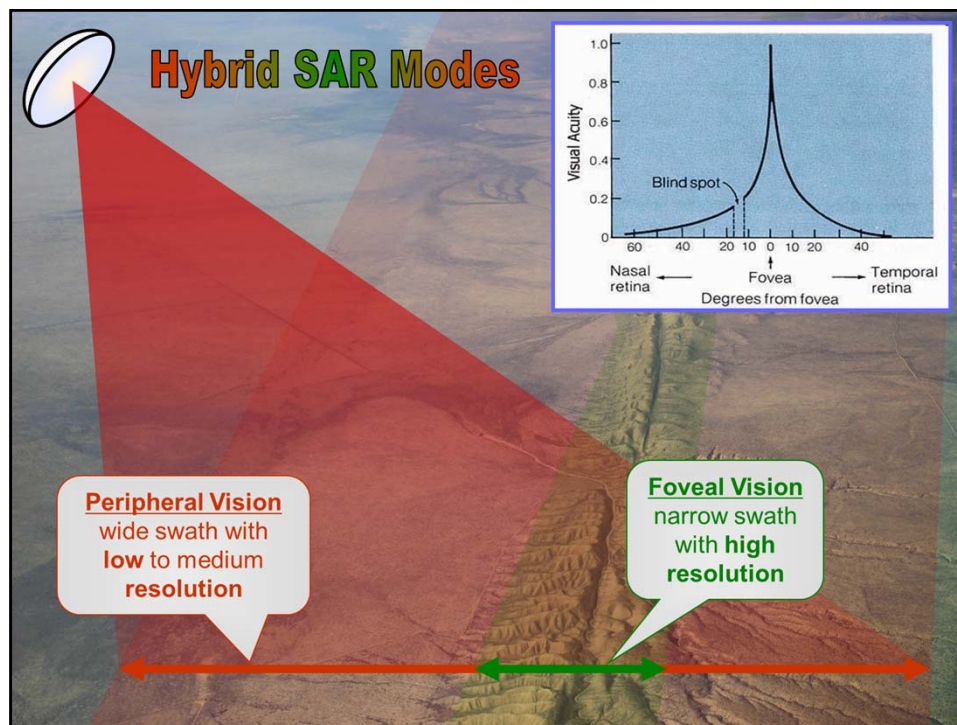


Outlook



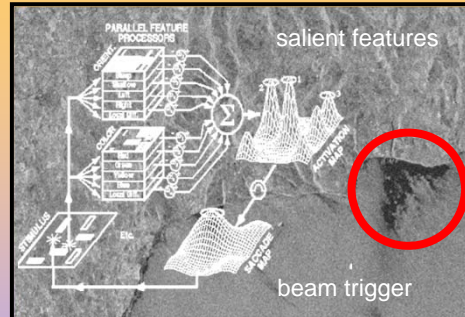
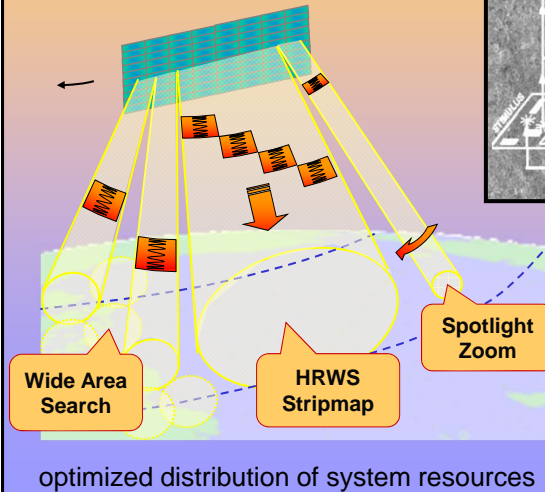
Data Bottleneck





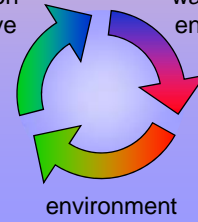
Adaptive & Cognitive MIMO-SAR Systems

maximize information gain for
a given power & data budget



DBF on
receive

waveform
encoding



Saccadic Eye Movements (Yarbus, 1967)

